## Gadgets

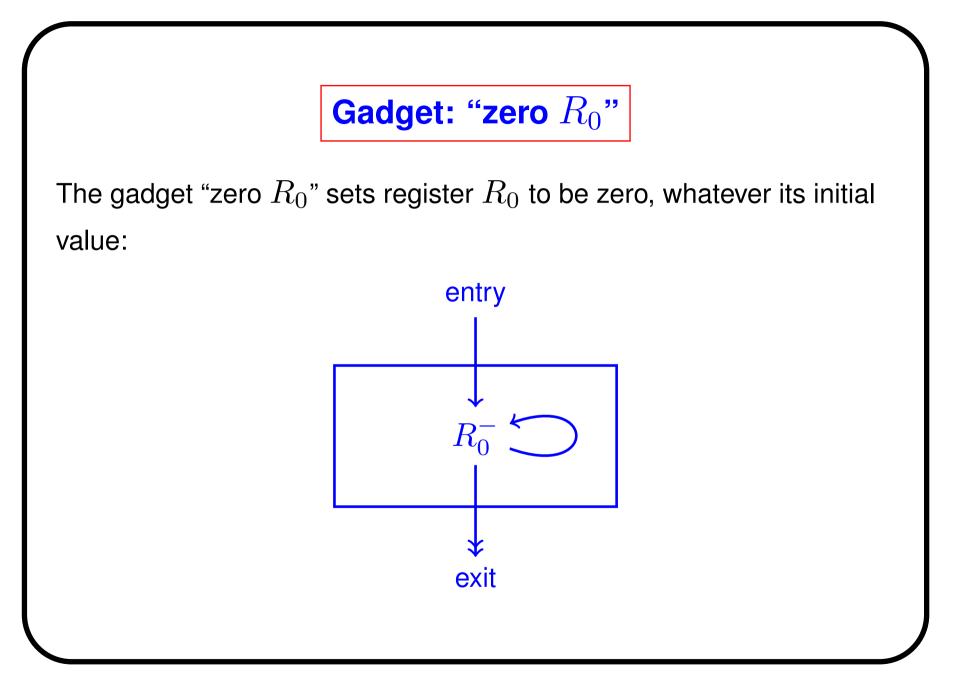
A gadget is a partial register-machine graph.

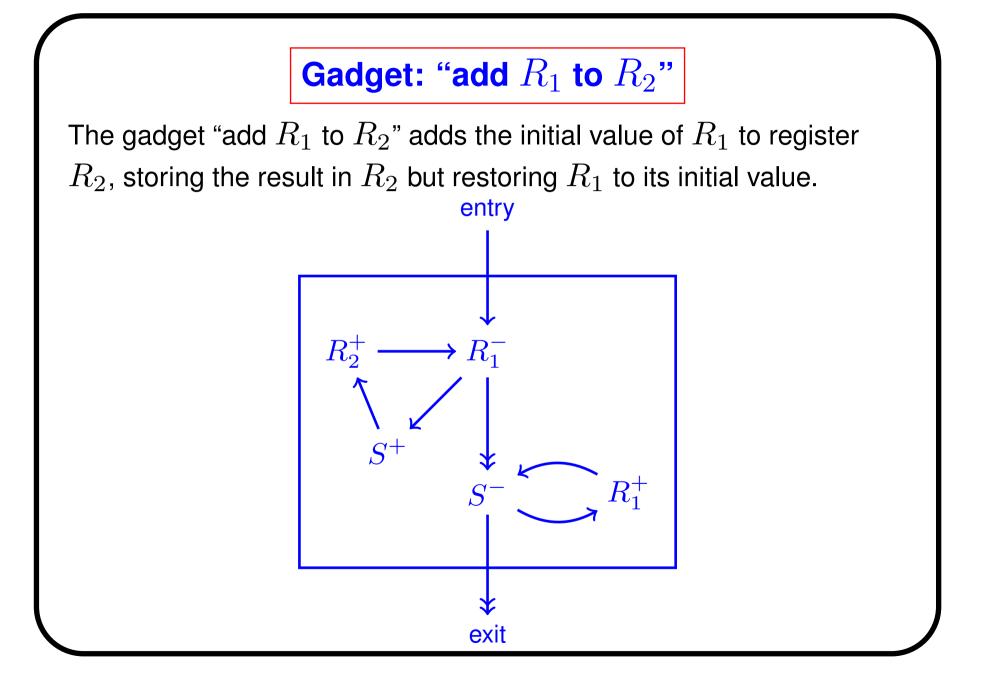
It has one entry wire, and one or more exit wires.

