



# UKPEW 2005 Invited Talk

## *The Future is Collaborative Performance Engineering!*

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Produced with prosper and L<sup>A</sup>T<sub>E</sub>X

# Drowning!

- ➔ We are drowning in modelling techniques and formalisms:
  - ➔ SPA (Stochastic Process Algebras)
  - ➔ SAN (Stochastic Automata Networks)
  - ➔ SPN (Stochastic Petri Nets)
  - ➔ LQN (Layered Queueing Networks)
  - ➔ ...

# Drowning!

- ➔ We have underlying models:
  - ➔ CTMC (Continuous Time Markov Chains)
  - ➔ DTMC (Discrete Time Markov Chains)
  - ➔ MDP (Markov Decision Processes)
  - ➔ MRP (Markov Reward Processes)
  - ➔ SMP (Semi Markov Processes)
  - ➔ GSMP (Generalised Semi Markov Processes)
  - ➔ ...

# Drowning!

- ➔ Not to mention analysis techniques:
  - ➔ steady-state analysis
  - ➔ transient analysis
  - ➔ passage time analysis
  - ➔ entropy maximisation
  - ➔ simulation
  - ➔ continuous approximation
  - ➔ ...

# Drowning!

- ➔ ...performance query formalisms
  - ➔ CSL/eCSL/aCSL
  - ➔ pCTL
  - ➔ stochastic probes
  - ➔ NICE automata
  - ➔ ...

# Drowning!

- ➔ ...and tools:
  - ➔ ETMCC
  - ➔ PRISM
  - ➔ ipc/DNAmaca
  - ➔ PEPA workbench
  - ➔ DSPNexpress
  - ➔ SMARTA
  - ➔ Two Towers
  - ➔ GreatSPN
  - ➔ Möbius
  - ➔ ... and many others...

# Some questions

- ➔ Do all the tools produce the same results for the same questions and models?
- ➔ Are some tools/formalisms/performance models better at capturing/modelling certain systems better than others?
- ➔ Which tools run faster on which type of model? Is this because they use BDDs/out-of-core solvers/MDDs/hypergraph partitioning?
- ➔ Are we reinventing the wheel?... in terms of tools and models?

# An answer...?

- ➔ The answer is another tool: Perform-DB!
- ➔ Not quite! More an *integrated collaborative performance engineering environment*
- ➔ Encourage a *performance engineering lifecycle*

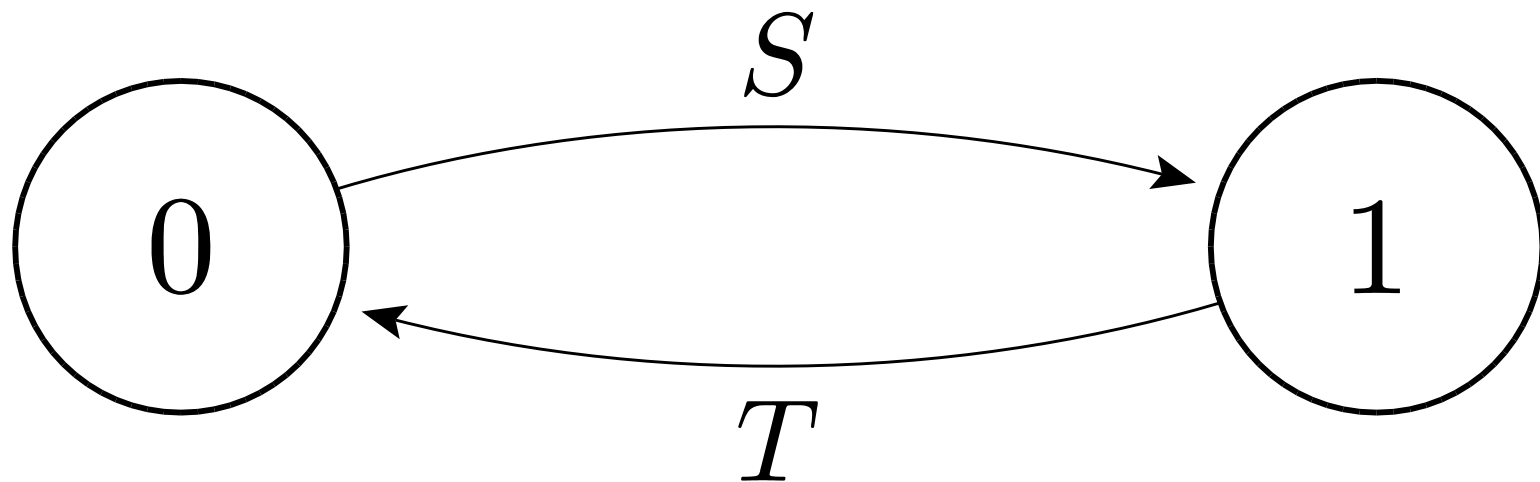


# A small but significant example...

➔ Fully deterministic system:

