Generative and adaptive methods in performance programming f • g p;q p|q p||q p(q) p<q>

Paul H J Kelly Imperial College London

Joint work with Olav Beckmann Including contributions from Tony Field and numerous students

Where we're coming from...



- I lead the Software Performance Optimisation group at Imperial College, London
- Stuff I'd love to talk about another time:
 - Run-time code-motion optimisations across network boundaries in Java RMI
 - Bounds-checking for C, links with unchecked code
 - Is Morton-order layout for 2D arrays competitive?
 - Domain-specific optimisation frameworks
 - Domain-specific profiling
 - Proxying in CC-NUMA cachecoherence protocols – adaptive randomisation and combining

eria

Performance programming

- Performance programming is the discipline of software engineering in its application to achieving performance goals
- This talk aims to review a selection of performance programming techniques we have been exploring

perial College

Construction

- What is the role of constructive methods in performance programming?
- "by construction"
- "by design"
- How can we build performance into a software project?
- How can we build-in the means to detect and correct performance problems?
- As early as possible
- With minimal disruption to the software's long-term value?

erial

"In constructive logic, we can synthesize correct programs by expressing the specification as a formula, and proving it. We call this style of programming constructive"

(Sato Masahiko / Kameya Yukiyoshi, *Constructive Programming based on SST//*, IPSJ SIGNotes Software Foundation Abstract No.031 - 006)

erial

Abstraction

Most performance improvement opportunities come from adapting components to their context

- So the art of performance programming is to figure out how to design and compose components so this doesn't happen
- Most performance improvement measures break abstraction boundaries
- This talk is about two ideas which can help:
 - Run-time program generation (and manipulation)
 - Metadata, characterising data structures, components, and their dependence relationships

eria

Abstraction

Most performance improvement opportunities come from adapting components to their context

- So the art of performance programming is to figure out how to design and compose components so this doesn't happen
- Most performance improvement measures break abstraction boundaries
- This talk is about two ideas which can help:
 - Run-time program generation (and manipulation)
 - Metadata, characterising data structures, components, and their dependence relationships

Abstraction

Most performance improvement opportunities come from adapting components to their context

So the art of performance programming is to figure out how to design and compose components so this doesn't happen Most performance improvement measures break abstraction boundaries

This talk is about two ideas which can help:

- Run-time program generation (and manipulation)
- Metadata, characterising data structures, components, and their dependence relationships

Abstraction

 Most performance improvement opportunities come from adapting components to their context

- So the art of performance programming is to figure out how to design and compose components so this doesn't happen
- Most performance improvement measures break abstraction boundaries

This talk is about two ideas which can help:

- Run-time program generation (and manipulation)
- Metadata, characterising data structures, components, and their dependence relationships

- Most performance improvement opportunities come from adapting components to their context
- So the art of performance programming is to figure out how to design and compose components so this doesn't happen
- Most performance improvement measures break abstraction boundaries
- This talk is about two ideas which can help:
 - Run-time program generation (and manipulation)
 - Metadata, characterising data structures, components, and their dependence relationships

This talk:

- Communication fusion
- Alignment in parallel BLAS
- Partial evaluation/specialisation
- Adapting to platform/resources
- Cross-component loop fusion

Adapting to context

Dependence metadata

Performance metadata

Component model to support composition-time adaptation

mperial College

opuo

Adaptation #1: Communication fusion

double s1, s2;

Component #1

```
void sum( double& data ) {
  double r = 0.0 ; ...
  for (j=jmin;j<=jmax;j++) {
    r += data[j] ;
  }</pre>
```

MPI Allreduce(&r,&s1,1,MPI SUM,...);

Component #2

```
void sumsq( double& data ) {
   double r = 0.0 ; ...
   for (j=jmin;j<=jmax;j++) {
     r += data[j]*data[j] ;
   }
   MPI_Allreduce(&r,&s2,1,...);</pre>
```

Example: calculating variance of distributed vector "data"

Component composition

```
double a[...][...],var[...] ;
```

```
for( i=0; i<N; i++ ) {</pre>
```

sum(a[i]) ;

```
sumSq(a[i]) ;
```

```
var[i] = (s2-s1*s1/N)/(N-1);
```

Adaptation #1: Communication fusion

double rVec[2];

