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**Project:**  
***Internet Worm Attacks and Stochastic  
Agent Models***

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Produced with prosper and L<sup>A</sup>T<sub>E</sub>X

# Contention...

Passage or response times are useful in an agent modelling setting

# Presentation

- Internet worms at work!
- A formal agent description
- Our existing techniques
- Other solutions methods

# Lifecycle of an Internet Worm

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5. Repeat from (2) for each new infection



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4. server may be repaired and patched
5. server may be rolled back, thus removing patch

# Internet worms

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- ➔ Usually malicious autonomous program that spreads without user intervention
- ➔ **Emergent behaviour:** causes huge network bottlenecks – brings internet to standstill for many hours, or even days



# Code Red II

- ➔ Example: Code Red II
  - ➔ 19th July 2001
  - ➔ 350,000 hosts infected in 14 hours
  - ➔ c.f. Sasser: 1–1.5 million hosts in 2 days
  - ➔ utilised *buffer overflow* in Microsoft IIS web server
  - ➔ infected machines would probe for other victims on port 80
  - ➔ 20th July 2001: mode changes from one of propagation to DDOS attack on the [www.whitehouse.gov](http://www.whitehouse.gov)

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- ⇒ infected computers/computers susceptible to infection will mix homogeneously
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  - ➔ Nicol et al use hybrid model of Internet worms: epidemiological/stochastic

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- ➔ Good news: We have an exact behavioural description of an individual worm in glorious detail