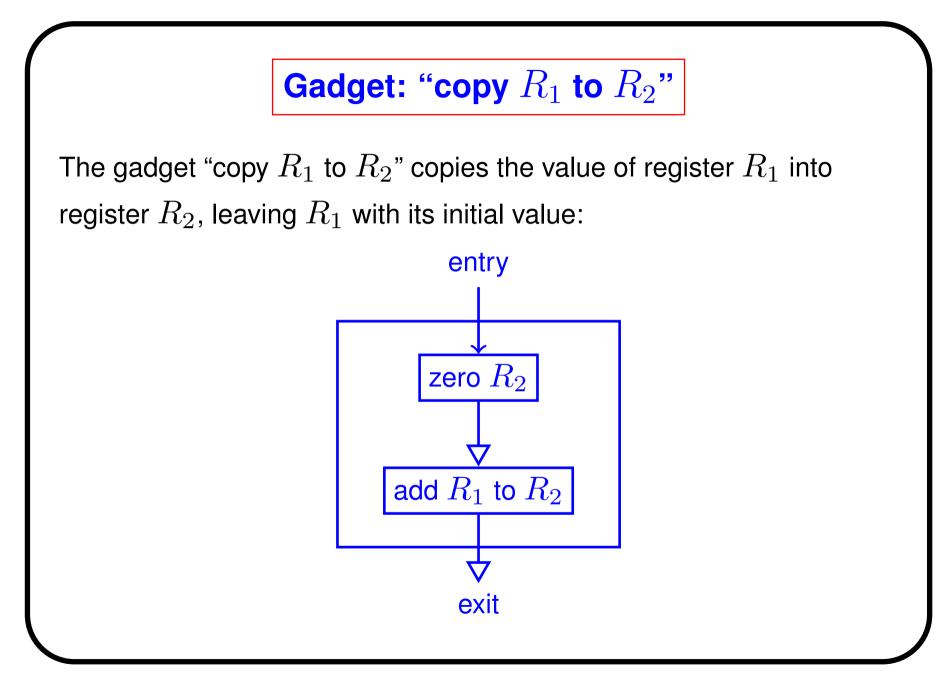
The gadget operates on input and output registers specified in the gadget's name.

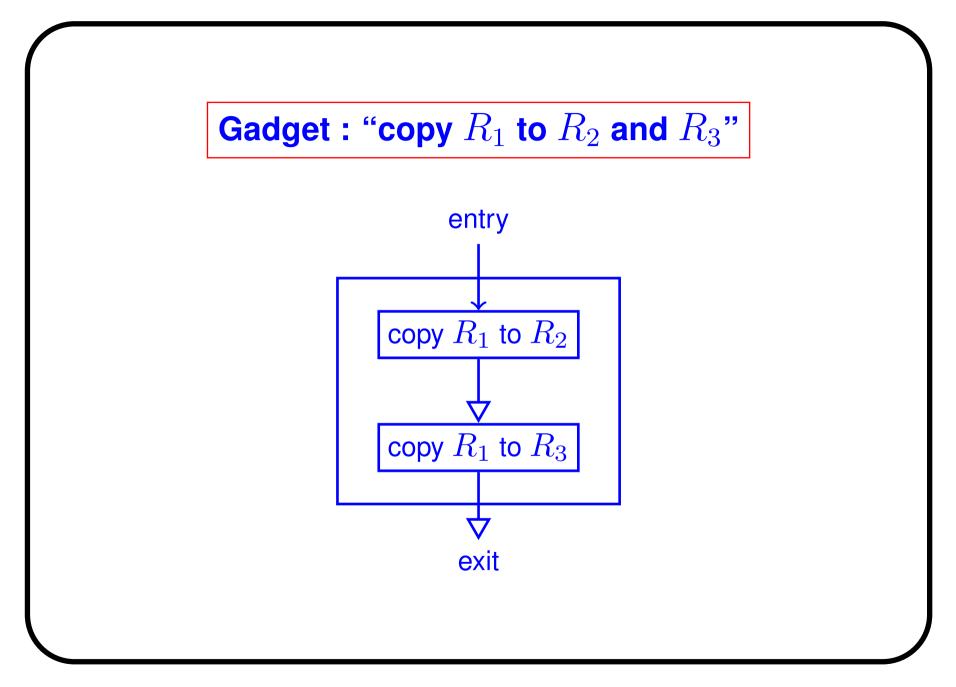
The gadget may use other registers, called scratch registers, for temporary storage.