Component #1

```
void sum( double& data ) {
  double r = 0.0; ...
  for (j=jmin;j<=jmax;j++) {</pre>
    r += data[i];
  }
 rVec[0] = r;
Component #2
void sumsq( double& data ) {
  double r = 0.0; ...
```

```
for (j=jmin;j<=jmax;j++) {</pre>
```

```
r += data[j]*data[j] ;
```

rVec[1]= r;

}

Example: calculating variance of distributed vector "data"

Component composition

```
double a[...][...],var[...] ;
```

```
for( i=0; i<N; i++ ) {</pre>
```

```
sum(a[i]) ;
```

```
sumSq(a[i]) ;
```

```
MPI_Allreduce(&rVec,&s,2,
```

```
MPI_SUM,..) ;
```

```
var[i] = (s2-s1*s1/N)/(N-1);
```

```
For N=3000 fusing MPI
Allreduces improved
performance on linux
cluster by 48.7%
```

Adaptation #1: Communication fusion

Component #1



Component #2

```
void sumsq( double& data ) {
    s2 = 0.0 ; ...
    for (j=jmin;j<=jmax;j++) {
        s2 += data[j]*data[j] ;
    }
    Global reduction</pre>
```

Component composition

```
double a[...][...],var[...] ;
```

```
for( i=0; i<N; i++ ) {</pre>
```

```
sum(a[i]) ;
```

```
sumSq(a[i]) ;
```



force point

For N=3000 our CFL library improved performance on linux cluster by 44.5%



A.J. Field, P.H.J. Kelly and T.L. Hansen, "Optimizing Shared Reduction Variables in MPI Programs". In Euro-Par 2002

Adaptation #2: alignment in parallel BLAS

15

_ D X

ptimi \bigcirc CO erforman Δ tware S mperial College

ndon

{

Permacs@SECONDSELF

Buffers Files Tools Edit Search Mule C++ Help

emplate<class Matrix, class Vector, class Precond, class Real> int CG(const Matrix &A. Vector &x. const Vector &b, const Precond &M, int &max_iter. Real &tol) // local vector and scalar declarations & initial convergence test omitted for(int i = 1; i <= max_iter; i++) {</pre> z = M.solve(r): rho(0) = dot(r, z);if (i == 1)p = z: else { $beta(0) = rho(0) / rho_1(0);$ p = z + beta(0) * p;3 $q = A^*p$; alpha(0) = rho(0) / dot(p, q);x += alpha(0) * p; r -= alpha(0) * q: if((resid = norm(r) / normb) <= tol)</pre> tol = resid; max_iter = i; return 0: $rho_1(0) = rho(0);$ tol = resid: return 1; CC

- This is a generic conjugategradient solver algorithm, part of Dongarra et al's IML++ library
- It is parameterised by the Matrix and Vector types
- Our DESOBLAS library implements this API for dense matrices
 - In parallel using MPI

mperial College ondon

Adaptation #2: alignment in parallel BLAS

 Execution is delayed until output or conditional forces computation
 BLAS functions return opaque handles



Library builds up data flow graph "recipe" representing delayed computation This allows optimization to exploit foreknowledge of how results will be used

Example: conjugate gradient



perial College

nobr

Adaptation #2: alignment in parallel BLAS

We are forced to insert a transpose:



perial College

Adaptation #2: alignment in parallel BLAS

We are forced to insert another transpose:



We can transpose either p or x

(or we could have kept an untransposed copy of p - if we'd known it would be needed)

erial

Adaptation #2: alignment in parallel BLAS

Delayed execution allows us to see how values will be used and choose better:



If we can foresee how p will be used, we can see it's the wrong thing to transpose...

erial

Adaptation #2: alignment in parallel BLAS

Delayed execution allows us to see how values will be used and choose better:

erial

Adaptation #2: alignment in parallel BLAS

Delayed execution allows us to see how values will be used and choose better:

Avoiding redistributions: performance

mperial College

ondon

Number of Processors (Opt means with DESO Optimisation)

Cluster of 2GHz P4, 500 MB RAM, running Linux 2.4.20 and gcc 2.95.3, using C/Fortran bindings (not C++ overloading)

Metadata in DESOBLAS

- Each DESOBLAS library operator carries metadata, which is used at run-time to find an optimized execution plan
- For optimizing data placement, metadata is set of affine functions relating operator's output data placement to the placement of each input
- Network of invertible linear relationships allows optimizer to shift redistributions around dataflow graph to minimise communication cost
 - ((broadcasts and reductions involve singular placement relationships - see Beckmann and Kelly, LCPC'99 for how to make this idea still work))