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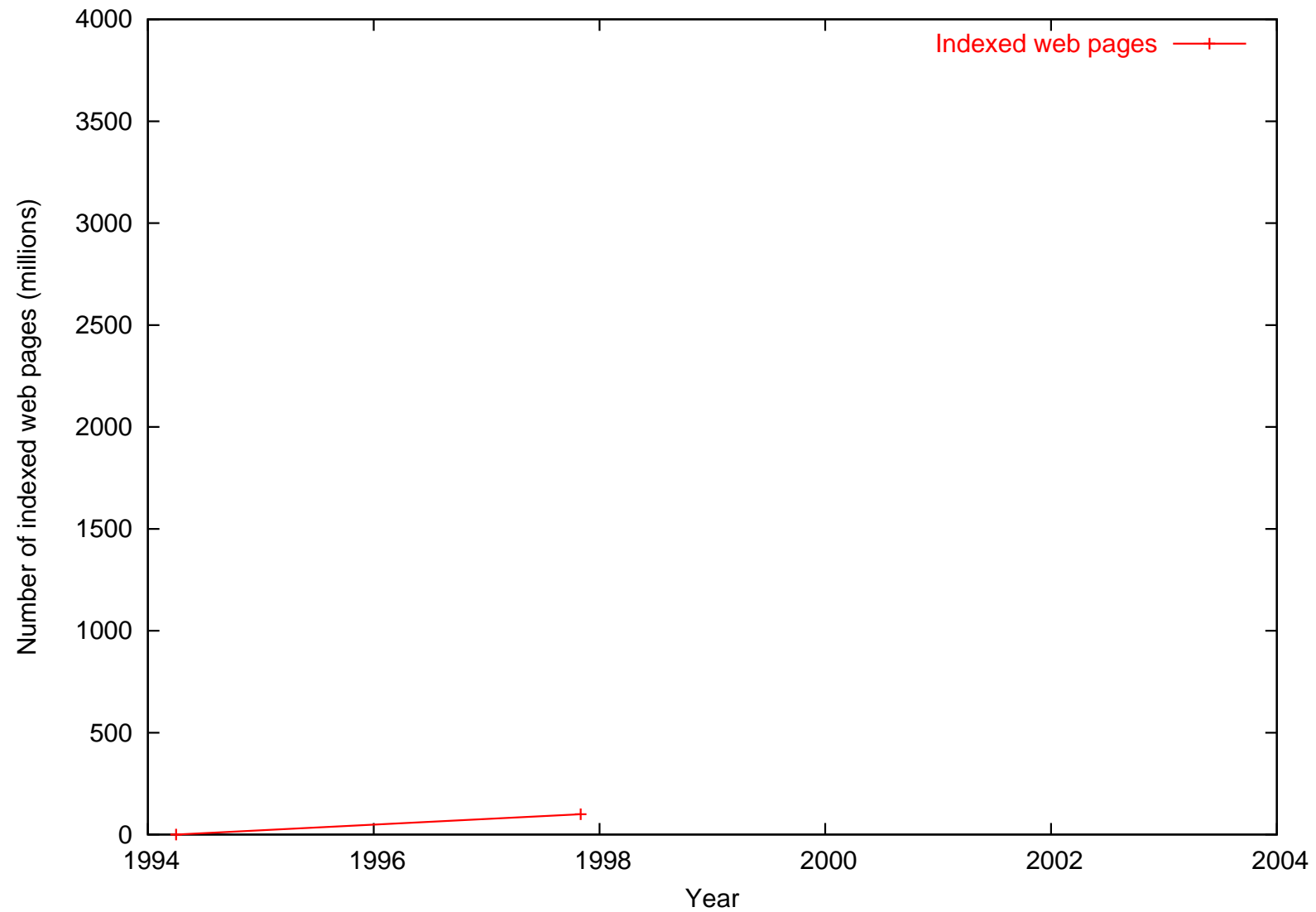
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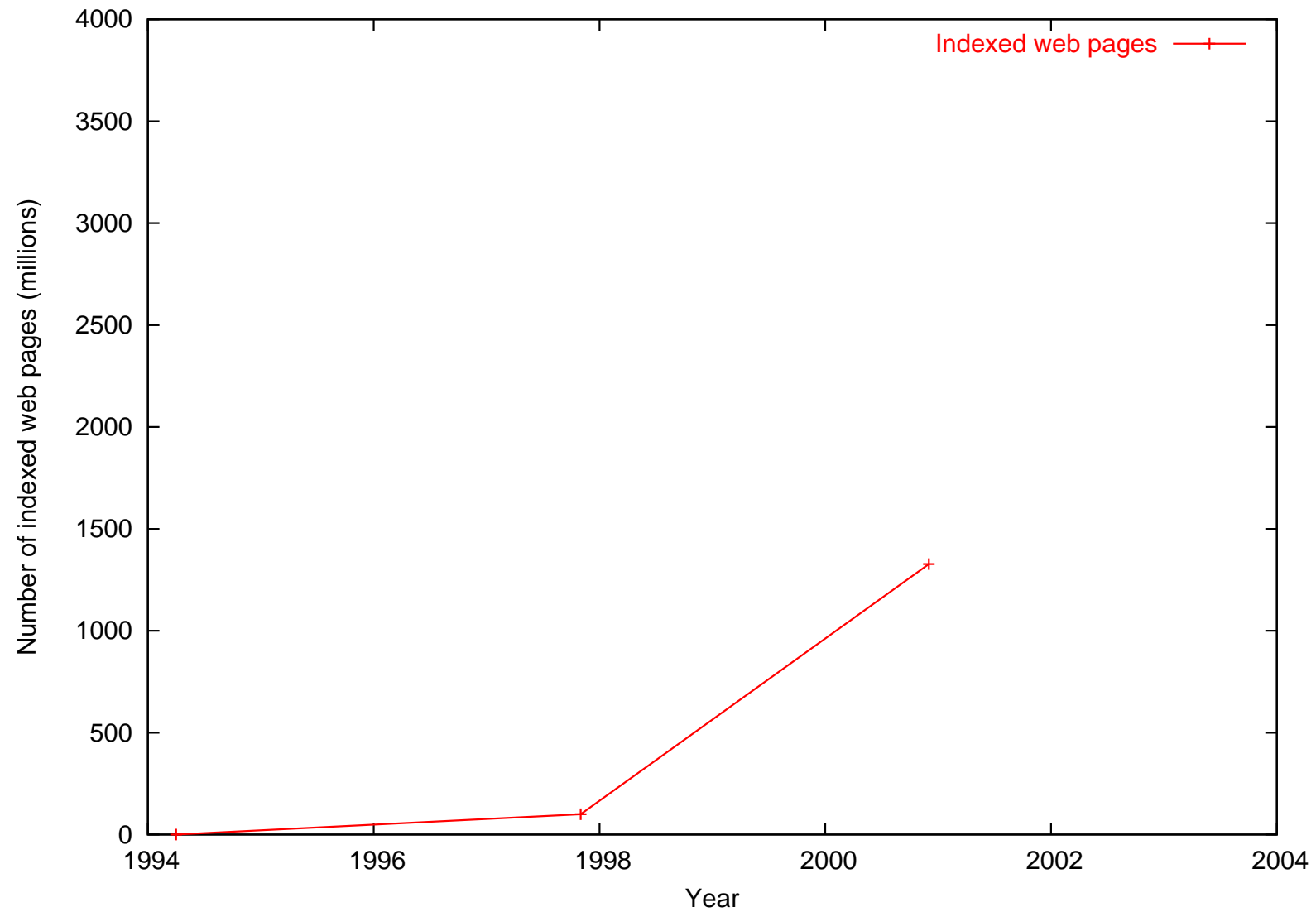
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- ⇒ We have to learn to prune *unimportant* behaviour

