

Numerical Aggregation of Trust Evidence: From Foundations to Reasoning Support

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Outline of presentation

- Motivation
- Peal: **p**luggable **e**vidence **a**ggregation **l**anguage
- Generating verification conditions for Peal
- Experimental results
- Future work and conclusions

Our Intel project aim

- understand how software annotations can generate trust evidence
- show that such evidence leads to policies that can effectively guard rail executions
- do this for both qualitative and quantitative evidence and develop verification support for this
- study programmers' intent as one source of evidence

focus of this talk



Trust evidence

- increasingly, *evidence for trust is numeric*
- e.g. *reputations* of web sites
- e.g. *age* of software
- e.g. *statistical information* about past behavior of subjects
- e.g. *probability* of one machine connecting to another





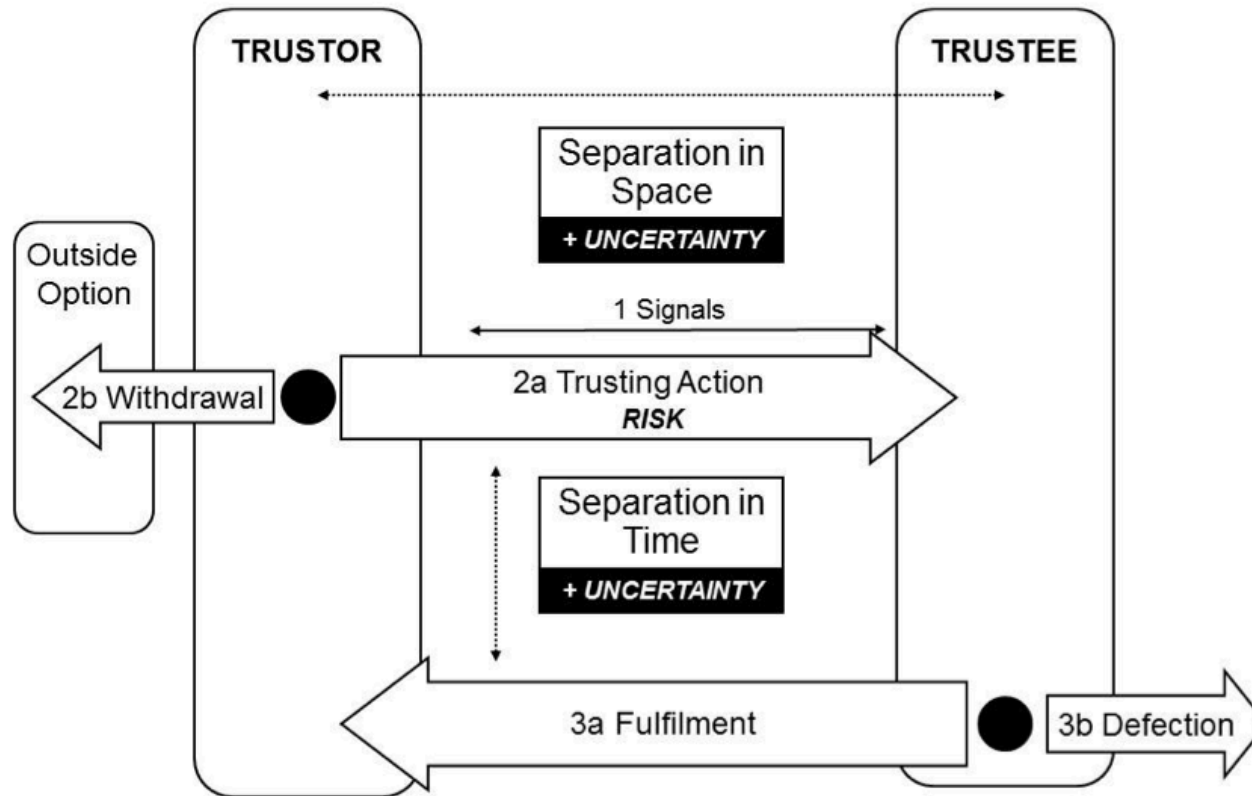
Example

- numeric evidence may be needed even in seemingly qualitative settings
- e.g. you just downloaded the MacTex 2012 package and it does not have a matching hash
- *how likely is it that this downloaded software is maliciously corrupted?*
- **conditional on which browser you use** (e.g. Chrome does things to your file!)

