

C240 Computability and Complexity : Tutorial 2

1. Design a TM Z whose output is “hello world” on any input. So formally, the input/output function f_Z of Z is
$$f_Z(w) = \text{hello world}$$
for any word w of Z 's input alphabet (say, the roman alphabet).
2. (a) Design a Turing machine to solve the following problem:
The input is a word $\{1\}$ of length n . So before M starts to run its tape contains a 1 in squares $0, 1, \dots, n-1$ and blanks (\wedge) in all other squares. The problem is to determine whether n is even or odd. When M halts, square 0 of the tape should contain a 0 if n is even, and a 1 if n is odd. Square 1 should contain a blank.

(b) write down the input/output function of M in mathematical notation.
3. Describe a TM, R , that reverses a word of $\{0,1\}$.
So $f_R(00011) = 11000$, etc. Use ‘pseudocode’ or English description.