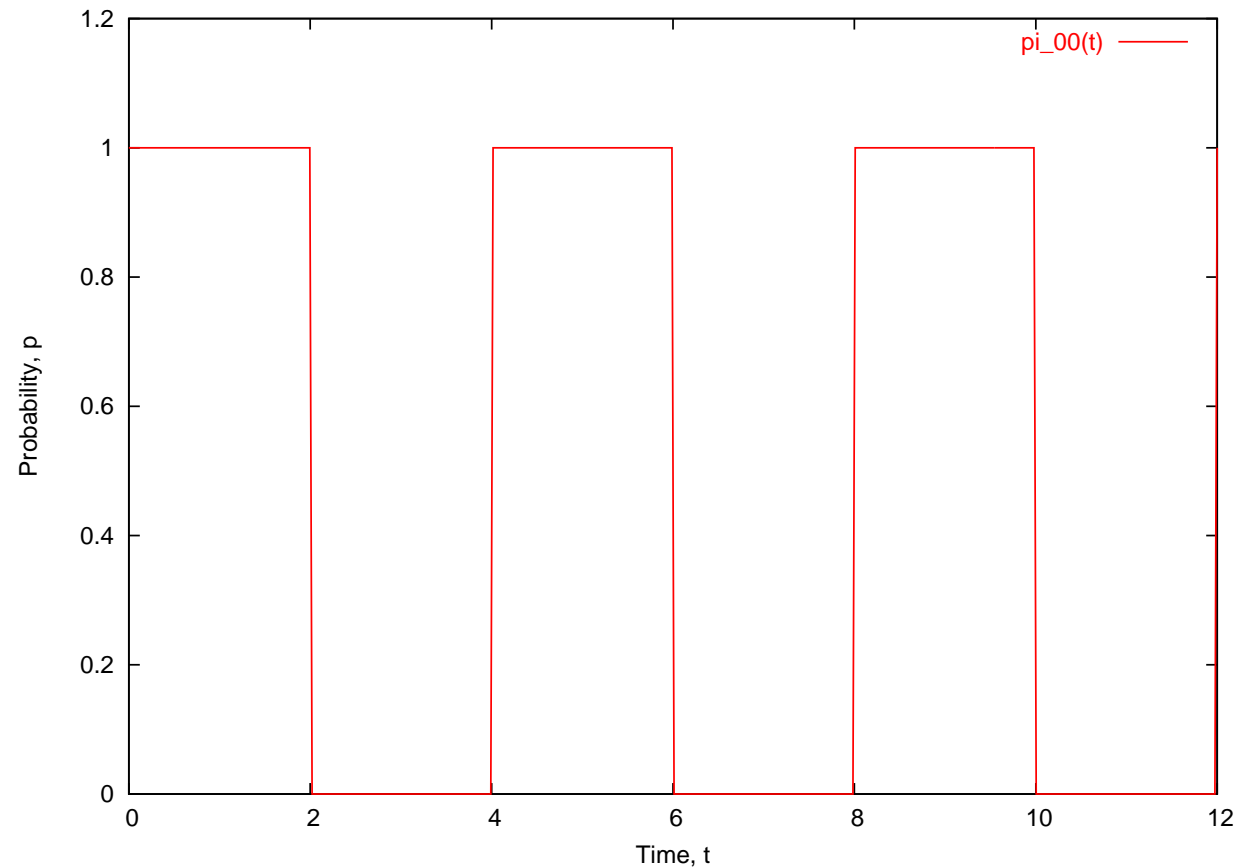
➔  $S \sim \text{det}(1)$

➔  $T \sim \text{det}(1)$



# Transient analysis...

- ➔  $\pi_{00}(t)$  : probability of being in state 0 having started in state 0

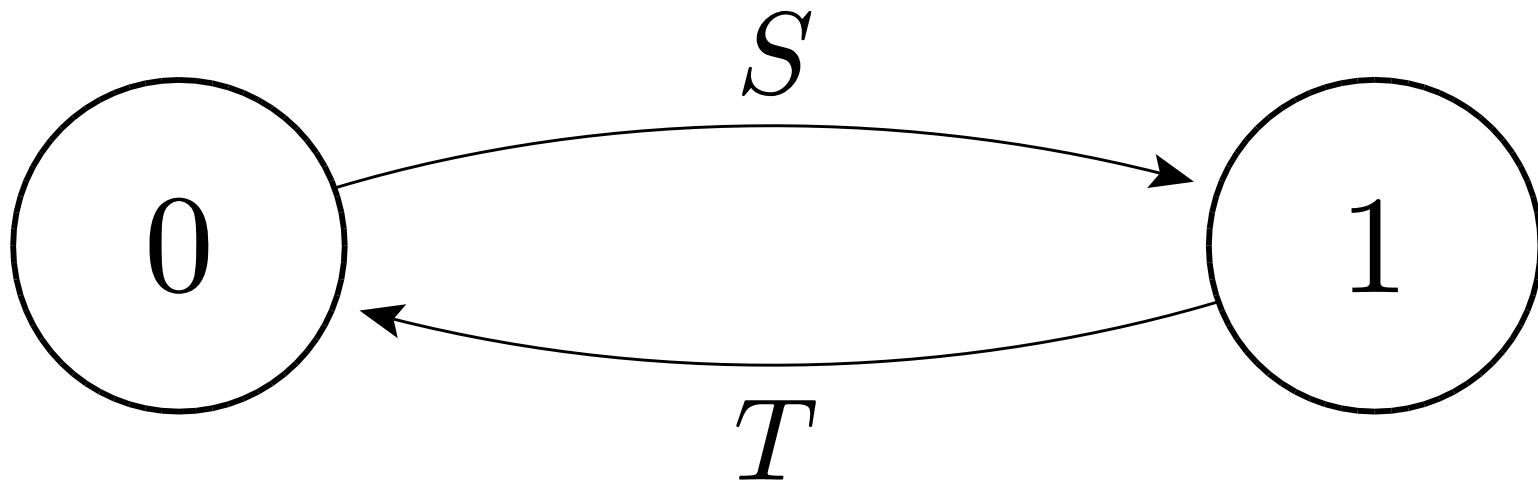


# With a small bit of randomness

➔ Semi deterministic system:

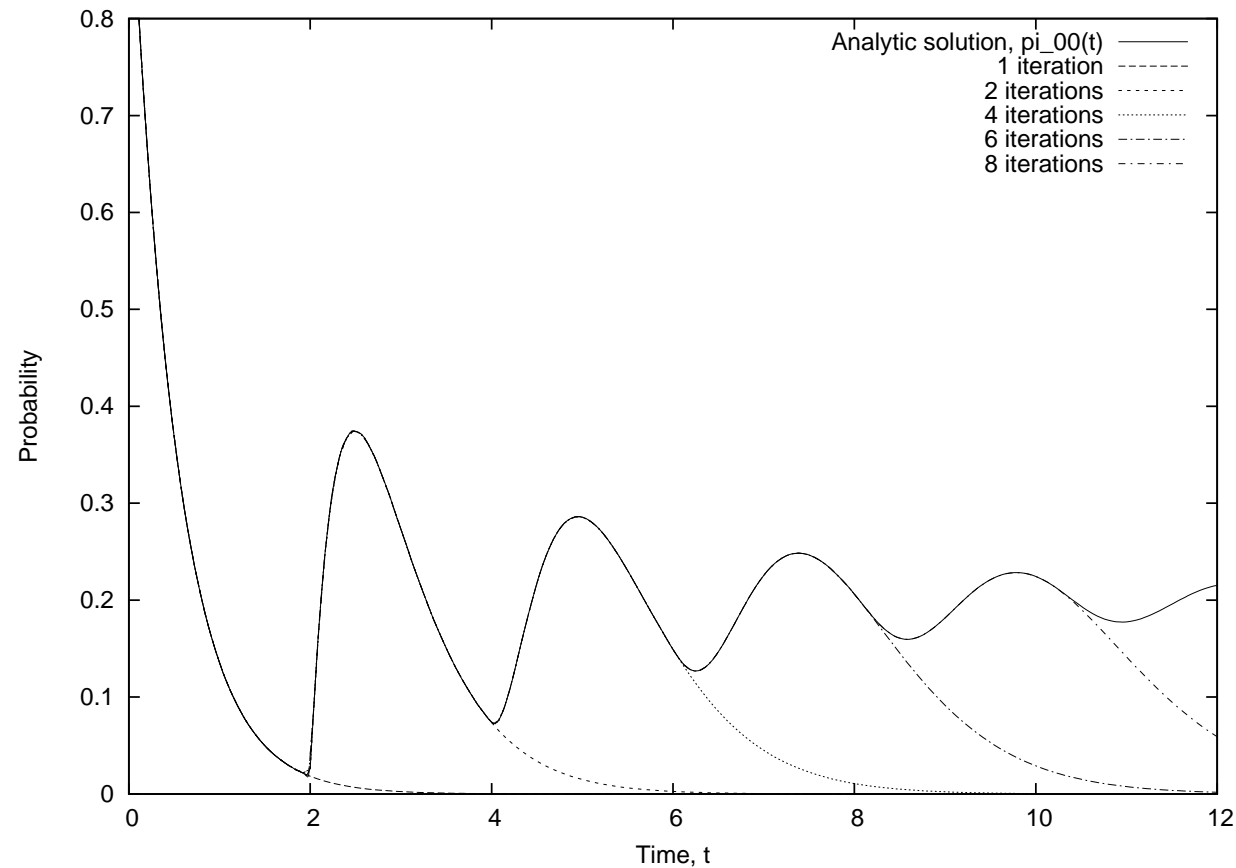
➔  $S \sim \exp(1)$

➔  $T \sim \det(1)$



# Transient analysis...

➔  $\pi_{00}(t)$  : probability of being in state 0 having started in state 0



# Stochastic Process Algebra

PEPA syntax:

$$P ::= (a, \lambda).P \mid P + P \mid P \boxtimes_L P \mid P/L \mid A$$

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- ➔ Competitive choice:  $P_1 + P_2$

