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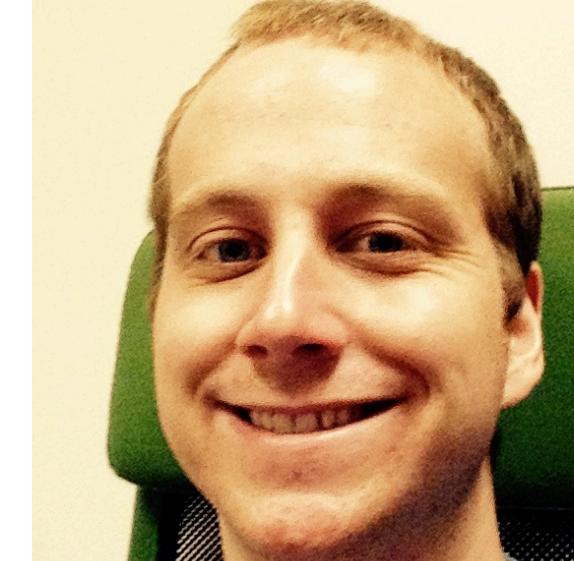
# Automatically Comparing Memory Consistency Models



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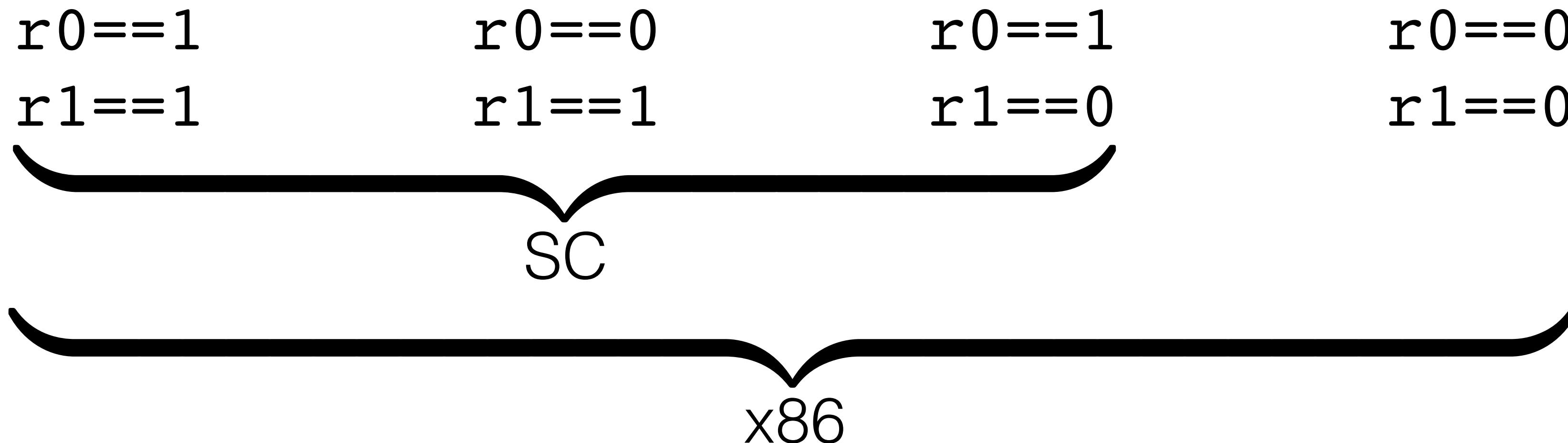
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# Memory Models

```
x = 1;      || y = 1;  
r0 = y;    || r1 = x;
```



# Summary

- **The problem is** that memory models are complex and counterintuitive. Misunderstanding them has led to lots of bugs.
- **Our contribution is** a technique for automatically generating litmus tests that distinguish two models.
- **This is useful because** we can compare two variants of a model, and we can debug compilers.

