

The Physics of shading

- Object properties:
 - Looking at a point on an object we see the reflection of the light that falls on it. This reflection is governed by:
 - 1. The position of the object relative to the light sources
 - 2. The surface normal vector
 - 3. The albedo of the surface (ability to adsorb light energy)
 - 4. The reflectivity of the surface
- Light source properties:
 - The important properties of the light source are
 - 1. Intensity of the emitted light
 - 2. The distance to the point on the surface

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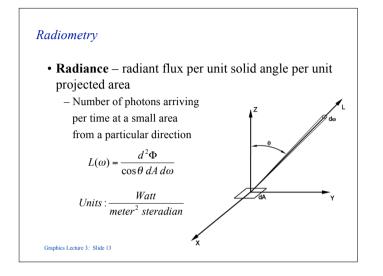
The Physics of shading

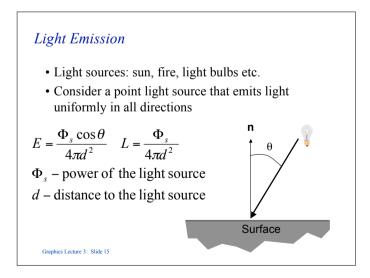
- If we look at a point on an object we perceive a colour and a shading intensity that depends on the various characteristics of the object and the light sources that illuminate it.
- For the time being we will consider only the brightness at each point. We will extend the treatment to colour later.

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Radiometry • Energy of a photon $e_{\lambda} = \frac{hc}{\lambda}$ $h \approx 6.63 \cdot 10^{-34} J \cdot s$ $c \approx 3 \cdot 10^8 m/s$ • Radiant Energy of *n photons* $Q = \sum_{i=1}^{n} \frac{hc}{\lambda_i}$ • Radiation flux (electromagnetic flux, radiant flux) Units: Watts $\Phi = \frac{dQ}{dt}$





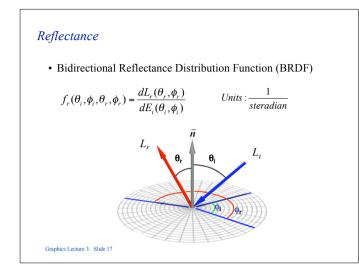
Radiometry

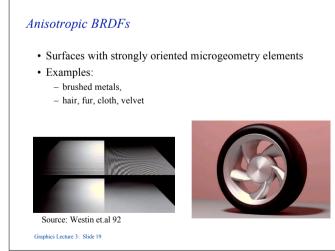
- Irradiance differential flux falling onto differential area $E = \frac{d\Phi}{dA} \qquad Units: \frac{Watt}{meter^2}$
- Irradiance can be seen as a density of the incident flux falling onto a surface.
- It can be also obtained by integrating the radiance over the solid angle.

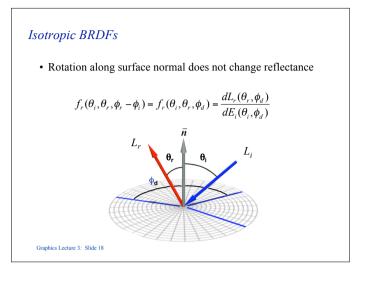
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Reflection & Reflectance

- Reflection the process by which electromagnetic flux incident on a surface leaves the surface without a change in frequency.
- Reflectance a fraction of the incident flux that is reflected
- We do not consider:
 - absorption, transmission, fluorescence
 - diffraction







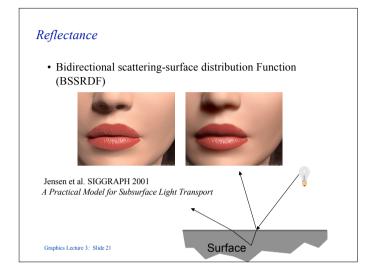
Properties of BRDFs

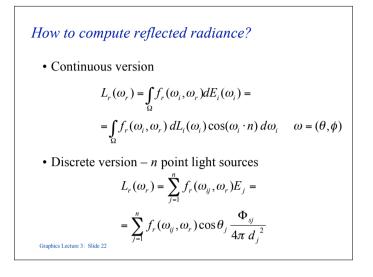
- Non-negativity $f_r(\theta_i, \phi_i, \theta_r, \phi_r) \ge 0$
- Energy Conservation