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- ➔ Cooperation:  $P_1 \boxtimes_L P_2$



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# Stochastic Process Algebra

PEPA syntax:

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- ➔ Cooperation:  $P_1 \bowtie_L P_2$
- ➔ Action hiding:  $P/L$
- ➔ Constant label:  $A$

# PEPA: Example

$$\text{Sys} \stackrel{\text{def}}{=} (AA \bowtie_{\{\text{run}\}} A1) \bowtie_{\{\text{alert}\}} (BB \bowtie_{\{\text{run}\}} B1)$$

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$$\text{A1} \stackrel{\text{def}}{=} (\text{start}, r_1).\text{A2} + (\text{pause}, r_2).\text{A3}$$

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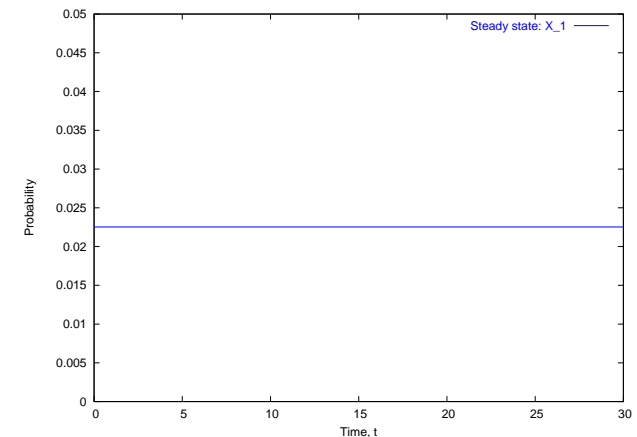
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# Types of Analysis

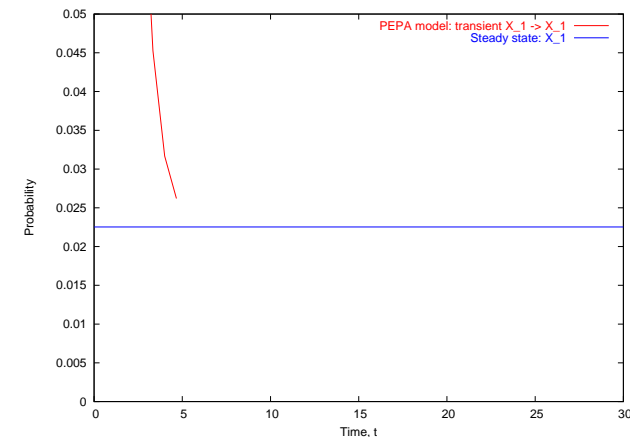
## Steady-state and transient analysis in PEPA:

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 \text{Sys} &\stackrel{\text{def}}{=} AA \bowtie_{\{run\}} A1
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# Types of Analysis