Numeric aggregation and its verification

- want to use numeric/non-numeric evidence to produce recommendations or obligations
- which then should inform access-control decisions
- and **at all sorts of hardware and software interfaces** (e.g. forgetful loaders, social networks, infrastructure integrity, risk postures of organizations)
- how can we verify such aggregation and what does verification mean here?

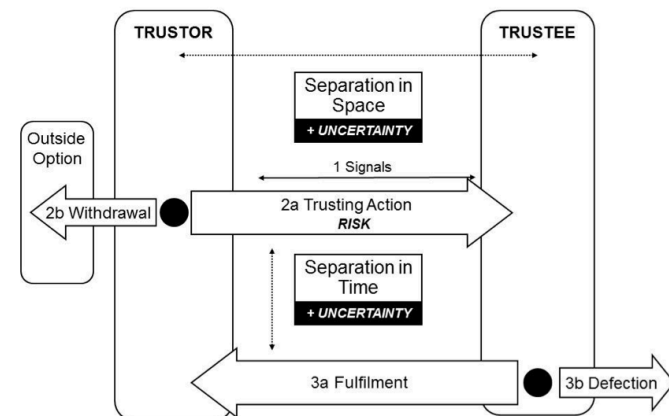
Trust-mediated Interactions



Jens Riegelsberger, Martina Angela Sasse, and John D. McCarthy. The mechanics of trust: A framework for research and design. *Int. J. Hum.-Comput. Stud.*, 62(3):381–422, 2005.

Trust & Assurance

- **Economic incentive to use trust:** assurance techniques are expensive
- But **trust signals less reliable in digital domain**
- *Want to use such signals and combine them with assurance techniques*
- ... and in a tuneable manner



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Policies as blocks of aggregated trust signals

$op ::= + \mid \min \mid \max \mid * \mid \dots$

$rule ::= \text{if } (q) \text{ score}$

$pol ::= op(rule^*) \text{ default score}$

scope for extensions



- policy (pol) returns a score:
- first, collect all scores of rules in policy whose predicate (i.e. *trust or distrust signal* q) is true
- second, apply op to all these scores to get result; if no q is true, return default score

Full Peal syntax

$op ::= + \mid * \mid \min \mid \max \mid \dots$

$rule ::= \text{if } (q) \text{ score}$

$pol ::= op(rule^*) \text{ default score}$

$pSet ::= pol \mid \max(pSet, pSet) \mid$
 $\min(pSet, pSet)$

$cond ::= th < pSet \mid pSet \leq th$

- *op* aggregates scores of true predicates in policy
- policy isA policy set, combine policy sets (*pSet*) with *min* or *max*
- *cond*: compares values of *pSet* with thresholds

Example

- Alice wants to pay Bob via PayPal on Facebook

$$b_1 = +((\text{if } (\text{lowCostTransaction } 0.3) (\text{if } \text{enoughMutualFriends } 0.1) \\ (\text{if } \text{enoughMutualFriendsNormalized } 0.2)) \text{ default } 0)$$
$$b_2 = \min((\text{if } (\text{highCostTransaction } 0.1) (\text{if } \text{aFriendOfAliceUnfriendedBob } 0.2) \\ (\text{if } \text{aFriendOfAliceVouchesForBob } 0.6)) \text{ default } 1)$$
$$\text{cond} = 0.5 < \min(b_1, b_2)$$


Analysis example:

Does the behavior of cond change when threshold 0.5 changes to 0.6?

Definition of signals

lostCostTransaction = (amountAlicePays < 100)

highCostTransaction = (1000 < amountAlicePays)

enoughMutualFriends = (4 < numberOfMutualFriends)

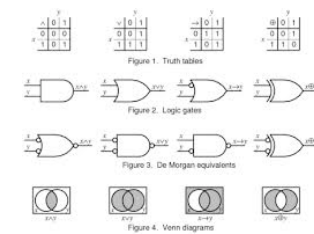
*enoughMutualFriendsNormalized = (numberOfBobsFriends <
100 * numberOfMutualFriends)*

- transaction risk relies on amount that Alice means to pay, **amount of 500 does not signal anything!**
- other signals also **rely on state of relationship graph**, e.g. the number of mutual friends
- Last predicate protects against Bob having way too many friends (e.g. celebrity)

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Logical synthesis



- For each *cond* (“*th* < *pSet*” or “*pSet* <= *th*”):
synthesize propositional formula $\Phi[cond]$ over q
- **Models** = determine truth values of predicates q
- $\Phi[cond]$ is true in model iff *cond* holds in model
- Synthesized $\Phi[cond]$ is **basis for verification tasks**
- predicates q themselves are/representable as **formulas of first-order logic**

Verification tasks

- Is $\Phi[cond]$ always true/false? **Vacuity checking**
- Do $\Phi[th < pSet]$ and $\Phi[th' < pSet]$ differ? **Sensitivity analysis**
- Is $cond$ **persistent**, i.e. incomplete requests will grant access only if complete one would?

