Algorithms for Optimal Decisions Tutorial 2 Questions

Exercise 1 Labor costs 2\$/hour and capital costs 1\$/unit. If l hours of labor and k units of capital are available then $l^{2/3} \cdot k^{1/3}$ machines can be produced. If the budget for purchasing capital and labor is 10\$, what is the maximum number of machines that can be produced?

Exercise 2 Find the optimum solution of the following constrained problem:

$$\max_{x} f(x) = x_1 x_2 + x_2 x_3 + x_1 x_3$$
s.t.
$$x_1 + x_2 + x_3 = 3.$$
 (1)

Exercise 3 Given a fixed area of cardboard, try to find the dimensions of a cardboard box with the largest possible volume.