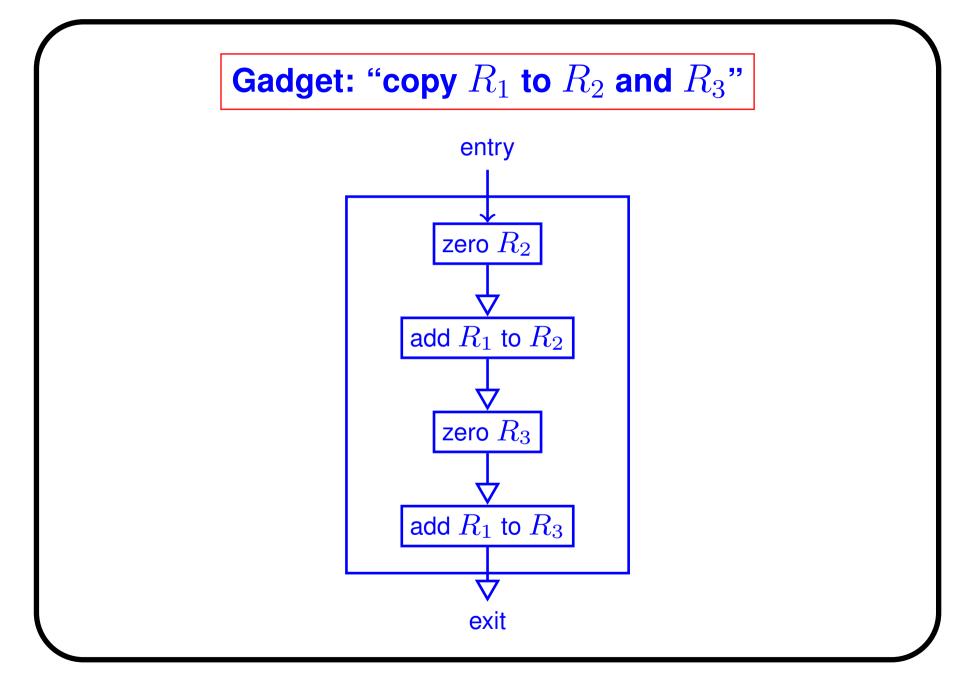
The gadget assumes the scratch registers are initially set to 0, and **must** ensure that they are set back to 0 when the gadget exits.