These and more complex verification tasks reduce to satisfiability checks of $\Phi[cond]$ in logic over predicates q



Analyze instrumentations of $\Phi[cond]$

- Is $\Phi[cond]$ always false? Satisfiability checking of that formula, then negate result
- Is $\Phi[cond]$ always true? Satisfiability checking of negation of that formula, then negate result
- Do $\Phi[th < pSet]$ and $\Phi[th' < pSet]$ differ, when $th < th'$? Satisfiability checking of $\Phi[th < pSet] \ \&\& \ !\Phi[th' < pSet]$

Etc. But satisfiability checks have to recognize logical dependencies of predicates q within $pSet$

SMT solvers



- SMT solvers: combine SAT solvers (“model checking”) with logical reasoning over theories (theorem proving)
- we have first prototype verification tool using [SMT solver Z3 \(Microsoft Research\)](#)
- below we will explore tradeoff between explicit synthesis of $\Phi[cond]$ (space intensive) and synthesis of symbolic version of $\Phi[cond]$
- but first we provide idea and usage of SMT solvers, using Z3 as an example

Simple Z3 code

```
(declare-const a Int) ; example from Z3 documentation
(declare-fun f (Int Bool) Int)
(assert (> a 10))
(assert (< (f a true) 100))
(check-sat)
```

- declares an integer, and a function that maps an (Int Bool) pair to an integer
- declares two assertions: a is greater than 10, and the value f(a,true) is less than 100
- (check-sat) directive to decide whether there is a **model for conjunction of all assertions**

Z3 witnesses

```
(declare-const a Int) ; example from Z3 documentation
(declare-fun f (Int Bool) Int)
(assert (> a 10))
(assert (< (f a true) 100))
(check-sat)
(get-model)
```

- (get-model) constructs witness of satisfiability, reports exception if no such model exists

```
sat
(model
  (define-fun a () Int
    11)
  (define-fun f ((x!1 Int) (x!2 Bool)) Int
    (ite (and (= x!1 11) (= x!2 true)) 0
          0))
)
```

Scoping in Z3

```
(declare-const x Int) ; example from Z3 documentation
(declare-const y Int)
(declare-const z Int)
(push)
(assert (= (+ x y) 10))
(assert (= (+ x (* 2 y)) 20))
(check-sat)
(pop) ; remove the two assertions
(push)
(assert (= (+ (* 3 x) y) 10))
(assert (= (+ (* 2 x) (* 2 y)) 21))
(check-sat)
(declare-const p Bool)
(pop)
(assert p) ; error, as declaration of p was removed from the stack
```

Each analysis in our tool wrapped in a push/pop frame

Predicate definitions in Z3

```
DOMAIN_SPECIFICS
(declare-const amountAlicePays Real)
(declare-const numberOfMutualFriends Int)
(declare-const numberOfBobsFriends Int)
(assert (= lowCostTransaction (> 100.0 amountAlicePays)))
(assert (= enoughMutualFriends (< 4 numberOfMutualFriends)))
(assert (= enoughMutualFriendsNormalized
          (< numberOfBobsFriends (* 100 numberOfMutualFriends))))
(assert (= highCostTransaction (> amountAlicePays 1000.0)))
```

- Our tool for Peal verification has text zone in which such domain specifics can be added

Possible Z3 answers

- Some theories and their combination are decidable over first-order logic
- *Even if not, conjunction of all assertions may still be decided in instances*
- “sat” means that conjunction has model
- “unsat” means that conjunction has no model
- “unknown” means Z3 does not know which is the case

Explicit synthesis

- Generate verification condition $\Phi[cond]$ by translating away all references to numerics
- Captures logical nature of condition
- Output is amenable to analysis with an SMT solver
- SMT solver will *correctly reflect logical dependencies of predicates within/across policies*