# Three tasks

1. To show that **M** is **stronger** than **N**:
  - find  $P, \sigma$  where  $\sigma \notin \llbracket P \rrbracket_M$  and  $\sigma \in \llbracket P \rrbracket_N$ .
2. To show that a **compiler optimisation** on **M** is unsound:
  - find  $P, Q, \sigma$  where  $\sigma \notin \llbracket P \rrbracket_M$ ,  $P$  optimises to  $Q$ , and  $\sigma \in \llbracket Q \rrbracket_M$ .
3. To show that a **compiler mapping** from **M** to **N** is unsound:
  - find  $P, Q, \sigma$  where  $\sigma \notin \llbracket P \rrbracket_M$ ,  $P$  maps to  $Q$ , and  $\sigma \in \llbracket Q \rrbracket_N$ .

# Related work

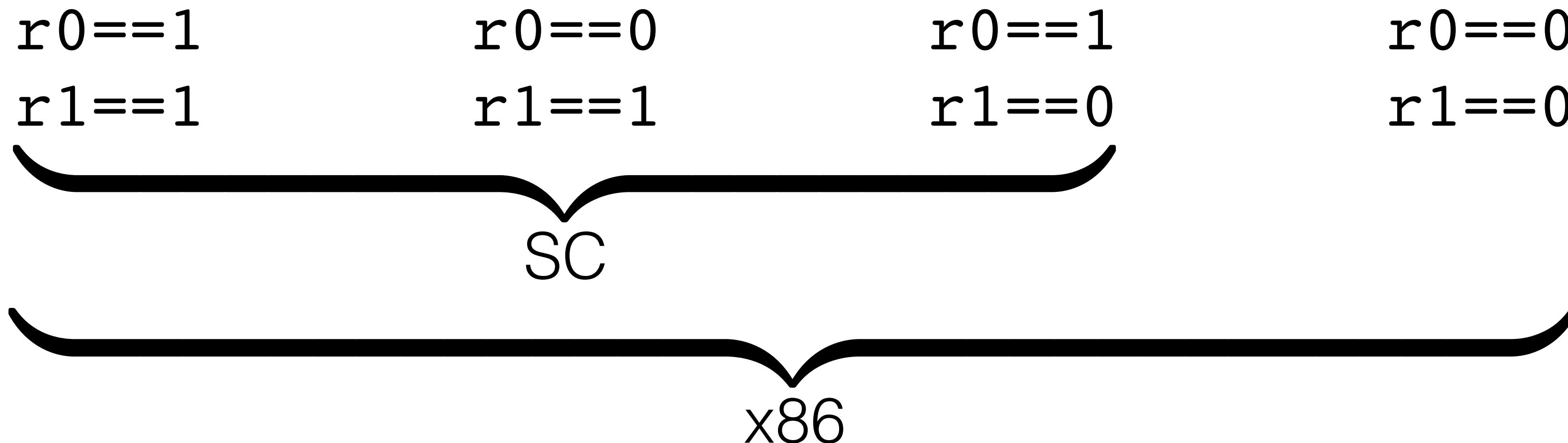
	<b>Manual c'examples</b>	<b>Manual proofs</b>	<b>Automatically</b>
<b>Comparing memory models</b>	[Batty et al. <i>POPL'16</i> ] [Nienhuis et al. <i>OOPSLA'16</i> ] [Lahav et al. <i>POPL'16</i> ]	[Owens et al. <i>TPHOLs'09</i> ] [Mador-Haim et al. <i>CAV'12</i> ]	[Mador-Haim et al. <i>CAV'10</i> ] <b>THIS WORK</b>
<b>Checking compiler optimisations</b>	[Vafeiadis et al. <i>POPL'15</i> ]	[Sevcik <i>PLDI'11</i> ]	[Burckhardt et al. <i>CC'10</i> ] [Chakraborty et al. <i>CGO'16</i> ] <b>THIS WORK</b>
<b>Checking compiler mappings</b>	[Wickerson et al. <i>OOPSLA'15</i> ]	[Batty et al. <i>POPL'11</i> ]	[Lustig et al. <i>MICRO'14</i> ] <b>THIS WORK</b>