Composition: metadata is assembled according to arcs of data flow graph to define system of alignment constraints:

$$A_u = A_v^T \quad A_x = A_y^T$$
$$A_A = A_u \quad A_w = A_x^T$$
$$A_C = A_w$$
$$A_B = A_x$$

Peter Liniker, Olav Beckmann and Paul H J Kelly, Delayed Evaluation, Self-Optimizing Software Components as a Programming Model. In Euro-Par 2002

- The TaskGraph library is a portable C++ package for building and optimising code onthe-fly
 - Compare:
 - `C (tcc) (Dawson Engler)
 - MetaOCaml (Walid Taha et al)
 - Jak (Batory, Lofaso, Smaragdakis)
 - Multi-stage programming: "runtime code generation as a firstclass language feature"

#include <TaskGraph> #include <stdio.h> #include <stdlib.h> #include <sys/time.h> using namespace tg; int main(int argc, char argv[]) { TaskGraph T; int b = 1, c = 1;taskgraph(T){ tParameter (tVar (int, a)); a = a + c;T.compile (TaskGraph::GCC); T.execute ("a", &b, NULL); printf("b = %d n", b);

perial College

Adaptation #3: specialisation

- A taskgraph is an abstract syntax tree for a piece of executable code
- Syntactic sugar makes it easy to construct
- Defines a simplified sublanguage
 - With first-class multidimensional arrays, no alliasing

```
#include <TaskGraph>
#include <stdio.h>
#include <stdlib.h>
#include <sys/time.h>
using namespace tg;
int main( int argc, char argv[] ) {
 TaskGraph T;
 int b = 1, c = 1;
 taskgraph (T) {
  tParameter (tVar (int, a));
  a = a + c;
 T.compile (TaskGraph::GCC);
 T.execute ("a", &b, NULL);
 printf("b = %d n", b);
```

perial Colleg

Adaptation #3: specialisation

- Binding time is determined by types
 In this example
 - c is static
 - a is dynamic

built using value of c at construction time #include <TaskGraph> #include <stdio.h> #include <stdlib.h> #include <sys/time.h> using namespace tg; int main(int argc, char argv[]) { TaskGraph T; int b = 1, c = 1;taskgraph (T) { tParameter (tVar (int, a)); a = a + c;T.compile (TaskGraph::GCC); T.execute ("a", &b, NULL); printf("b = %d n", b);

mperial College

nopu

Adaptation #3: specialisation

Better example:

- Applying a convolution filter to a 2D image
- Each pixel is averaged with neighbouring pixels weighted by a stencil matrix


```
void filter (float *mask, unsigned n, unsigned m,
const float *input, float *output,
unsigned p, unsigned q)
```

```
unsigned i, j;
int k, l;
float sum;
int half_n = (n/2);
int half_m = (m/2);
```

```
for (i = half_n; i for (j = half_m; j < q - half_m; j++) {
sum = 0;
```

// Loop bounds unknown at compile-time
// Trip count 3, does not fill vector registers

```
for (k = -half_n; k <= half_n; k++)
for (l = -half_m; l <= half_m; l++)
sum += input[(i + k) * q + (j + l)]
* mask[k * n + l];
```

output[i * q + j] = sum;

First without TaskGraph

erial College

Adaptation #3: specialisation

- TaskGraph representation of this loop nest
- Inner loops are static – executed at construction time
- Outer loops are dynamic
- Uses of mask array are entirely static
- This is deduced from the types of mask, k, m and l.

```
void taskFilter (TaskGraph &t,
                float *mask, unsigned n, unsigned m,
                unsigned p, unsigned q)
 taskgraph (t) {
  unsigned img_size[] = { IMG_SIZE, IMG_SIZE };
  tParameter(tArray(float, input, 2, img_size));
  tParameter(tArray(float, output, 2, img_size));
   unsigned k, l;
   unsigned half_n = (n/2);
   unsigned half_m = (m/2);
  tVar (float, sum);
  tVar (int, i);
  tVar (int, j);
  tFor (i, half_n, p - half_n - 1) {
    tFor (j, half_m, q - half_m - 1) {
     sum = 0;
     for (k = 0; k < n; ++k)
      for (I = 0; I < m; ++I)
        sum += input[(i + k - half_n)][(j + l - half_m)]
                * mask[k * m + l];
     output[i][j] = sum;
                          // Inner loops fully unrolled
                          // j loop is now vectorisable
                              Now with TaskGraph
```