Explicit synthesis for *pSet* composition

- Induction on min/max compositions
- Encodes order properties of min/max

$$\phi[\min(pS_1, pS_2) \leq th] \stackrel{\text{def}}{=} \phi[pS_1 \leq th] \vee \phi[pS_2 \leq th]$$

$$\phi[\max(pS_1, pS_2) \leq th] \stackrel{\text{def}}{=} \phi[pS_1 \leq th] \wedge \phi[pS_2 \leq th]$$

$$\phi[th < \min(pS_1, pS_2)] \stackrel{\text{def}}{=} \phi[th < pS_1] \wedge \phi[th < pS_2]$$

$$\phi[th < \max(pS_1, pS_2)] \stackrel{\text{def}}{=} \phi[th < pS_1] \vee \phi[th < pS_2]$$

$x < \max(a, b)$
iff $(x < a)$ or $(x < b)$



Synthesis of defaults

- $pol = op((q_1 s_1) \dots (q_n s_n))$ **default s**
- reflect whether default is possible or not

non-default case

$$\begin{aligned} \phi[pol \leq th] &\stackrel{\text{def}}{=} \left(\bigwedge_{i=1}^n \neg q_i \right) \vee \phi_{op}^{ndf}[pol \leq th] && (s \leq th) \\ \phi[pol \leq th] &\stackrel{\text{def}}{=} \left(\bigvee_{i=1}^n q_i \right) \wedge \phi_{op}^{ndf}[pol \leq th] && (th < s) \\ \phi[th < pol] &\stackrel{\text{def}}{=} \left(\bigwedge_{i=1}^n \neg q_i \right) \vee \phi_{op}^{ndf}[th < pol] && (th < s) \\ \phi[th < pol] &\stackrel{\text{def}}{=} \left(\bigvee_{i=1}^n q_i \right) \wedge \phi_{op}^{ndf}[th < pol] && (s \leq th) \end{aligned}$$

Synthesis of defaults

- default s **consistent with threshold**:
conjunction of all negated q_i as one disjunct
- otherwise, ensure at least one q_i be true

$$\phi[pol \leq th] \stackrel{\text{def}}{=} \left(\bigwedge_{i=1}^n \neg q_i \right) \vee \phi_{op}^{ndf}[pol \leq th] \quad (s \leq th)$$

$$\phi[pol \leq th] \stackrel{\text{def}}{=} \left(\bigvee_{i=1}^n q_i \right) \wedge \phi_{op}^{ndf}[pol \leq th] \quad (th < s)$$

$$\phi[th < pol] \stackrel{\text{def}}{=} \left(\bigwedge_{i=1}^n \neg q_i \right) \vee \phi_{op}^{ndf}[th < pol] \quad (th < s)$$

$$\phi[th < pol] \stackrel{\text{def}}{=} \left(\bigvee_{i=1}^n q_i \right) \wedge \phi_{op}^{ndf}[th < pol] \quad (s \leq th)$$

consistent 

inconsistent 

Polarity of synthesis

- *want witnessing sets of predicates to be closed under supersets*
- X contained in Y implying $op(X) \leq op(Y)$ means *op is monotone*; in that case

$$\phi_{op}^{ndf} [pol \leq th] \stackrel{\text{def}}{=} \neg \phi_{op}^{ndf} [th < pol]$$

- X contained in Y implying $op(Y) \leq op(X)$ means *op is anti-tone*; in that case

$$\phi_{op}^{ndf} [th < pol] \stackrel{\text{def}}{=} \neg \phi_{op}^{ndf} [pol \leq th]$$

Monotone: op is max

- $pol = max((q_1 s_1) \dots (q_n s_n))$ default s
- $th < pol$ if for some q_i inequality $th < s_i$ is true
- last slide: reduce $pol \leq th$ to $th < pol$ case

$$\phi_{op}^{ndf} [th < pol] \stackrel{\text{def}}{=} \bigvee_{i|th < s_i} q_i$$

$$\phi_{op}^{ndf} [pol \leq th] \stackrel{\text{def}}{=} \neg \phi_{op}^{ndf} [th < pol]$$