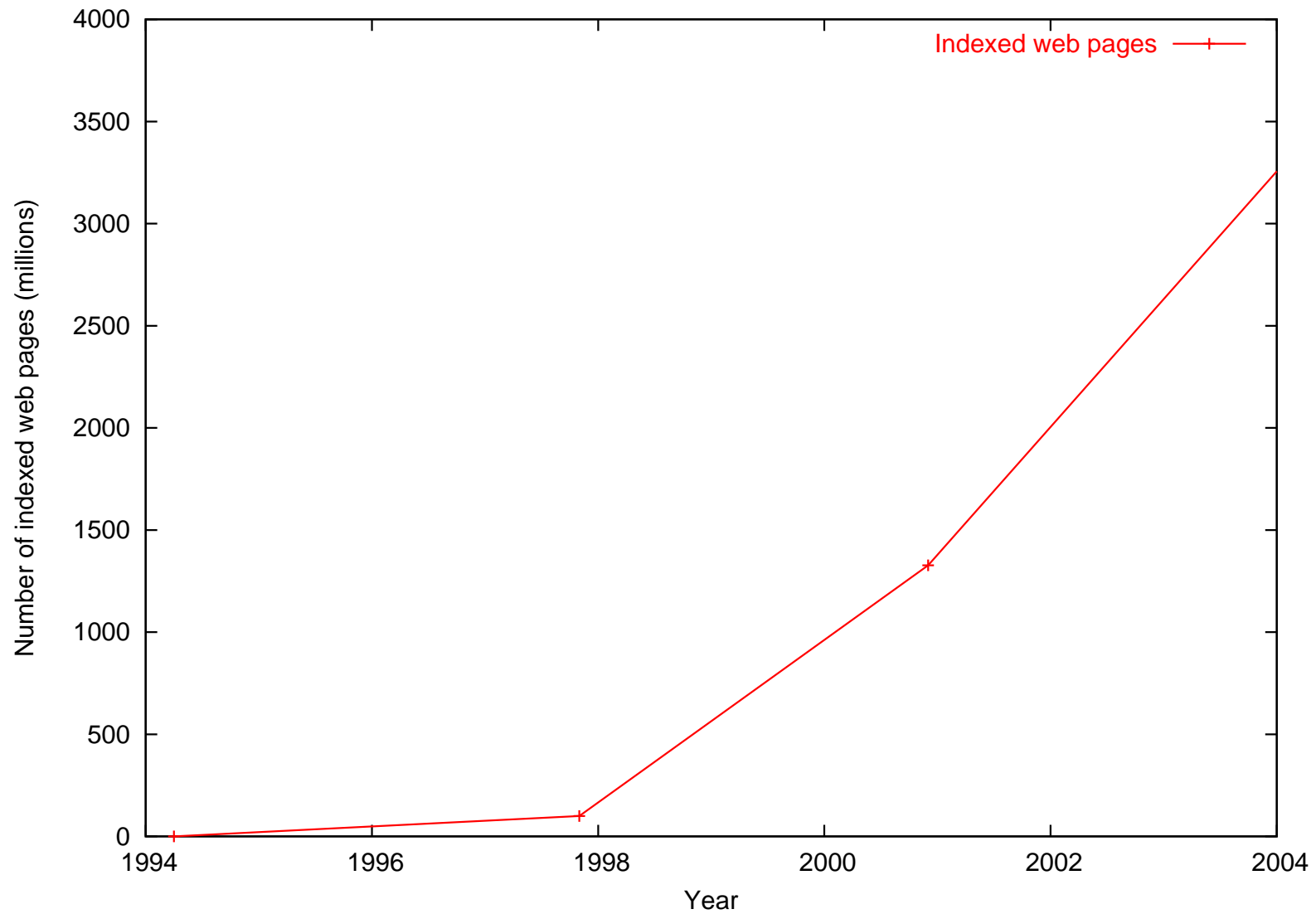
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# Stochastic Process Algebra

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# Biological PEPA Agent Modelling

Require a pairwise cooperation paradigm:

$$P ::= (a, \lambda).P \mid P + P \mid P \underset{L}{\oplus} P \mid P/L \mid A$$