Adaptation #3: specialisation

roup

Application: Sobel filters in image processing (8-bit RGB data) – compared with Intel's Performance Programming Library

perial College

Adaptation #4: Adapting to platform/resources³²

- The TaskGraph library is a tool for dynamic code generation and optimisation
- Large performance benefits can be gained from specialisation alone

But there's more:

- TaskGraph library builds SUIF intermediate representation
- Provides access to SUIF analysis and transformation passes
 - SUIF (Stanford University Intermediate Form)
 - Detect and characterise dependences between statements in loop nests
 - Restructure tiling, loop fusion, skewing, parallelisation etc

d	void taskMatrixMult (TaskGraph &t ,	
jõ	TaskLoopIdentifier *loop) {	
Ū	taskgraph (t) {	
	tParameter (tArray (float, a, 2, sizes));	
tic	tParameter (tArray (float, b, 2, sizes));	
Sa	tParameter (tArray (float, c, 2, sizes));	
<u> </u>	tVar (int, i);	int main (i
pti	tVar (int, j);	TaskGrap
O	tVar (int, k);	TaskLoop
Ð		
anc	tGetld (loop[0]); // label	// Build Ta
Ц Ц	tFor (i, 0, MATRIXSIZE - 1) {	tack Matrix
0LI	tGetId (loop[1]); // label	laskivialitz
erf(tFor (J, U, MATRIXSIZE - I) {	
ď	tGetid (loop[2]); // label	// Intercha
Ð	tFor (K, U, MATRIXSIZE - T) {	interchang
้าลเ	C[i][j] += a[i][k] * b[k][j];	
ft∨	}	int trip[] =
Ö	, } , }	
		// Tile the
ge	Original TaskGraph	tilel oon (
e	for matrix multiply	
8		
		mm.comp
i ob		mm.execi
ēč		}
Ľ٦		Code to

```
Tilir
              Example: matrix
           multiply
nt argc, char **argv ) {
h mm;
Identifier loop[3];
askGraph for ijk multiply
xMult ( loop, mm );
ange the j and k loops
geLoops ( loop[1], loop[2] );
= { 64, 64 };
j and k loops into 64x64 tiles
2, &loop[1], trip );
oile ( TaskGraph::GCC );
ute ( "a", a, "b", b, "c", c, NULL );
```

Code to interchange and tile

```
void taskMatrixMult (TaskGraph &t,
                                                      Loop interchange and tilind<sup>4</sup>
                 TaskLoopIdentifier *loop) {
  taskgraph(t){
   tParameter (tArray (float, a, 2, sizes));
                                                   extern void taskGraph_1(void **params)
   tParameter (tArray (float, b. 2, sizes)):
   tParameter (tArray (float, c, 2, sizes));
   tVar (int. i):
                                                     float (*a)[512];
   tVar (int. i):
   tVar (int, k);
                                                     float (*b)[512];
   tGetId (loop[0]): // label
                                                     float (*c)[512];
   tFor (i. 0. MATRIXSIZE - 1) {
                                                     int i:
    tGetId (loop[1]); // label
                                                                                    Generated code
    tFor (j, 0, MATRIXSIZE - 1) {
                                                     int i:
     tGetId (loop[2]); // label
     tFor (k, 0, MATRIXSIZE - 1) {
                                                     int k:
                                                                                      (Slightly tidied)
      c[i][i] += a[i][k] * b[k][i];
                                                     int j_tile;
                  Original TaskGraph
                                                     int k_tile;
                  for matrix multiply
     int main ( int argc, char **argv ) {
                                                     a = *params;
      TaskGraph mm;
      TaskLoopIdentifier loop[3];
                                                     b = params[1];
                                                     c = params[2];
      // Build TaskGraph for ijk multiply
                                                     for (i = 0; i \le 511; i++)
      taskMatrixMult (loop, mm);
                                                       for (j_tile = 0; j_tile \le 511; j_tile + 64)
      // Interchange the j and k loops
                                                         for (k_{tile} = 0; k_{tile} <= 511; k_{tile} += 64)
      interchangeLoops ( loop[1], loop[2] );
                                                          for (j = j_tile;
      int trip[] = \{ 64, 64 \};
                                                                i \le \min(511, 63 + i_t); i++)
College
                                                            for (k = max(0, k_tile));
      // Tile the j and k loops into 64x64 tiles
                                                                 k \le \min(511, 63 + k_{tile}); k++)
      tileLoop ( 2, &loop[1], trip );
                                                              c[i][k] = c[i][k] + a[i][j] * b[j][k];
erial
      mm.compile ( TaskGraph::GCC );
      mm.execute ( "a", a, "b", b, "c", c, NULL );
    Code to interchange and tile
```