Anti-tone: op is min

- $pol = min((q1\ s1) \dots (qn\ sn))$ default s
- $pol \leq th$ if there is some qi with $si \leq th$
- now reduce $th < pol$ to $pol \leq th$ case

$$\phi_{op}^{ndf} [pol \leq th] \stackrel{\text{def}}{=} \bigvee_{i|s_i \leq th} q_i$$

$$\phi_{op}^{ndf} [th < pol] \stackrel{\text{def}}{=} \neg \phi_{op}^{ndf} [pol \leq th]$$

Monotone: op is $+$

- let pol be $+((q_1 s_1) \dots (q_n s_n))$ default s
- sort predicates q_i in pol by **ascending score order**, e.g. the vector $[0.1, 0.2, 0.2, 0.3, 0.5]$
- want to find **minimal index sets** $\{i, \dots, j\}$ of predicates whose score sum is greater than 0.5 (" $0.5 < pol$ "), say
- here: $M1 = \{\{4,5\}, \{3,5\}, \{2,5\}, \{2,3,4\}, \{1,3,4\}, \{1,2,4\}\}$
- explore from highest score, expand only if partial sum $t_i = s_0 + \dots + s_i$ can get current mass over threshold 0.5

Computing all minimal index sets: $M1$

unit of +
current index set

call $\text{enumOne}(\{\}, 0, n+1, +)$ for n rules where $t_i = s_0 + \dots + s_i$

explore indexes less than this

aggregation operator

```
enumOne(X, acc, index, op) {  
  if (th < acc) { output X; }  
  else {  
    j = index - 1;  
    while ((0 < j) ∧ (th < op(acc, tj)) {  
      enumOne(X ∪ {j}, op(acc, sj), j, op);  
      j = j - 1; }  
  }
```


Example trace

th = 0.5, **s** = [0.1,0.2,0.2, 0.3, 0.5], **t** = [0.1,0.3,0.5,0.8,1.3]

enumOne({},0,6,+)

enumOne({5},0.5,5,+)

enumOne({5,4},0.8,4,+)
--> {5,4}

enumOne({5,3},0.7,3,+)
--> {5,3}

enumOne({5,2},0.7,2,+)
--> {5,2}

enumOne({5,1},0.6,1,+)
--> {5,1}

enumOne({4},0.3,4,+)

enumOne({4,3},0.5,3,+)

enumOne({4,3,2},0.7,2,+)
--> {4,3,2}

enumOne({4,3,1},0.6,1,+)
--> {4,3,1}

enumOne({4,2},0.5,2,+)

enumOne({4,2,1},0.6,1,+)
--> {4,2,1}

Non-default formula for \neq

- $pol = +((q1\ s1) \dots (qn\ sn))\ default\ s$
- sort rules so that $s0 \leq s1 \leq \dots \leq sn$
- use `enumerateOne` to generate $M1$ below

$$\phi_{op}^{ndf} [th < pol] \stackrel{\text{def}}{=} \bigvee_{X \in \mathcal{M}_1} \bigwedge_{i \in X} q_i$$

Anti-tone: op is $*$

- let pol be $*((q_1 s_1) \dots (q_n s_n))$ default s
- **Need:** scores in $[0, 1]$; so multiplication $*$ is **anti-tone**; sort scores in pol by **descending** order
- find minimal index sets $\{i, \dots, j\}$ of q_i whose score sum is $\leq th$; M_2 = set of such minimal index sets
- explore from **lowest** score, recurse only if partial product t_i can get current mass **below** threshold th

$$\phi_{op}^{ndf} [pol \leq th] \stackrel{\text{def}}{=} \bigvee_{X \in M_2} \bigwedge_{i \in X} q_i$$

Computing all minimal index sets: *M2*

call `enumTwo({}, 1, n+1, *)` for n rules where `unit = 1`
`enumTwo` only reverses “th” comparisons of `enumOne`

```
enumTwo(X, acc, index, op) {  
  if (acc ≤ th) { output X; }  
  else {  
    j = index - 1;  
    while ((0 < j) ∧ (op(acc, tj) ≤ th) {  
      enumTwo(X ∪ {j}, op(acc, sj), j, op);  
      j = j - 1; }  
  }
```

Example: Z3 code

- policies b1, b2 composed with max, satisfiability of “cond” explored

cond = pSet <= 0.5

b1 = min ((q1 0.2) (q2 0.4) (q3 0.9)) default 1

b2 = + ((q4 0.1) (q5 0.2) (q6 0.2)) default 0

pSet = max(b1, b2)