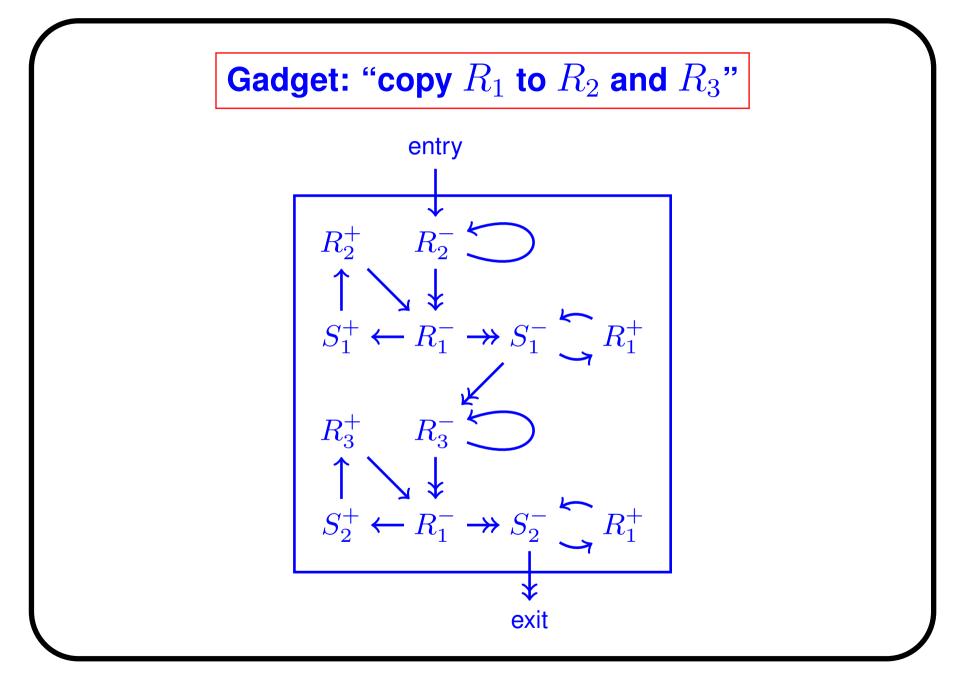


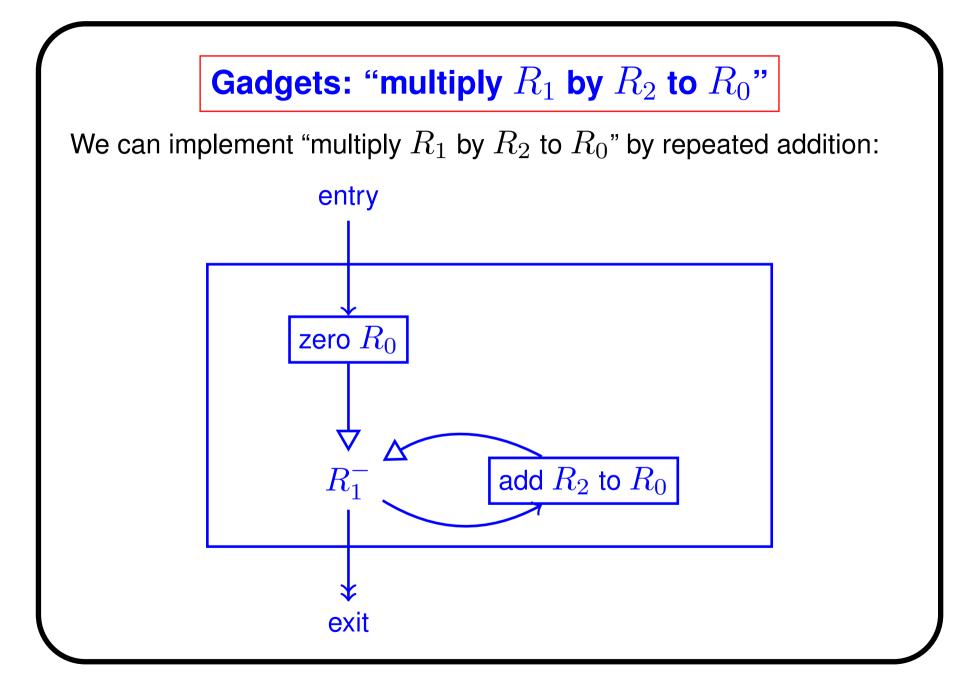


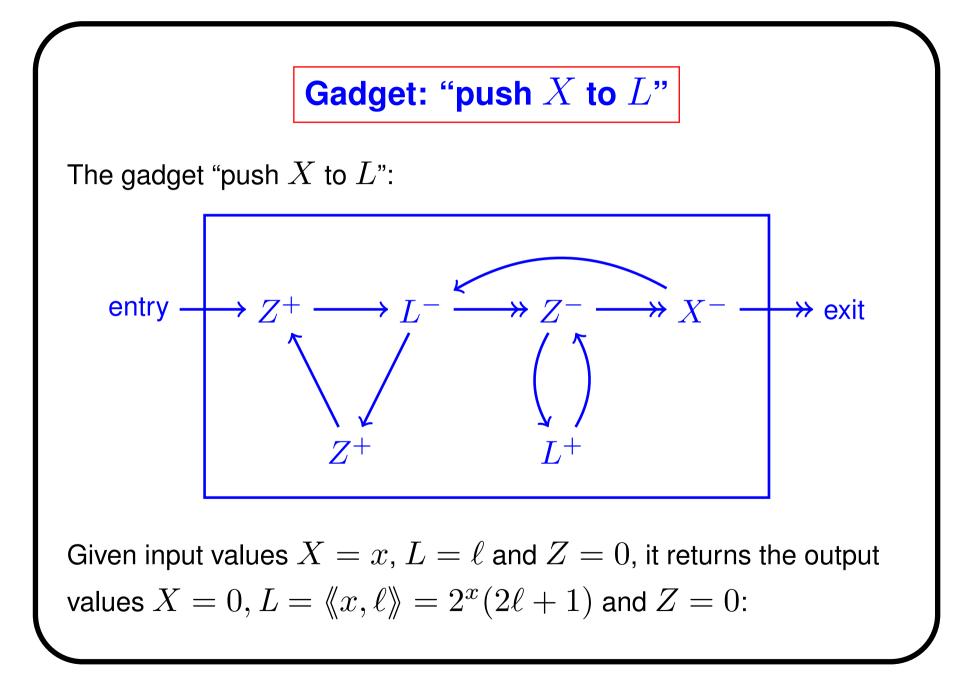


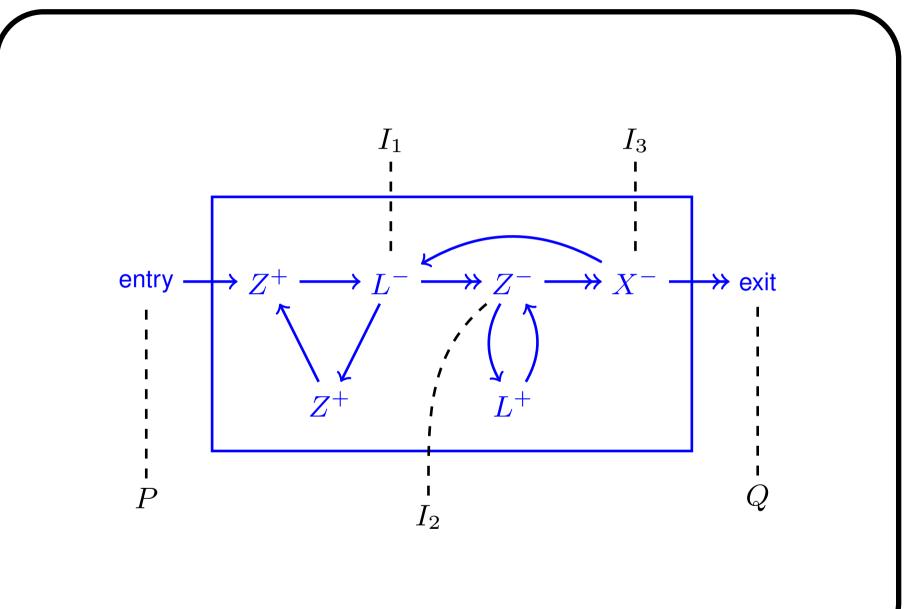




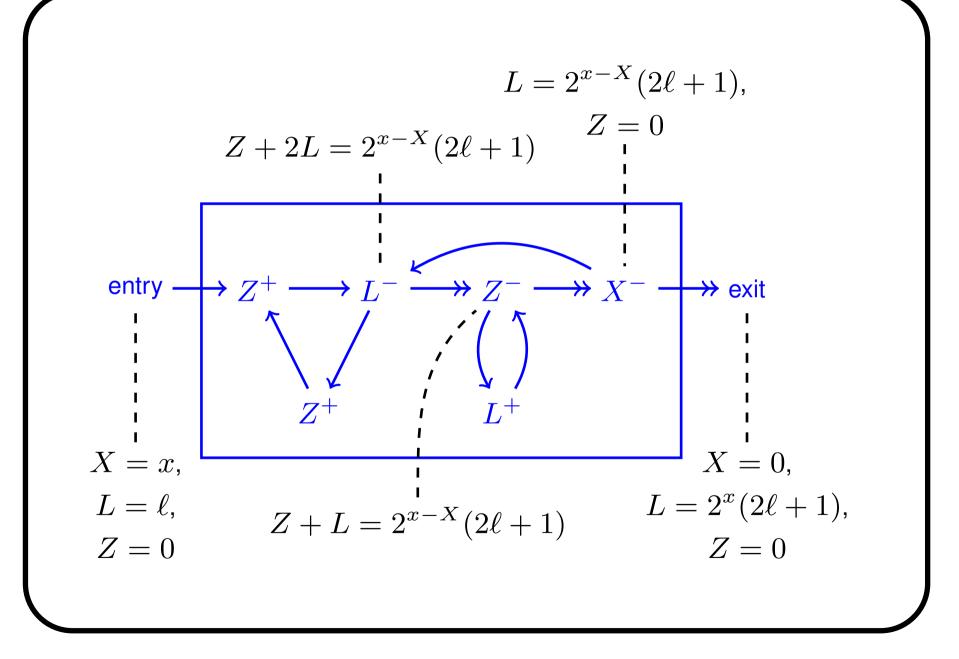