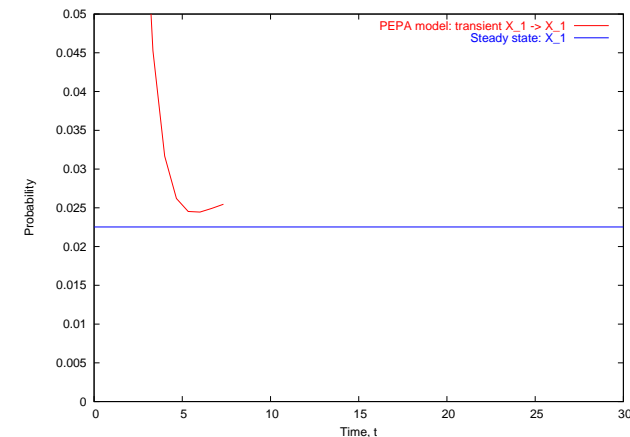
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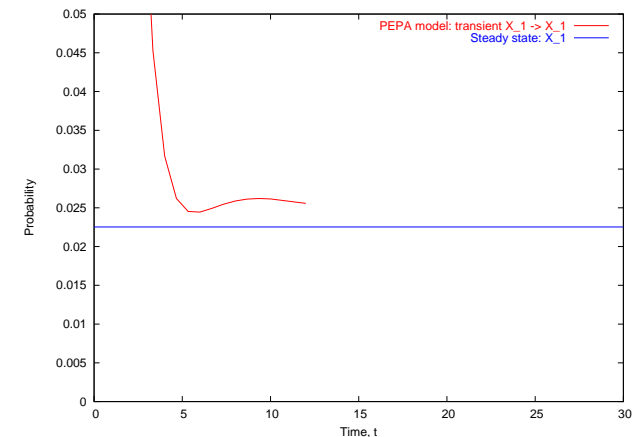
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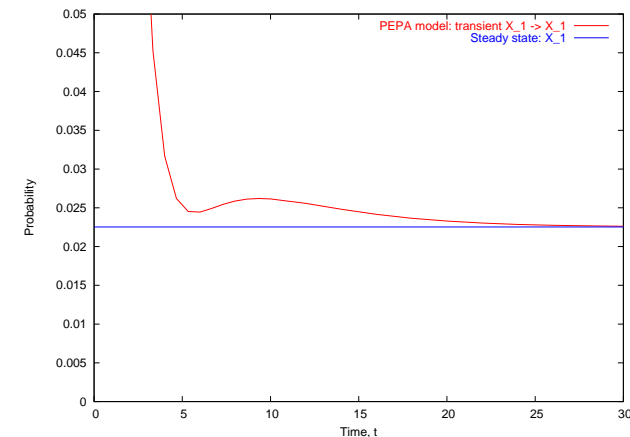
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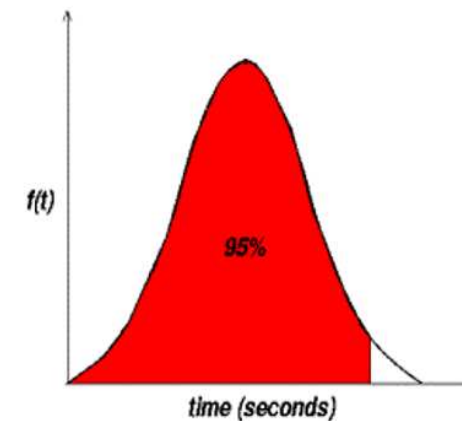
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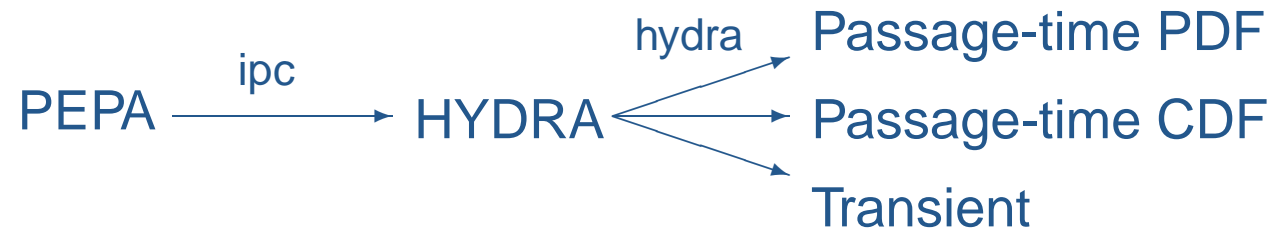


# Passage-time Quantiles

Extract a passage-time density from a PEPA model:

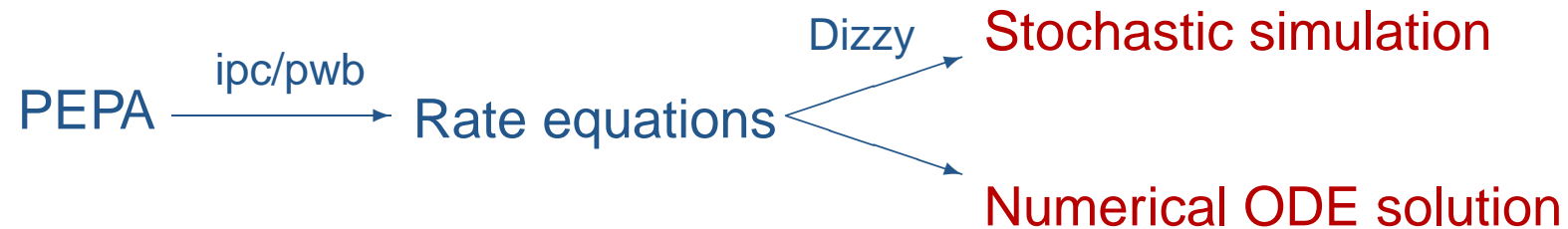
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# The story used to be...



- ➔ For state spaces of  $O(10^9)$
- ➔ Very precise probabilistic results

# Now the story is...



- ➔ For very large state spaces, e.g.  $10^{1000}+$  states
- ➔ Aggregate deterministic results

# Keeping track...

- ➔ Keeping track of:
  - ➔ model version
  - ➔ documentation of model version
  - ➔ type/version of query
  - ➔ parameter sets in model
  - ➔ tool version numbers
- ➔ ...is non-trivial



# Perform-DB

- ➔ Allow modellers to link to/import/alter! other peoples' models
- ➔ Keep track of model-result trail
  - model → query → result
- ➔ Allow modellers to compare results from:
  - different queries
  - different parameters
  - different models!