(declare-const q4 Bool) ... ; declare variables/functions
(assert (and (and (or q1 q2 q3) (or q1 q2)) (or (and (not q4)
(not q5) (not q6)) (not false)))) ; synthesised formula in red
(check-sat) ; directive to check for satisfiability
(get-model) ; extraction of witness if satisfiable

Parse tree of assertion

$$\text{cond} = \text{pSet} \leq 0.5$$

$$b1 = \min((q1 \ 0.2) (q2 \ 0.4) (q3 \ 0.9)) \text{ default } 1$$

$$b2 = +((q4 \ 0.1) (q5 \ 0.2) (q6 \ 0.2)) \text{ default } 0$$

$$\text{pSet} = \max(b1, b2)$$

max ≤ 0.5

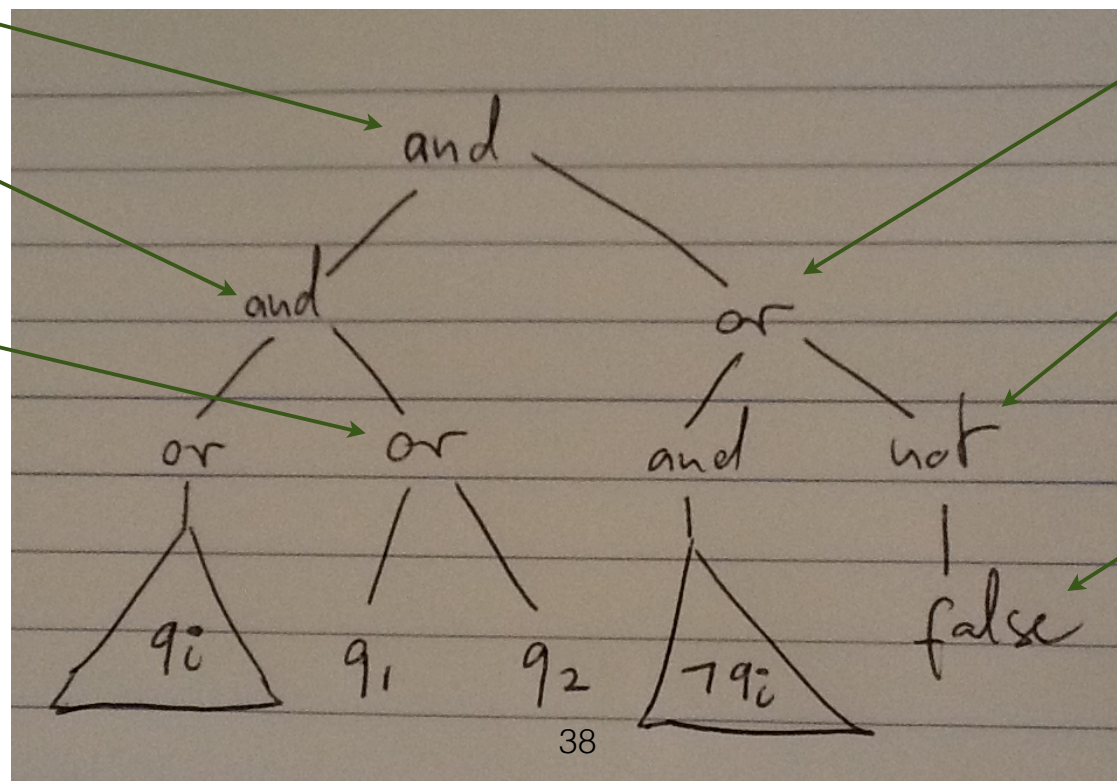
**inconsistent
default score**

**qi with
si ≤ 0.5**

**consistent
default score**

**make +
monotone**

M1 empty



Naming mechanisms

- use simple naming mechanism for all syntactic categories: policies, policy sets, conditions, and analyses
- E.g. we actually bind **condition names** to **formulas** in asserts, as in

```
(assert (= cond (and (and (or  
q1 q2 q3) (or q1 q2)) (or (and  
(not q4) (not q5) (not q6)) (not  
false))))))
```