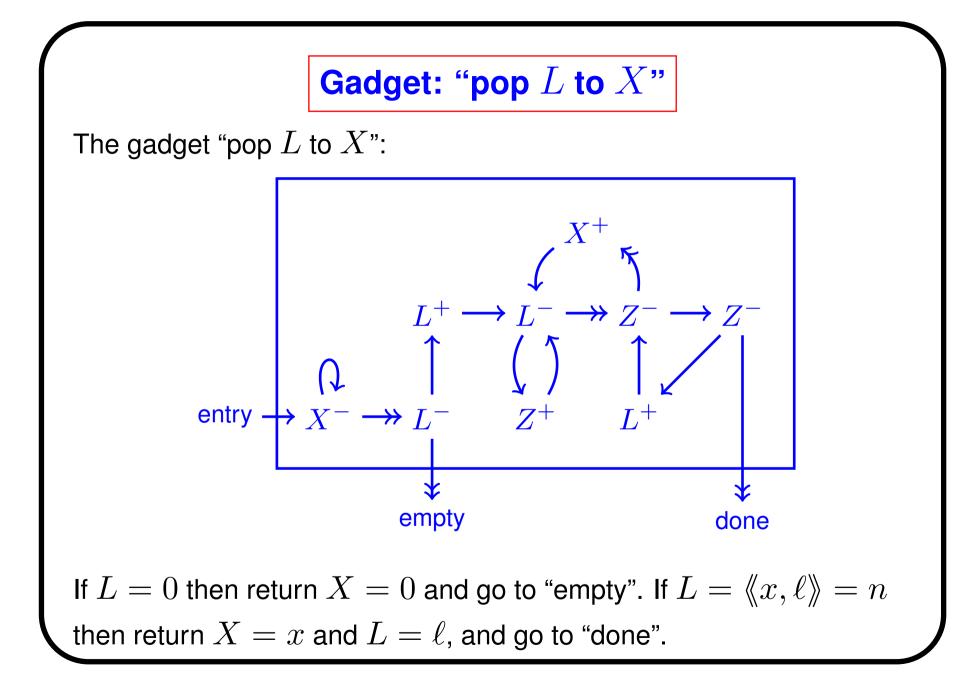


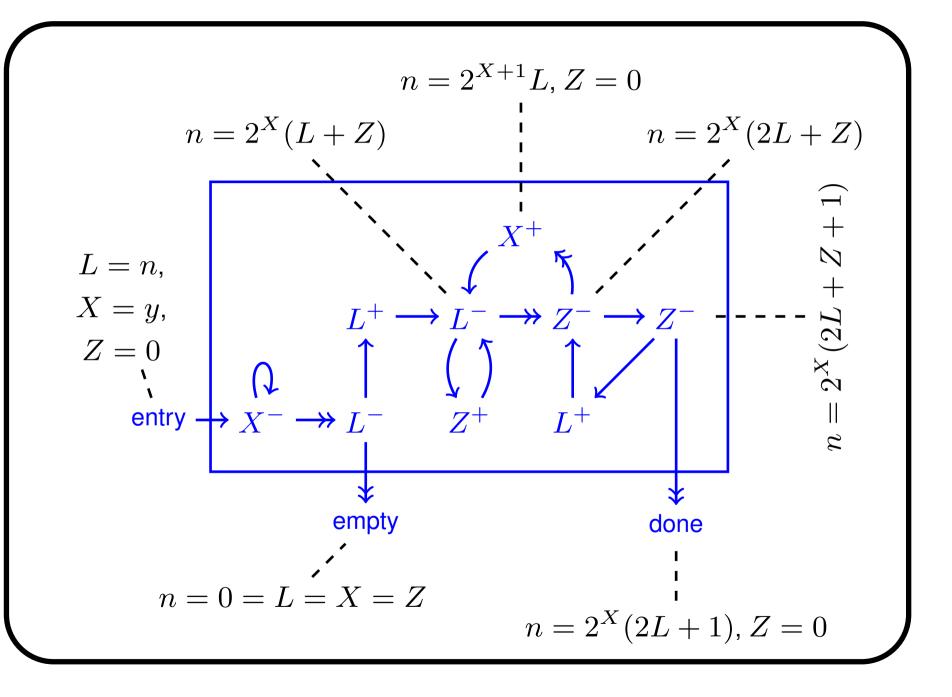


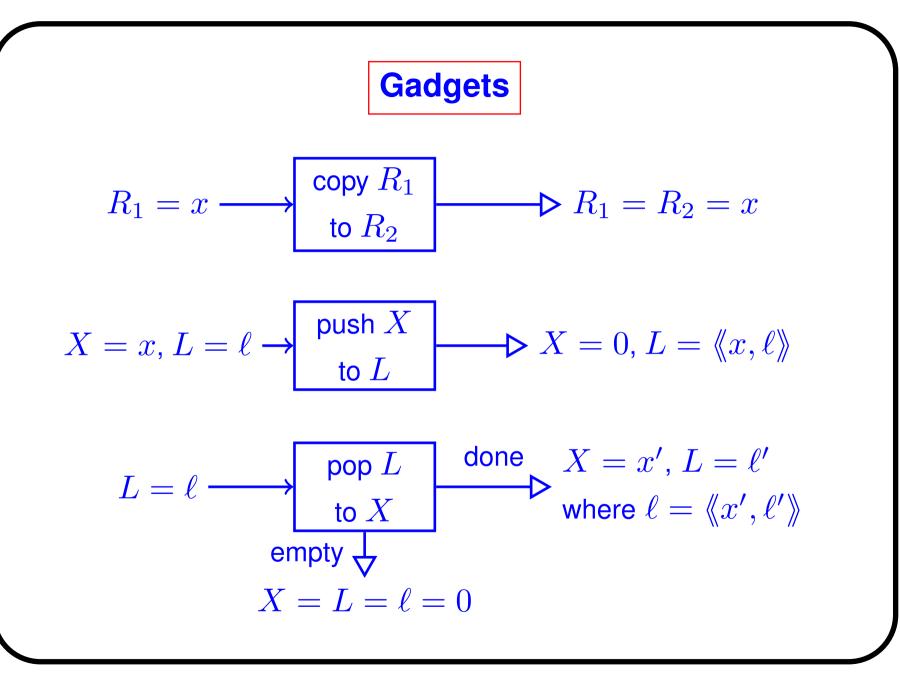


Models of Computation, 2023









## **The Universal Register Machine**

The *universal register machine* carries out the following computation, starting with  $R_0 = 0$ ,  $R_1 = e$  (code of a program),  $R_2 = a$  (code of a list of arguments) and all other registers zeroed:

- decode e as a RM program P
- decode a as a list of register values  $a_1, \ldots, a_n$
- carry out the computation of the RM program P starting with  $R_0 = 0, R_1 = a_1, \ldots, R_n = a_n$  (and any other registers occurring in P set to 0).