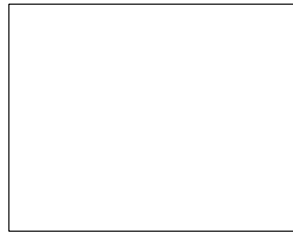
# Parameter Sweeping

Model

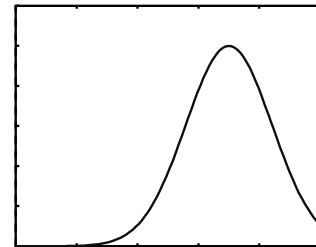
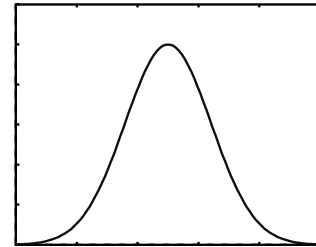
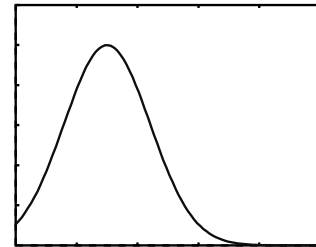
PEPA net

$$A \xrightarrow{L} B[B]$$
$$A \stackrel{\text{def}}{=} (up, \rho).A'$$
$$+ \dots$$

Rate parameter sweep



Results



# Parameter Sweeping

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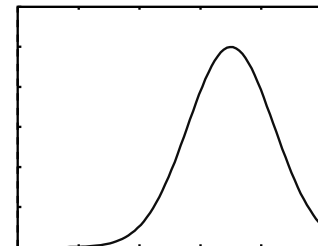
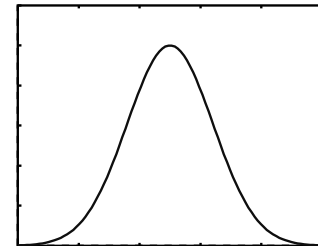
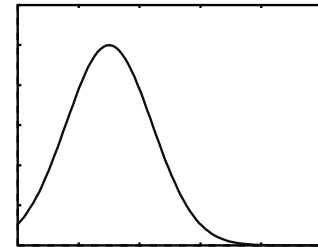
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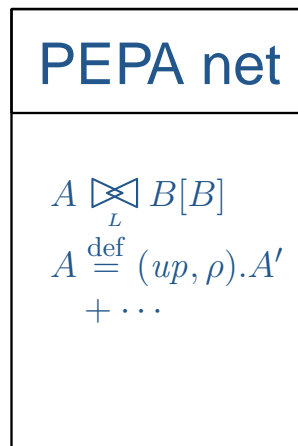
$$\rho = 0.8$$

Results



# Parameter Sweeping

Model



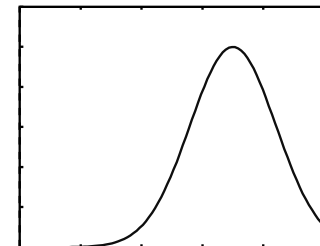
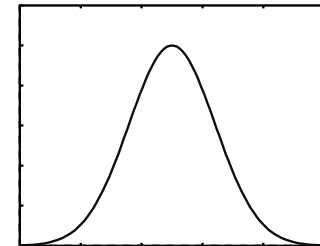
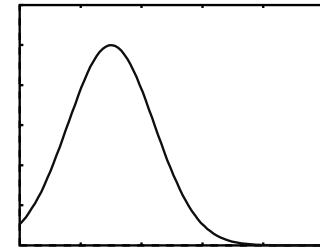
Rate parameter sweep

$$\rho = 0.8$$

$$\rho = 0.9$$

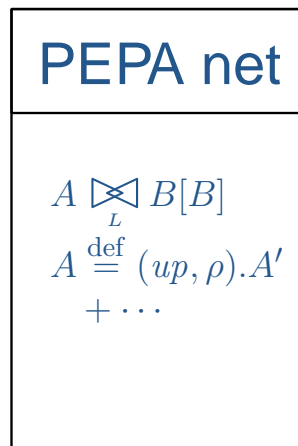


Results



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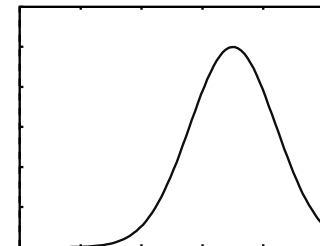
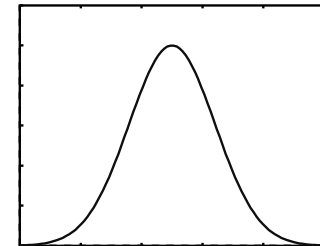
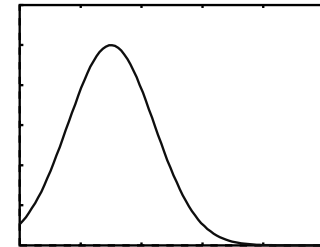
Rate parameter sweep

$$\rho = 0.8$$

$$\rho = 0.9$$

$$\rho = 1.0$$

Results



# Distinct formalism support

## Model description

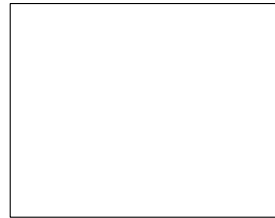
### GSPN

```
...  
\transition{t1}{  
  \condition{cpu>0}  
  \action{  
    cpu = cpu - 1;  
    id = id + 1;  
  }  
  \rate{mu}  
}  
...
```

