

Imperial College of Science, Technology and Medicine
Department of Computing

Computer Systems (M2) / Architecture, Tutorial 3 – Floating Point Numbers

1) Binary fractions are:

a) 5.5 is **101.1**

b) 8.25 is **1000.01**

c) 9 is 1001

0.3 □ **0.6, 1.2, 0.4, 0.8, 1.6, 1.2,**
= 01001 1001 1001 etc.

9.3 is **1001.01001 1001 1001** repeating etc

2) Convert the binary number 1001.1010101 to decimal.

1001 binary is 9 decimal

.	1	0	1	0	1	0	1	Sum =85
128	64	32	16	8	4	2	1	

Fraction = 85 /128 = 0.6640625

Number = **9.6640625**

3) a) 101.1 = **1.011 x 2²**

b) 1000.01 = **1.00001 x 2³**

c) 0.00010101 = **1.0101 x 2⁻⁴**

4) Convert -31.3 to IEEE Single Precision format.

First convert to a binary number -31.3 = -11111.01001 1001 1001

Next Normalise

$$1.11110 1001 1001 1001 1001 1001 \times 2^4$$

Significant field is **1111 0100 1100 1100 1100 110 (23 bits with 1. omitted)**

Exponent field is 4+127 = 131 = **1000 0011**

Number is -ve therefore Sign field is **1**

Sign	Exponent	Significant
1	1000 0011	1111 0100 1100 1100 1100 110

5) Convert the IEEE Single Precision format hex value C154 0000 to decimal.

C154 0000 = 1100 0001 0101 0100 0000 0000 0000 0000

Sign	Exponent	Significand
1	1000 0010	1010 1000 0000 0000 0000 000

Exponent field = 1000 0010 = 130 => Exponent = 130 - 127 = 3

Significand field = 10101 Adding Hidden Bit => 1.10101

Therefore number is $1.10101 \times 2^3 = 1101.01 = \text{Decimal } 13.25$

Sign is 1 therefore number is **-13.25**

6) Carry out the operation 31.3 + 13.25 in IEEE single precision arithmetic

Number	Sign	Exponent	Significand
31.3	0	1000 0011	1111 0100 1100 1100 1100 110
13.25	0	1000 0010	1010 1000 0000 0000 0000 000

Significand of Larger Number = 1.1111 0100 1100 1100 1100 110

Significand of Smaller Number = 1.1010 1000 0000 0000 0000 000

Exponents differ by 1. Therefore shift binary point of Smaller Number 1 place.

Significand of Larger Number = 1.1111 0100 1100 1100 1100 1100

Significand of Smaller Number = 0.1101 0100 0000 0000 0000 0000

Significand of Sum =

Sum = 10.1100 1000 1100 1100 1100 1100 $\times 2^4$

Normalise 1.01100 1000 1100 1100 1100 1100 $\times 2^5$

Sign	Exponent	Significand
0	1000 0100	0110 0100 0110 0110 0110 011

7)

Fraction	Binary	Decimal
1/4	0.01	0.25
3/8	0.011	0.375
23/16	1.0111	1.4375
45/16	10.1101	2.8125
11/8	1.011	1.375
45/8	101.101	5.625
49/16	11.0001	3.0625

8)

Bits	Binary value or special value	Decimal value or special value
0 00 00	0	0
0 00 01	0.01	0.25
0 00 10	0.10	0.50
0 00 11	0.11	0.75
0 01 00	1.00	1
0 01 01	1.01	1.25
0 01 10	1.10	1.5
0 01 11	1.11	1.75
0 10 00	10.0	2
0 10 01	10.1	2.5
0 10 10	11.0	3
0 10 11	11.1	3.5
0 11 00	∞	∞
0 11 01	NaN	NaN
0 11 10	NaN	NaN
0 11 11	NaN	NaN