Mnemonics for the registers of U and the role they play in its program:

- $R_0$  result of the simulated RM computation (if any).
- $R_1 \equiv P$  Program code of the RM to be simulated

 $R_2 \equiv A$  list of RM Arguments (or register contents) of the simulated machine

- $R_3 \equiv PC$  Program Counter—label number of the current instruction
- $R_4 \equiv N$  label number(s) of the Next instruction(s)—also used to hold code of current instruction
- $R_5 \equiv C$  code of the Current instruction body

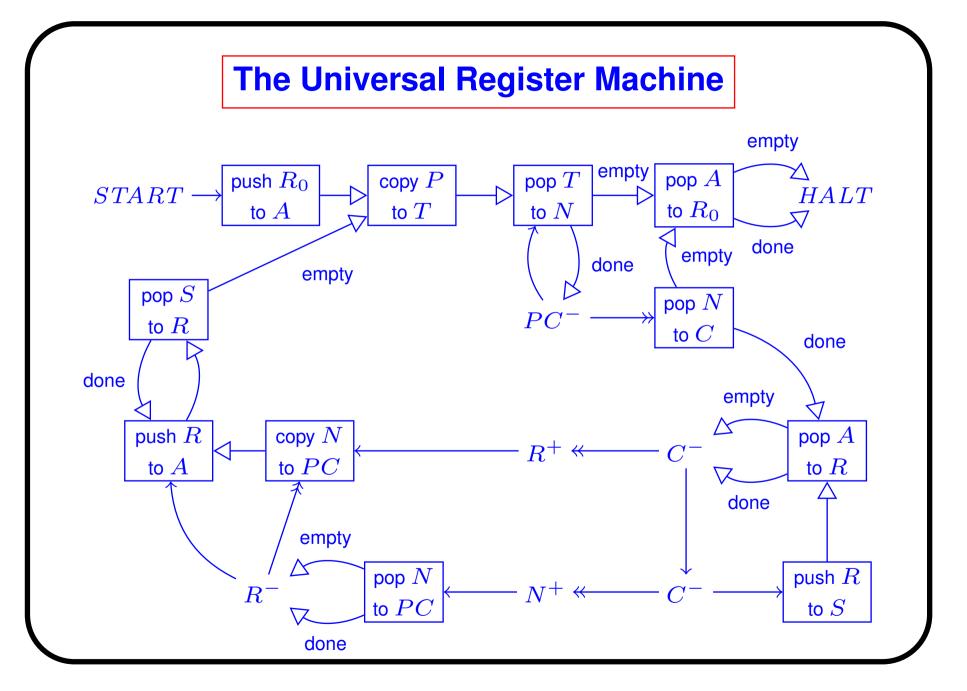
 $R_6 \equiv R$  value of the Register to be used by current instruction

 $R_7 \equiv S$  and  $R_8 \equiv T$  are auxiliary registers.

 $R_9$ ... other scratch registers.

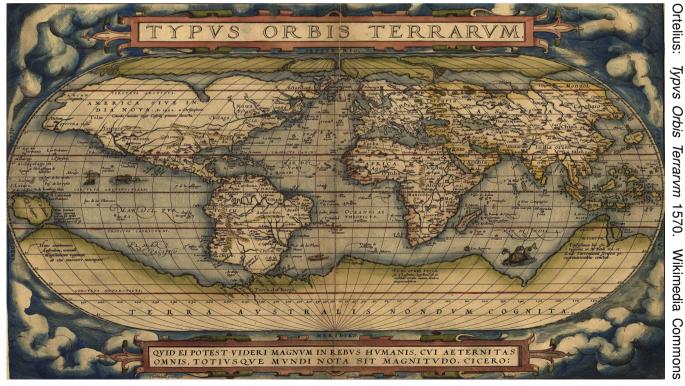


copy PC th item of list in P to N (halting if PC > length of list); goto 2 2 if N = 0 then halt, else decode N as  $\langle\!\langle y, z \rangle\!\rangle$ ; C ::= y; N ::= z; goto 3 {at this point either C = 2i is even and current instruction is  $R_i^+ \to L_z$ , or C = 2i + 1 is odd and current instruction is  $R_i^- \to L_j, L_k$  where  $z = \langle j, k \rangle$ **3** copy *i*th item of list in A to R; goto **4** 4 execute current instruction on R; update PC to next label; restore register values to A; goto **1** 



## **Universal Register Machines**

Ivan Korec: Small Universal Register Machines. Theoretical Computer Science, Volume 168 (1996), pp267–301.



Typvs Orbis Terrarvm 1570. Wikimedia Commons