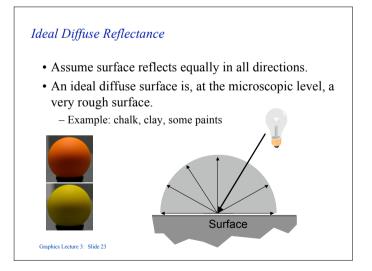
 $\int_{\Omega} f_r(\theta_i, \phi_i, \theta_r, \phi_r) d\mu(\theta_r, \phi_r) \le 1 \quad \text{for all} (\theta_i, \phi_i)$

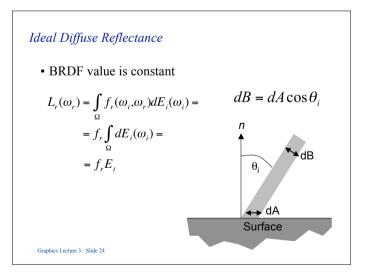
Reciprocity

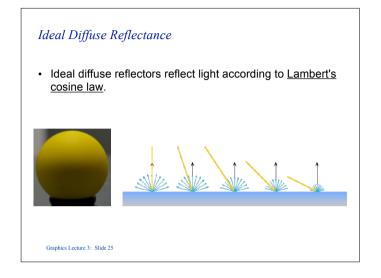
 $f_r(\theta_i, \phi_i, \theta_r, \phi_r) = f_r(\theta_r, \phi_r, \theta_i, \phi_i)$









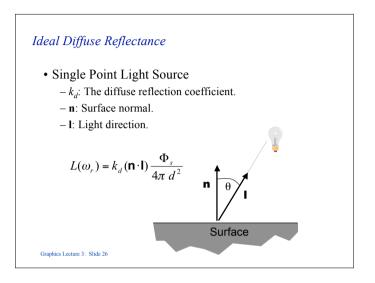


Ideal Diffuse Reflectance – More Details

- If **n** and **l** are facing away from each other, **n l** becomes negative.
- Using max((**n l**), 0) makes sure that the result is zero.
 - From now on, we mean max() when we write $\boldsymbol{\cdot}.$

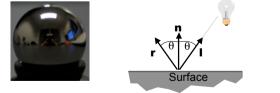
Do not forget to normalize your vectors for the dot product!

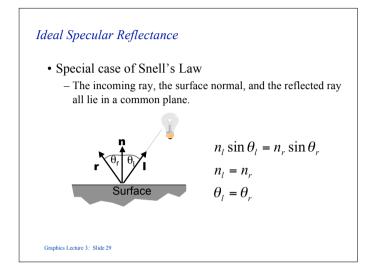
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Ideal Specular Reflectance

- Reflection is only at mirror angle.
 - View dependent
 - Microscopic surface elements are usually oriented in the same direction as the surface itself.
 - Examples: mirrors, highly polished metals.



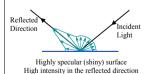


Non-ideal Reflectors

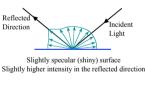
- Simple Empirical Model:
 - We expect most of the reflected light to travel in the direction of the ideal ray.
 - However, because of microscopic surface variations we might expect some of the light to be reflected just slightly offset from the ideal reflected ray.
 - As we move farther and farther, in the angular sense, from the reflected ray we expect to see less light reflected.