- ➔ Action prefix:  $(a, \lambda).P$
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- ➔ Pairwise agent cooperation:  $P_1 \underset{L}{\oplus} P_2$
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# Types of Analysis

## Steady-state and transient analysis in PEPA:

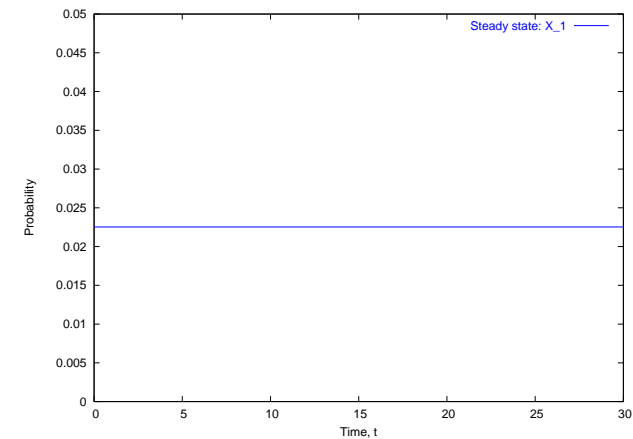
$A1 \stackrel{\text{def}}{=} (\text{start}, r_1).A2 + (\text{pause}, r_2).A3$

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$A3 \stackrel{\text{def}}{=} (\text{recover}, r_1).A1$

$AA \stackrel{\text{def}}{=} (\text{run}, \top).(\text{alert}, r_5).AA$

$\text{Sys} \stackrel{\text{def}}{=} AA \begin{array}{c} \diagup \diagdown \\ \{run\} \end{array} A1$



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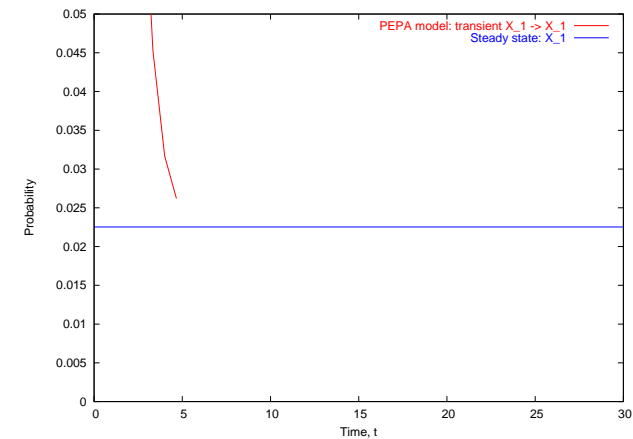
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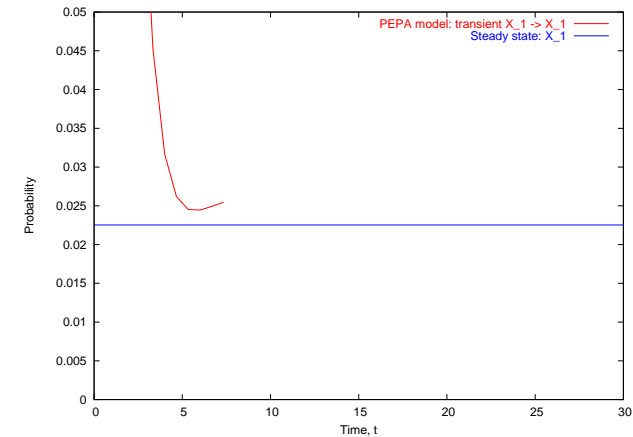
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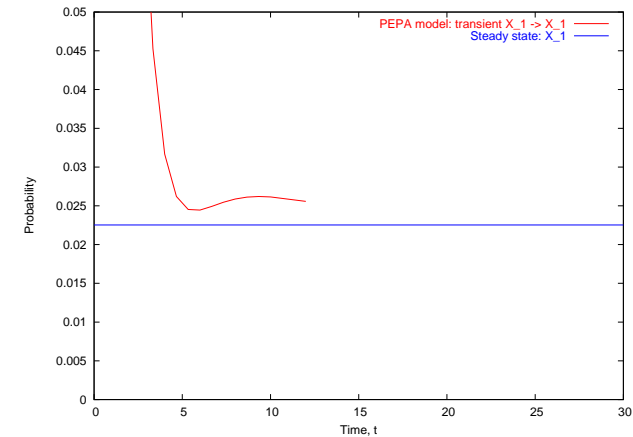
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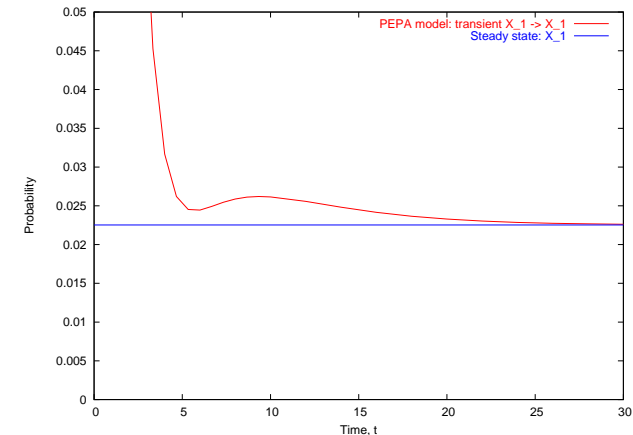
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# Passage-time Quantiles

