

Part a H

$$(1) \quad h_{TF} \sim h$$

$$(2) \quad e, h_{TF} \rightsquigarrow e', h'_{TF}$$

then $\exists h'$

$$(3) \quad h'_{TF} \sim h'$$

$$(4) \quad \mathcal{P}(e), h \rightsquigarrow^* \mathcal{P}(e'), h'$$

Proof By structural induction over (2). We apply case analysis over the last rule applied in the derivation of (2).

1st Case FID-CNTX. By application of induction hypothesis and CNTX.

2nd Case FID-EX-PROP by apl of EX-PROP.

3rd Case FID-SEQ. \therefore

4th Case RUN appl. induction hypothesis and RUN

5th Case FID-NEW. Therefore

$$(5) \quad e = \text{new } C, \mathcal{P}(e) = \text{new } C.\text{int.}$$

Apply rules FID-NEW for the \downarrow CHOOLET execution
and rules NEW, ASYNC, SEQ for the \downarrow CHOOLET execution.

6th case FLD-ASYNC. Therefore

$e = L.m(v)$ and m is an asynchron method
 in P_{+F} , with $async\ m(-) \in M(P_{+F}, m)$. Therefore,
 by construction $async\ m(-) \in M(\mathcal{P}(P_{+F}), c, m)$.

7th case FLD-WR. Therefore,

- (5) $e = L.f := v$
- (6) $h_{+F}(v) = \llbracket c \parallel q_s \parallel f_s \rrbracket$
- (7) $h'_{+F} = h_{+F} [L \rightarrow \llbracket c \parallel q_s \parallel f_s [f \mapsto v] \rrbracket]$

(7a) $e' = v$
 Because of S , we have

(8) $\mathcal{P}(e) = L.set-f(v)$

Because of (6) and (1) we also have

- (9) $h(v) = \llbracket c \parallel q_s \parallel q_{s'} \rrbracket, \text{ dom}(q_{s'}) = \text{dom}(f_s)$
- $q_{s'}(f) = \{ f_s(f) \}$

Therefore, by construction of $\mathcal{P}(P_{+F})$ we obtain

- (10) $L.set-f(v), h \rightsquigarrow L.ready-f(v); v, h''$
- (11) $h'' = h [L \mapsto \llbracket c \parallel q_s \parallel q_{s'} [ready-f \mapsto \emptyset] \rrbracket]$

By application of ASYNC, and SEQ we obtain

- (12) $L.set-f(v), h \xrightarrow{*} v; h'$
- (13) $h' = h [L \mapsto \llbracket c \parallel q_s \parallel q_{s'} [ready-f \mapsto \{v\}] \rrbracket]$

and