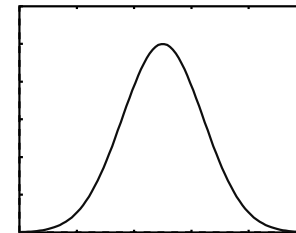
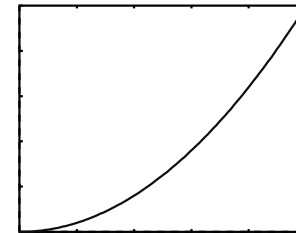
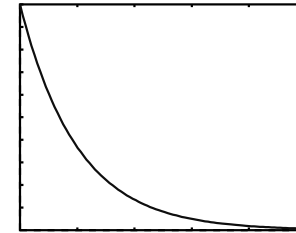
### PRISM m

```
...  
module queue  
  q : [0..N];  
  [] q < N ->  
    mu:(q'=q+1);  
  [] q = N ->  
    mu:(q'=q);  
  [serve] q > 0 ->  
    lambda:(q'=q-1);  
endmodule  
...
```

## Performance query



## Performance results



# Distinct formalism support

## Model description

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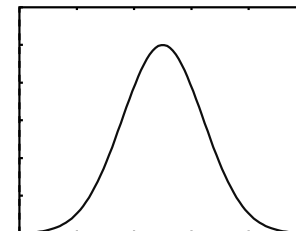
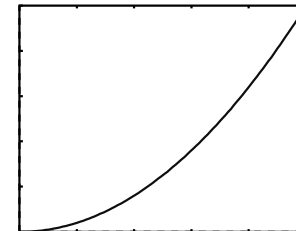
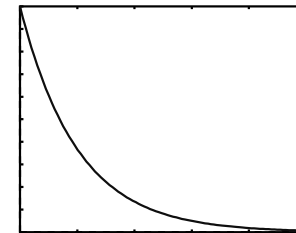
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endmodule
...
```

## Performance query

### Response time

```
\passage{
  \source{cpu==1}
  \target{id==1}
  \t_start{0.1}
  \t_stop{10.0} }
```

## Performance results



# Distinct formalism support

## Model description

### GSPN

```
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\transition{t1}{  
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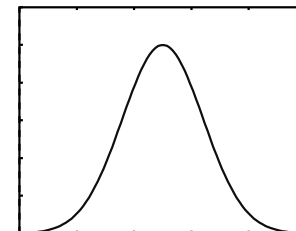
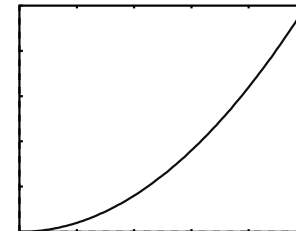
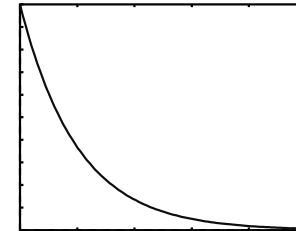
```
\passage{  
  \source{cpu==1}  
  \target{id==1}  
  \t_start{0.1}  
  \t_stop{10.0} }  
}
```

### Transient dist.

```
\transient{  
  \source{id==1}  
  \target{ex==1}  
  \t_start{0.1}  
  \t_stop{5.0} }  
}
```



## Performance results





# Distinct formalism support

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## Performance query

### Response time

```
\passage{
  \source{cpu==1}
  \target{id==1}
  \t_start{0.1}
  \t_stop{10.0} }
```

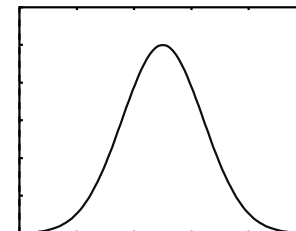
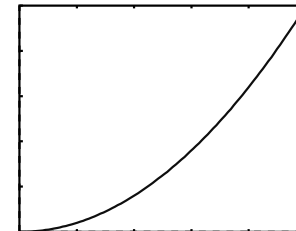
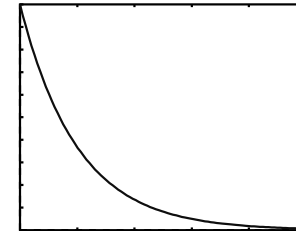
### Transient dist.

```
\transient{
  \source{id==1}
  \target{ex==1}
  \t_start{0.1}
  \t_stop{5.0} }
```

### CSL query

$serve \Rightarrow$   
 $\mathcal{P}(ar \mathcal{U}^{\leq t} fi)$

## Performance results



# More than a database...

- ➔ When can I reuse the results of someone else's model as well as the model itself
- ➔ separable solution
  - steady-state → RCAT, product-forms
  - passage-time/transient → ?