On Pentium 4-M, 1.8 GHz, 512KB L2 cache, 256 MB, running Linux 2.4 and icc 7.1.

n

erial College

Adaptation #4: Adapting to platform/resources

College

mperial

perial

Potential for user-directed restructuring

- Programmer controls application of sophisticated transformations
- Performance benefits can be large in this example >8x
- Different target architectures and problem sizes need different combinations of optimisations
 - ijk or ikj?
 - Hierarchical tiling
 - 2d or 3d?
 - Copy reused submatrix into contiguous memory?
- Matrix multiply is a simple example

Cross-component loop fusion

Cross-component loop fusion

40

Cross-component loop fusion

- Simple fusion leads to small improvement
- Beats Intel library only on large images
- Further fusion opportunities require skewing/retiming

erial

Performance-programming Component model

Dependence metadata

- Components should carry a description of their dependence structure
- That is based on an abstraction of the component's Iteration Space Graph (ISG)
- Eg to allow simple check for validity of loop and communication fusion
- Eg to determine dependence constraints on distribution
- Eg so we can align data distributions to minimise communication
- To predict communication volumes

Jacobi1D(U,V): Jacobi1D(V,W) W For (i=1; i<N; i++) V[i] = (U[i-1] + U[i+1])/2For (i=1; i<N; i++) W[i] = (V[i-1] + V[i+1])/2For (i=1; i<N; i++) W[i] = (V[i-1] + V[i+1])/2Fusion *invalid*: iteration i of second loop reads value generated at iteration i of first loop

erial

Performance-programming Component model

Dependence metadata

- Components should carry a description of their dependence structure
- That is based on an abstraction of the component's Iteration Space Graph (ISG)
- Eg to allow simple check for validity of loop and communication fusion
- Eg to determine dependence constraints on distribution
- Eg so we can align data distributions to minimise communication
- To predict communication volumes

perial College

Performance-programming Component model

Performance metadata

- Components should carry a Eg to allow scheduling model of how execution time depends on parameters and configuration
- That is based on an abstraction of the component's Iteration Space Graph (ISG)

and load balancing

44

Eg to determine communicationcomputationrecomputation tradeoffs

erial

Performance-programming Component model

Performance metadata

- Components should carry a Eg to allow scheduling model of how execution time depends on parameters and configuration
- That is based on an abstraction of the component's Iteration Space Graph (ISG)

- and load balancing
 - Eg to determine communicationcomputationrecomputation tradeoffs

M: Inner loop bounds

Input volume: M

Output volume: M-1

Component metadata research agenda

46

- We want to adapt to shape of data
- But in interesting applications, data shape is not regular
 - Shape description/metadata depends on data values
 - Metadata size is significant
 - Metadata generation/manipulation is significant part of computational effort
- The problem:
 - Cost of organising and analysing the data may be large compared to the computation itself
 - Size of metadata may be large compared with size of the data itself
- What does this mean?
 - Some kind of reflective programming
 - Arguably, metaprogramming
- Programs that make runtime decisions about how much work to do to optimise future execution

Paul H J Kelly, Olav Beckmann, Tony Field and Scott Baden, "Themis: Component dependence metadata in adaptive parallel applications". Parallel Processing Letters, Vol. 11, No. 4 (2001)

mperial College

ria

Conclusions

- Performance programming as a software engineering discipline
- The challenge of preserving abstractions
- The need to design-in the means to solve performance problems
- Adaptation to data-flow context
- Adaptation to platform/resources
- Adaptation to data values, sizes, shapes
- Making component composition explicit: build a plan, optimise it, execute it

erial College

Acknowledgements

- This work was funded by EPSRC
 Much of the work was done by colleagues and members of my research group, in particular
 - Olav Beckmann
 - Tony Field

Students:

Alastair Houghton, Michael Mellor, Peter Fordham, Peter Liniker, Thomas Hansen