Non-ideal Reflectors: Surface Characteristics Reflected Incident Direction Light Perfectly Matt surface The reflected intensity is the same in all directions



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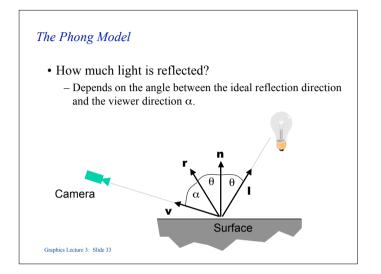


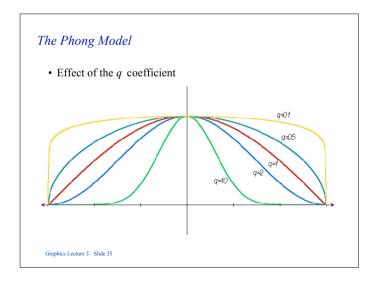


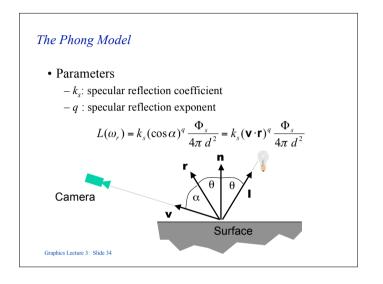
Perfect Mirror All light re-admitted in the reflected direction

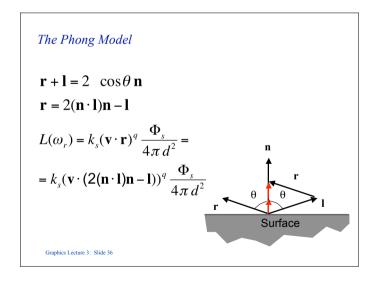
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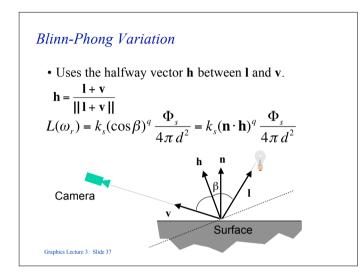
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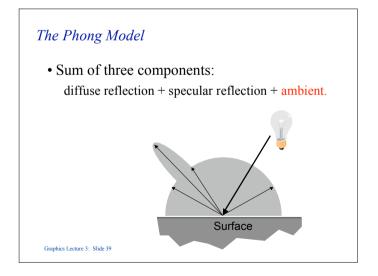






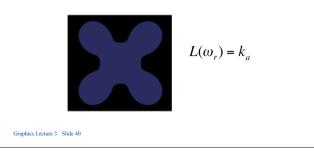


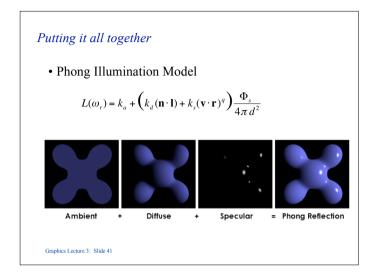


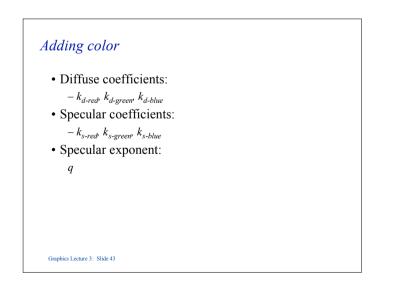


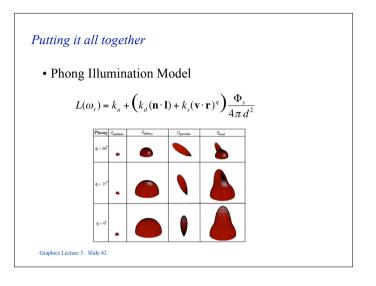
Ambient Illumination

- Represents the reflection of all indirect illumination.
- This is a total hack!
- Avoids the complexity of global illumination.