# Results

	Previous work	Our tool (automatic)	Time taken
<b>Comparison:</b> Batty et al.'s C++ vs. original	7	5	<1 sec
<b>Comparison:</b> Lahav et al.'s C++ vs. original	10	6	1 sec
<b>Comparison:</b> Nienhuis et al.'s C++ vs. original	12	12	4 min
<b>Optimisation:</b> strengthening memory order in C++	8	7	1 min
<b>Optimisation:</b> thread linearisation in C++	6	6	5 sec
<b>Compiler mapping:</b> from OpenCL to AMD	12	11	22 min
<b>Compiler mapping:</b> from C++ to Power	14	14	2 min

# Memory Models

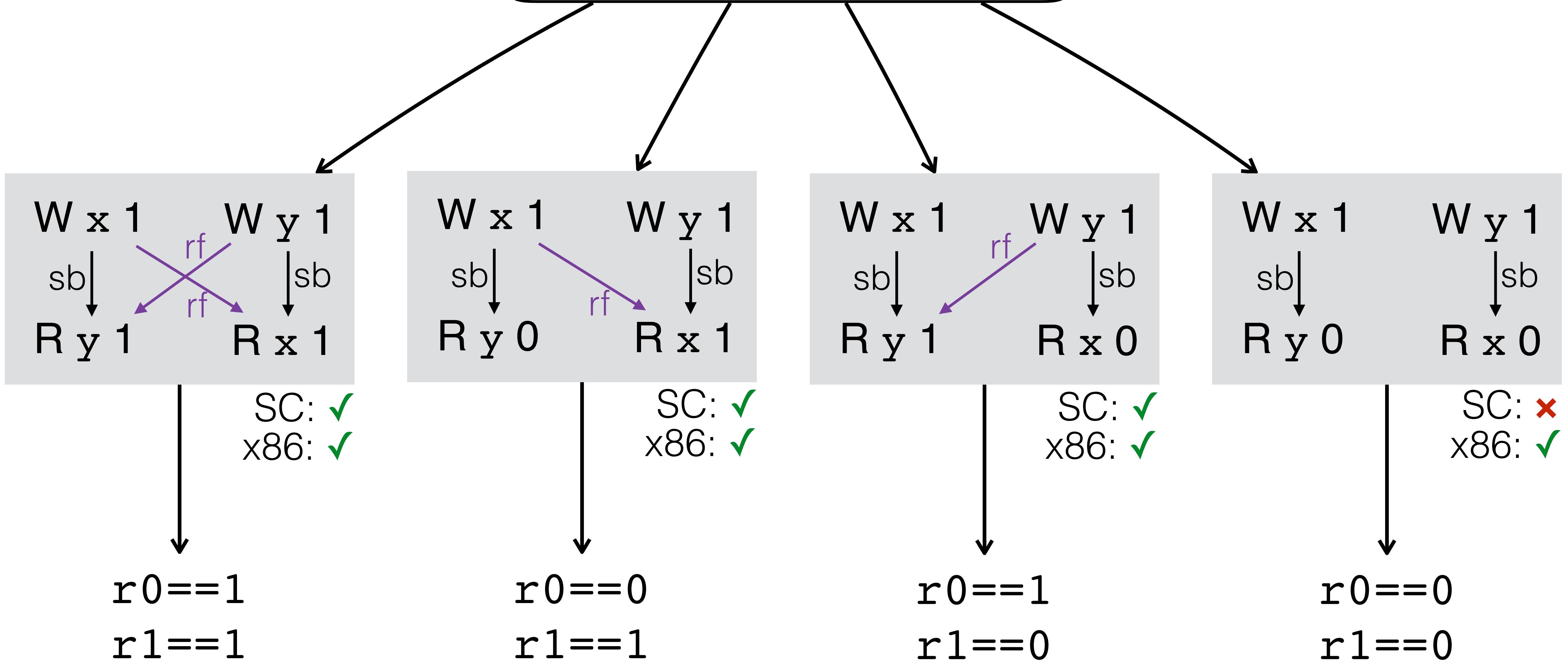
```
x = 1;      || y = 1;  
r0 = y;    || r1 = x;
```



```

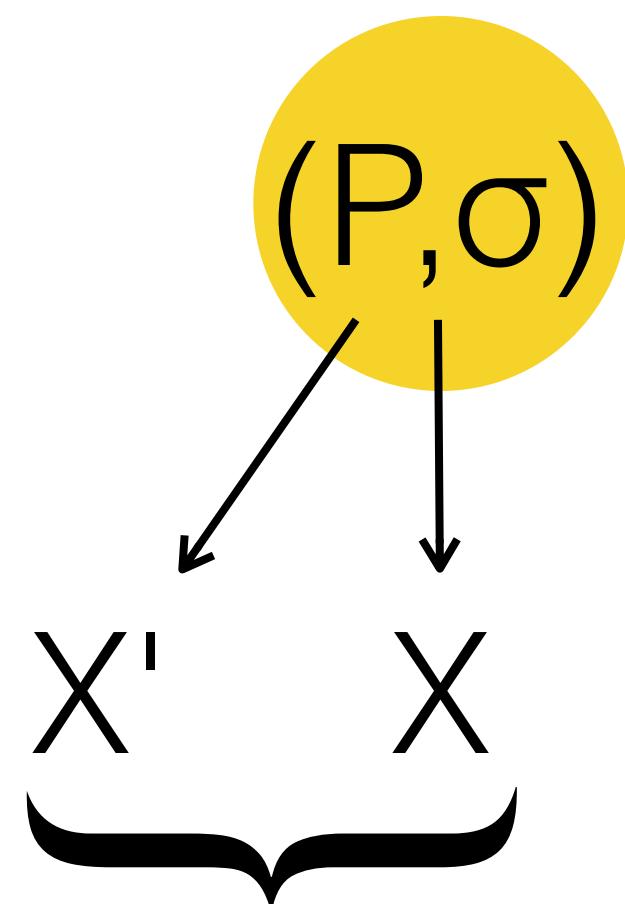
x = 1;      ||| y = 1;
r0 = y;      ||| r1 = x;

