Algorithms for Optimal Decisions Tutorial 4 Questions

Exercise 1

Solve the following Q.P. using the Frank–Wolfe method:

$$\min_{x} f(x) = x_{1}^{2} - x_{1}x_{2} + x_{2}^{2} - 3x_{1}$$
s.t. $-x_{1} \leq 0$
 $-x_{2} \leq 0$
 $x_{1} + x_{2} - 4 \leq 0.$
(1)

Starting point : $x^{(0)} = (x_1^{(0)}, x_2^{(0)}) = (0, 0).$

Exercise 2 Solve the following problem by using **SUMT** and taking $x^{(0)} = (x_1^{(0)}, x_2^{(0)}) = (1, 1)$ as a starting point

$$\max_{x} f(x) = x_{1}x_{2}$$

s.t. $x_{1}^{2} + x_{2} - 3 \le 0$
 $x_{1} \ge 0, x_{2} \ge 0.$ (2)

The solution is $x^* = (x_1^*, x_2^*) = (1, 2).$