DEMO of web app

1. Enter policies, policy sets, conditions, and analyses in the text area below:

Or click on one of the blue buttons to generate a valid input

Constant-score sample

Non-constant score sample

Majority-voting sample, n =

Random sample without domain specifics: n, m_min, m_max, m_+, m_*, p, th, delta

Random sample with domain specifics: n, m_min, m_max, m_+, m_*, p, th, delta

Clear text area

```
pSet2 = min(b1, b2)
CONDITIONS
cond1 = pSet1 <= 0.5
cond2 = 0.6 < pSet2
cond3 = cond1 && cond2
cond4 = cond1 || cond2
cond5 = !cond4
cond6 = true
cond7 = false
DOMAIN_SPECIFICS
(declare-const a Real)
(declare-const b Real)
(assert (= q1 (< a (+ b 1))))
ANALYSES
name1 = always_true? cond1
name2 = equivalent? cond1 cond2
name3 = different? cond1 cond2
name4 = implies? cond3 cond4
name5 = always_true? cond3
name6 = always_true? cond4
name7 = always_true? cond5
```

2. Choose a synthesis method. Then click on one of the green synthesiser buttons:

Explicit Synthesis

Symbolic Synthesis

Display results of all analyses in pretty printed form

Generate, show, and run Z3 code, display results in pretty-printed and raw form

Generate and show Z3 code

Generate Z3 code and a link to it below

Non-random benchmark

- Majority voting: $pol = +((q1 \ 1/n) (q2 \ 1/n) \dots (qn \ 1/n))$
default 0
- synthesis of $0.5 < pol$ generates **exponentially many disjuncts** in set $M1$
- e.g. for $n=27$, **synthesized formula 0.5 GB !**
- satisfiability checks easy, size of formula is real issue here: $\text{choose}(n, \text{ceil}(n/2))$ many terms
- explore space-time trade-offs: **symbolic synthesis**

Symbolic synthesis

- **Hybrid approach**: synthesis of *min* and *max* composition of rules still done explicitly --
linear in input size
- Synthesis of conditions for policy sets makes logical decomposition into **conditions for policies** explicit
- But synthesis of conditions for policies **symbolically** encodes operational semantics with auxiliary real variables

Simple example

- a policy composed with $+$
- $b2 = + ((q4\ 0.1)\ (q5\ 0.2)\ (q6\ 0.2))$ default 0
- declare real variables $b2_score_qi$ for each predicate qi in $b2$
- *assert that these variables have desired operational value*
- exploits that $+$ (respectively $*$) has semantic unit 0 (respectively 1)

Declaring rule effect

b2 = + ((q4 0.1) (q5 0.2) (q6 0.2)) default 0

```
(declare-const b2_score_q4 Real) ; reals for b2
(assert (implies q4 (= 0.1 b2_score_q4)))
(assert (implies (not (= 0.0 b2_score_q4)) q4))
```

```
(declare-const b2_score_q5 Real)
(assert (implies q5 (= 0.2 b2_score_q5)))
(assert (implies (not (= 0.0 b2_score_q5)) q5))
```

```
(declare-const b2_score_q6 Real)
(assert (implies q6 (= 0.2 b2_score_q6)))
(assert (implies (not (= 0.0 b2_score_q6)) q6))
```

Declaring policy effect

$b1 = \min(\dots) \dots$

$b2 = +((q4\ 0.1)\ (q5\ 0.2)\ (q6\ 0.2))\ \text{default}\ 0$

$\text{cond2} = 0.6 < \min(b1, b2)$

- effect of policy (here $b2$) is function of condition, here cond2 :

```
(declare-const cond2_b2 Bool)
```

```
(assert (= cond2_b2 (or
```

```
(and (< 0.6 0) (not (or q4 q5 q6))) ; default case
```

```
(and (or q4 q5 q6) ; non-default case
```

```
(< 0.6 (+ b2_score_q4 b2_score_q5  
         b2_score_q6))))))
```

Symbolic synthesis

- Z3 input code **linear** in size of Peal conditions
- space/time tradeoff: e.g. for majority voting
- **explicit synthesis could only deal with $n=27$ for majority voting**
- **symbolic synthesis generates and verifies equivalent condition for $n=5000$ in seconds!**