```



# Why is this tricky?

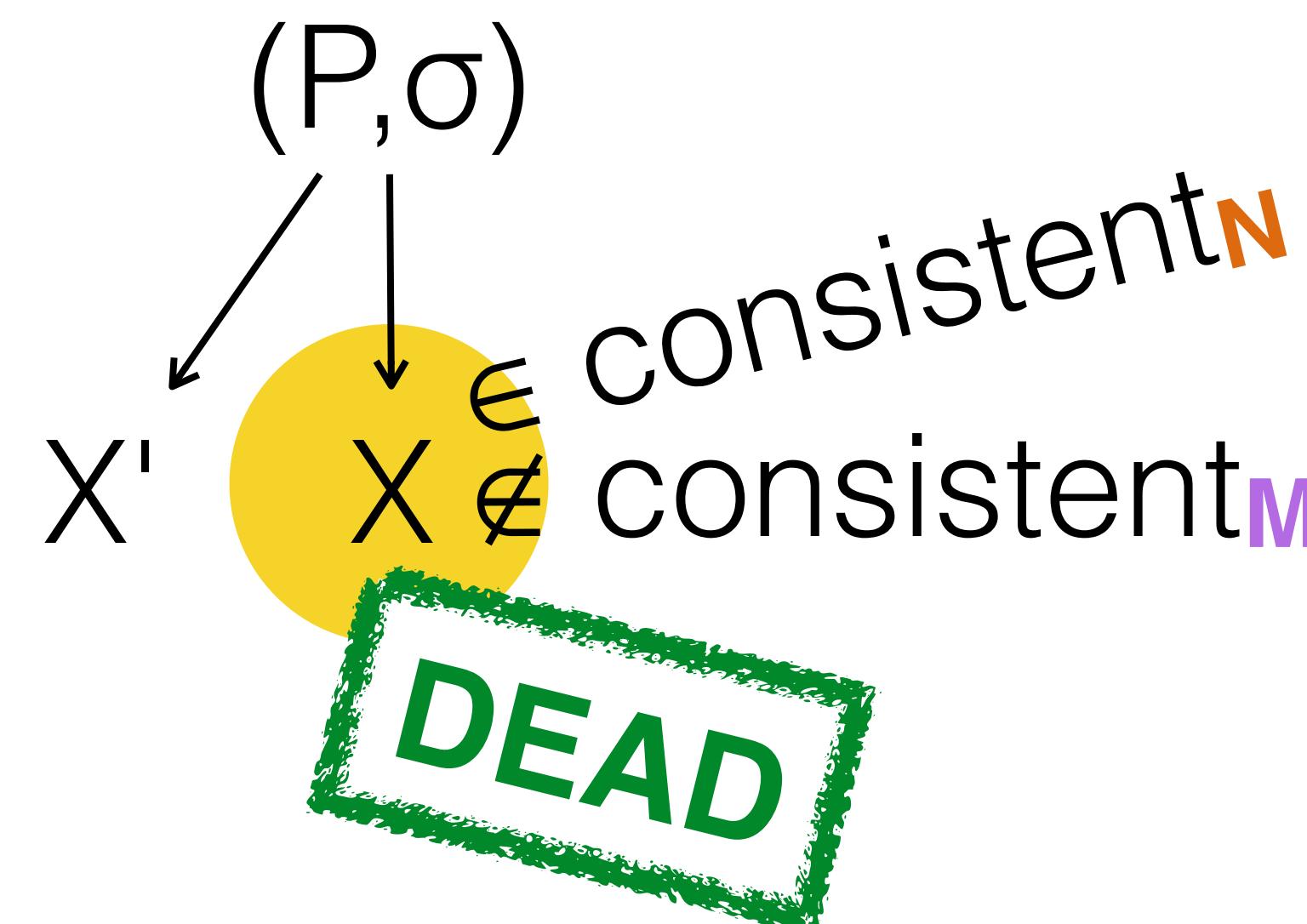
$$\{(P, \sigma) \mid \sigma \notin \llbracket P \rrbracket_{\textcolor{violet}{M}} \wedge \sigma \in \llbracket P \rrbracket_{\textcolor{brown}{N}}\}$$