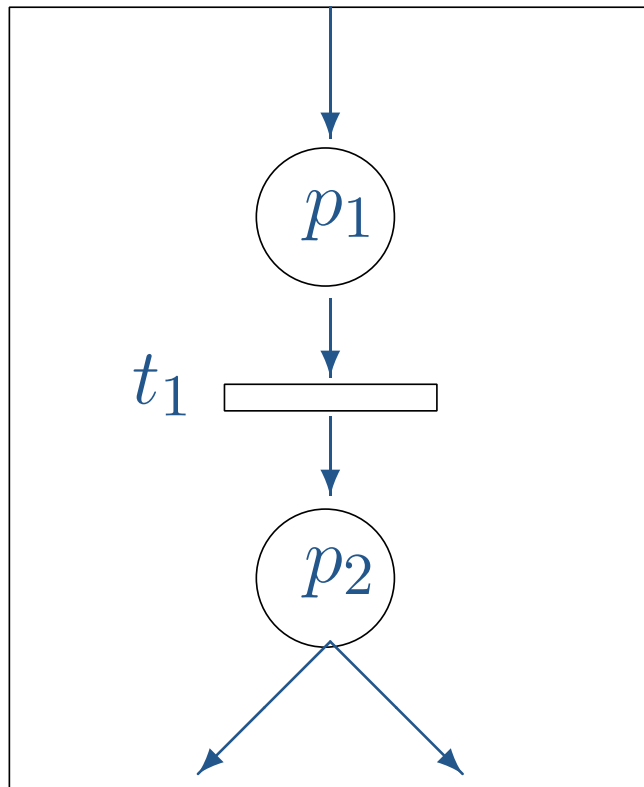
# Engineering collaboration

- ➔ use your tool/formalism of choice
- ➔ allow modellers to write system components in the formalism that best suits the component

# Interformalism synchronisation

- ➔ How can a stochastic Petri net model synchronise with stochastic process algebra component?
- ➔ ...or a PEPA component with a PRISM module?
- ➔ ...or an IMC component with a Stochastic automata network?

# Interformalism synchronisation



$$A \stackrel{\text{def}}{=} (a, \nu).A'$$

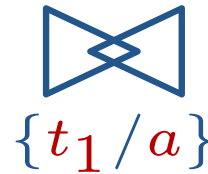
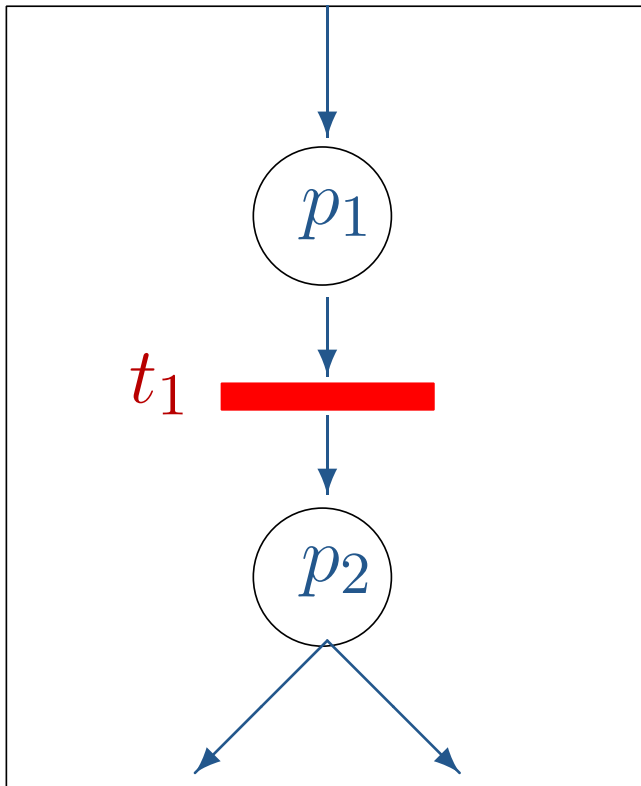
$$A' \stackrel{\text{def}}{=} (b, \top).A$$

$$B \stackrel{\text{def}}{=} (c, \lambda).B'$$

$$B' \stackrel{\text{def}}{=} (b, \mu).B$$

$$Sys \stackrel{\text{def}}{=} A \underset{\{b\}}{\bowtie} B$$

# Interformalism synchronisation



$$A \stackrel{\text{def}}{=} (\textcolor{red}{a}, \nu).A'$$

$$A' \stackrel{\text{def}}{=} (b, \top).A$$

$$B \stackrel{\text{def}}{=} (c, \lambda).B'$$

$$B' \stackrel{\text{def}}{=} (b, \mu).B$$

$$Sys \stackrel{\text{def}}{=} A \begin{array}{c} \diagup \diagdown \\ \{b\} \end{array} B$$

# User-definable semantics

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- ➔ My idea of how a DSPN should communicate with a SAN will differ from another modeller
- ➔ user-definable cooperation semantics
- ➔ user-definable translation semantics

# Conclusion

- ➔ Integrate with some parallelised toolsets: e.g. ETMCC, PRISM, DNAmaca, PWB
- ➔ Attach to a large cluster computer
- ➔ Allow jobs to be received/sent to other Perform-DB enabled clusters
- ➔ Hopefully has potential!