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Experiments

- All experiments test: **Z3 code generation and Z3 analysis both take less than five minutes?**
- Server funded by this Intel project: 24-core, Linux, 48-GB RAM; **generated random analyses** one single core, here is an example:

```
POLICIES
b0 = max ((q3 0.2602799435758082) (q2 0.8465841883500088) (q1 0.5206939762267451) (q6
0.9230438145042877)) default 0.35448995987981113
b1 = + ((q2 0.5067729289557699) (q1 0.9809171774005019) (q3 0.1957352016220224)) default
0.06811372400781202
b2 = min ((q0 0.3996348599684737) (q6 0.1617558737504945)) default 0.4678754705036007
b3 = * ((q3 0.7832597548785873) (q5 0.5795098955834747)) default 0.4486210823937763
POLICY_SETS
p0_1 = min(b0,b1)
p2_3 = min(b2,b3)
p0_3 = max(p0_1,p2_3)
CONDITIONS
cond1 = 0.50 < p0_3
cond2 = 0.60 < p0_3
ANALYSES
analysis1 = always_true? cond1
analysis2 = always_false? cond2
analysis3 = different? cond1 cond2
```


First experiment

- Don't report results on * aggregation of rules in policies for these experiments, see Tech Report for details
- Analyzed *sole* policy with *min* or *max* composition: handle about 2 million rules within five minutes
- *Sole* policy for *+* composition: explicit synthesis can handle around 150 rules within five minutes
- *Sole* policy for *+* composition: symbolic synthesis can handle about six-thousand(!) rules within five minutes

First experiment + Domain Specifics

- Repeated first experiment but added domain-specific constraints: linear inequalities, and model of method-call graph with in-degree at most 1
- Analyzed *sole* policy with *min* or *max* composition: handle about 7000 (2-million before) rules within five minutes
- *Sole* policy for *+* composition: explicit synthesis can handle around 130 (150 before) rules within five minutes
- *Sole* policy for *+* composition: symbolic synthesis can handle about two-thousand (6000 before) rules within five minutes

Second experiment

- How many policies analyzable in 5 minutes where each policy has $x/10$ rules and x was 5-minute bound on number of rules from First Experiment (e.g. $x = 200,000$ for min and max)
- *min* or *max* composition: handle about 50 policies with about 200,000 rules within five minutes
- \neq composition: explicit synthesis can handle around 18,000 policies with 14 rules within five minutes
- \neq composition: symbolic synthesis can handle 24 policies with about six-hundred rules within five minutes

Third experiment

- How many policies n with n rules each can we handle within five minutes?
- *min* or *max* composition: handle about 2000 to 3000 policies with that many rules each within five minutes
- + composition: explicit synthesis can handle about 100 policies with 100 rules each within five minutes
- + composition: symbolic synthesis can handle about 160 policies with 160 rules each within five minutes

Alice/Bob example

- $cond1 = 0.5 < pSet$ different from $cond2 = 0.6 < pSet$
- pretty printed explanation extracted from explicit synthesis analysis (colors added manually):

```
Result of analysis [name1 = different? cond1 cond2]  
cond1 and cond2 are different
```

```
For example, when  
highCostTransaction is false  
enoughMutualFriendsNormalized is true  
lowCostTransaction is true  
enoughMutualFriends is true  
aFriendOfAliceUnfriendedBob is false  
cond2 is false  
cond1 is true  
numberOfBobsFriends is 5  
amountAlicePays is 2.0  
numberOfMutualFriends is 5
```

Alice/Bob explanation

- $0.5 < pSet \text{ true}$, $0.6 < pSet \text{ false}$ because
- all predicates in b_1 false, so b_1 returns 0.6
- first two predicates in b_2 true, so b_2 returns **at least 0.6**
- don't care about value of $aFriendVouchesForBob$
- so $pSet = \min(b_1, b_2)$ returns 0.6

$b_1 = +((if (lowCostTransaction 0.3) (if enoughMutualFriends 0.1)$
 $(if enoughMutualFriendsNormalized 0.2)) default 0$

$b_2 = \min((if (highCostTransaction 0.1) (if aFriendOfAliceUnfriendedBob 0.2)$
 $(if aFriendOfAliceVouchesForBob 0.6)) default 1$

$cond = 0.5 < \min(b_1, b_2)$

Future work

- Comprehensive experimental evaluation
- Case studies that make use of this tool
- Extension to non-constant or negative scores and metrics: symbolic synthesis allows for this
- Independent verification of reported Z3 models, shortening of models for symbolic synthesis
- Implementation of more complex analyses (e.g. computing “**threshold spectrum**” of policy set)

References

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Thank You

Questions?