Inverse Square Law

• It is well known that light falls off according to an inverse square law. Thus, if we have light sources close to our polygons we should model this effect.

$$L(\omega_r) = k_a + \left(k_d(\mathbf{n} \cdot \mathbf{l}) + k_s(\mathbf{v} \cdot \mathbf{r})^q\right) \frac{\Phi_s}{4\pi d^2}$$

where *d* is the distance from the light source to the object

Heuristic Law

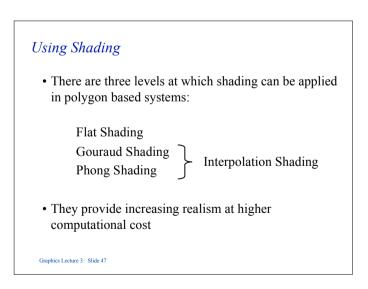
- Although physically correct the inverse square law does not produce the best results.
- Instead the following is often used:

$$L(\omega_r) = k_a + \left(k_d(\mathbf{n} \cdot \mathbf{l}) + k_s(\mathbf{v} \cdot \mathbf{r})^q\right) \frac{\Phi_s}{4\pi (d+s)}$$

where *s* is an heuristic constant.

- One might be tempted to think that light intensity falls off with the distance to the viewpoint, but it doesn't!
- Why not?

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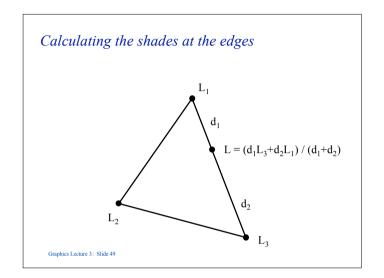




Using Shading

• Flat Shading:

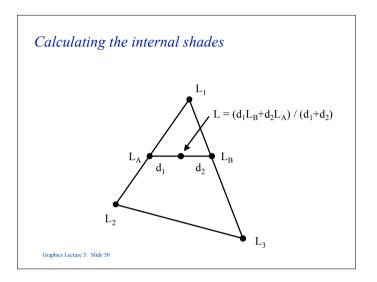
- Each polygon is shaded uniformly over its surface.
- The shade is computed by taking a point in the centre and the surface normal vector. (Equivalent to a light source at infinity)
- Usually only diffuse and ambient components are used.
- Interpolation Shading:
 - A more accurate way to render a shaded polygon is to compute an independent shade value at each point.
 - This is done quickly by interpolation:
 - 1. Compute a shade value at each vertex
 - 2. Interpolate to find the shade value at the boundary
 - 3. Interpolate to find the shade values in the middle

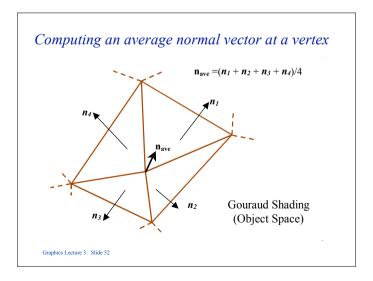




- In addition to interpolating shades over polygons, we can interpolate them over groups of polygons to create the impression of a smooth surface.
- The idea is to create at each vertex an averaged intensity from all the polygons that meet at that vertex.







Smooth Shading

- Need to have per-vertex normals
- Gouraud Shading
 - Interpolate color across triangles
 - Fast, supported by most of the graphics accelerator cards
 - Can't model specular components accurately, since we do not have the normal vector at each point on a polygon.

Phong Shading

- Interpolate normals across triangles
- More accurate modelling of specular compoents, but slower.

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Interpolation of the 3D normals

• We may express any point for this facet in parametric form:

$$\mathbf{P} = \mathbf{V}_{1} + \mu_{1}(\mathbf{V}_{2} - \mathbf{V}_{1}) + \mu_{2}(\mathbf{V}_{3} - \mathbf{V}_{1})$$

• The average normal vector at the same point may be calculated as the vector **a**:

$$\mathbf{a} = \mathbf{n}_1 + \mu_1(\mathbf{n}_2 - \mathbf{n}_1) + \mu_2(\mathbf{n}_3 - \mathbf{n}_1)$$

and then

$$\mathbf{n}_{\mathbf{average}} = \mathbf{a} / | \mathbf{a} |$$

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2D or 3D

- The interpolation calculations may be done in either 2D or 3D
- For specular reflections the calculation of the reflected vector and viewpoint vector must be done in 3D.