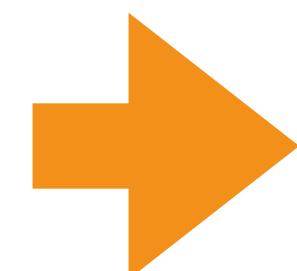
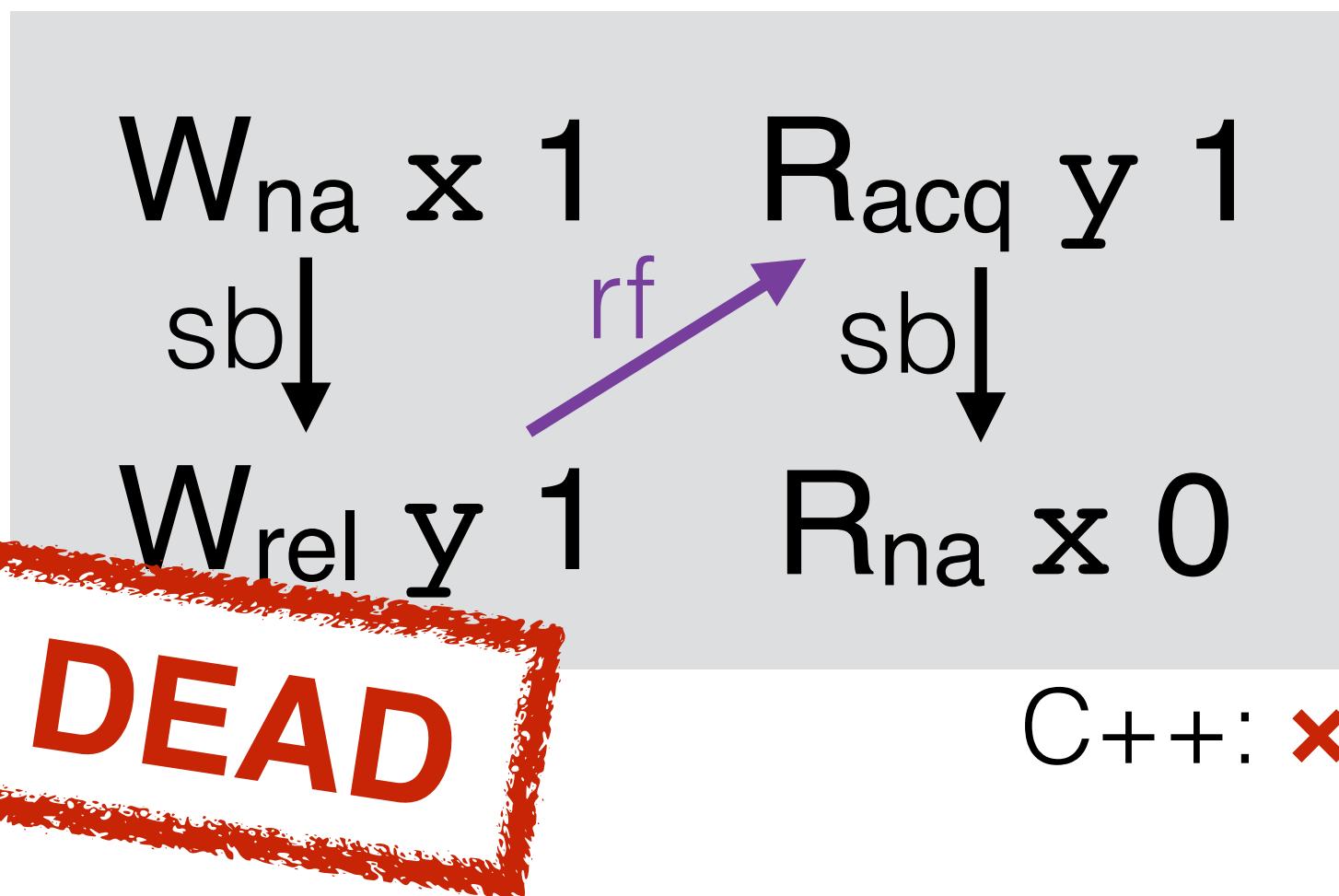
**all** are inconsistent under **M**  
**some** are consistent under **N**