Extract a passage-time density from a PEPA model:

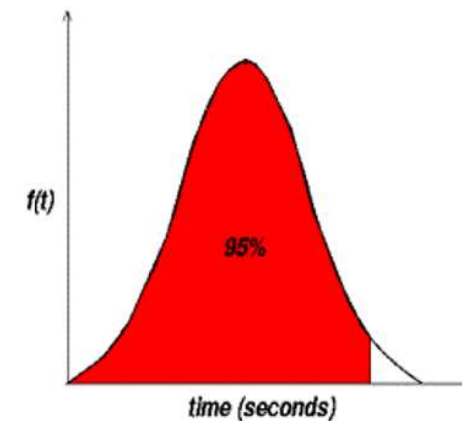
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# State of the Art

- ➔ Good news
  - ➔ PEPA model: passage time/transient analysis -  $O(10^8)$  states
  - ➔ Semi-Markov PEPA: passage time/transient analysis -  $O(10^7)$  states

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- ➔ Bad news
  - ➔ This only represents 8 agents with 10 states each!

# Ways forward for PEPA Agent modelling

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- ➔ Either:
  - selective model aggregation
  - ⇒ allows use of passage/transient
  
- ➔ Or:
  - development of approximate techniques
  - ⇒ automated generation of MFA/ODE equations from PEPA model [c.f. Sumpter 2000, Hillston 2004]

# SIR: Epidemiological model

- ➔ Consider fixed population of  $N$  computers
- ➔ Partition population into, computers that are:
  - ➔ susceptible to infection,  $s(t)$
  - ➔ infected,  $i(t)$
  - ➔ removed,  $r(t)$
- ➔ Deterministic system:
  - ➔  $\frac{ds(t)}{dt} = -\beta s(t)i(t)$
  - ➔  $\frac{di(t)}{dt} = \beta s(t)i(t) - \gamma i(t)$
  - ➔  $\frac{dr(t)}{dt} = \gamma i(t)$

# Agent worm model

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Susceptible = (infect,  $\top$ ).Infected  
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Infected = (infect,  $\lambda_i$ ).Infected  
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$$\text{System}(p, q) = \bigoplus_{i=1}^p \text{Infected}_i \bigoplus_{i=1}^q \text{Susceptible}_i \\ \bigoplus_{i=1}^{N-p-q} \text{Removed}_i$$

# Analysis possibilities

Sumpter Look to count numbers of agents,  $A(t)$ , in a given state by solving a derived mean field equation (MFE)

$$f(t, i) = \mathbb{E}(A(t + \Delta t) \mid A(t) = i)$$

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➔ remodel using *bimodal assumption*

# Agent Count-based Model

Bimodal characterisation of variables:

$$\begin{array}{l} S_H \stackrel{\text{def}}{=} (\text{infect}, \top).S_L \\ \quad + (\text{patch}, r_2).S_L \\ S_L \stackrel{\text{def}}{=} (\text{rollback}, \lambda_s).S_H \\ \vdots \quad \quad \quad \vdots \end{array} \Rightarrow \begin{array}{l} \frac{ds(t)}{dt} = -\beta s(t)i(t) \\ \frac{di(t)}{dt} = \beta s(t)i(t) - \gamma i(t) \\ \frac{dr(t)}{dt} = \gamma i(t) \end{array}$$

# Conclusion

- ➔ Internet worms have a reasonable biological analogy
- ➔ State spaces too large for traditional temporal modelling
- ➔ The answer: Selective aggregation/agent counting
- ➔ Passage times in an agent setting
  - ➔ a useful cost function for a model
  - ➔ probability of extinction within a given time