# Our solution

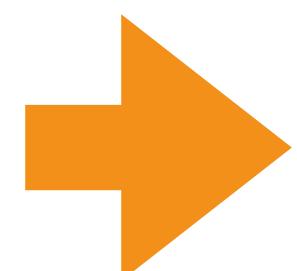
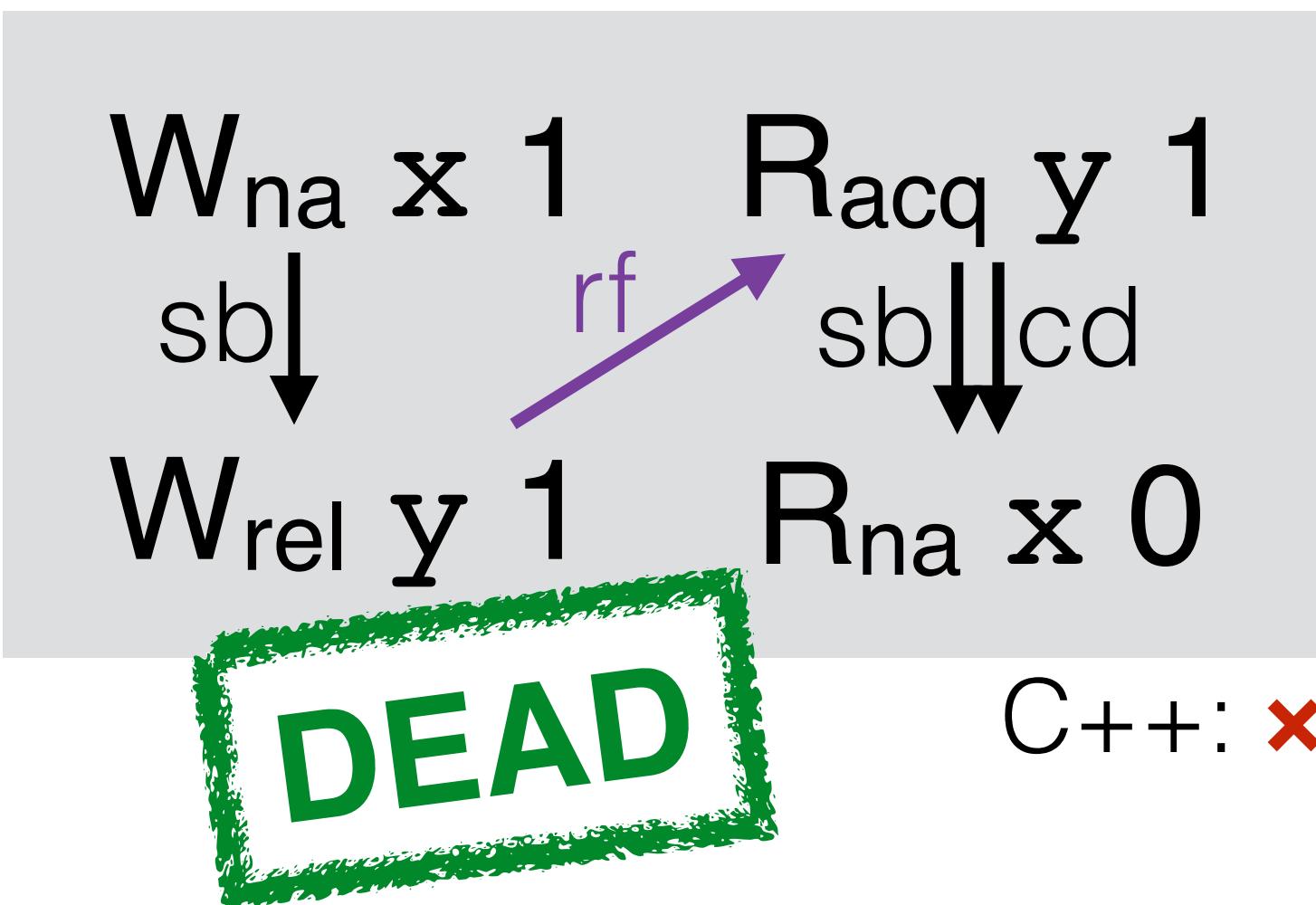
$$\{(P, \sigma) \mid \sigma \notin \llbracket P \rrbracket_M \wedge \sigma \in \llbracket P \rrbracket_N\}$$



# Generating useful tests



```
x=1;           || r0=ld(y,ACQ);  
st(y,1,REL); || r1=x;
```



```
x=1;           || r0=ld(y,ACQ);  
st(y,1,REL); || if(r0) r1=x;
```

# Conclusion

- **In summary:** we use Alloy to compare memory consistency models, and check for compiler bugs.
- **Future work:** how to extend our work to handle more recent styles of model like Promising model.