

C240 Computability and Complexity

Tutorial 4

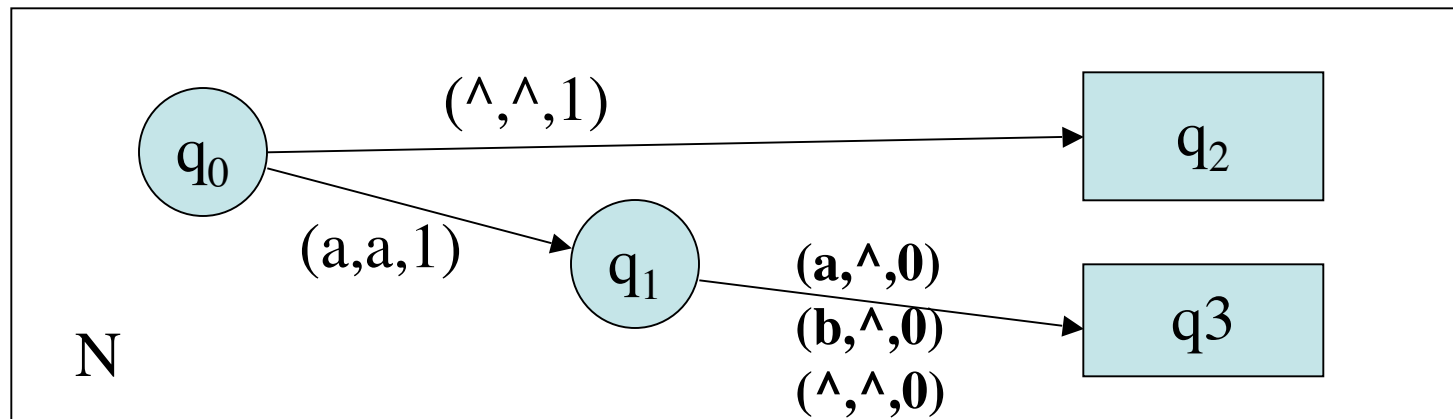
- Design a Turing Machine M with input alphabet $\{a, b\}$, which, given as input a word w of this alphabet, outputs the word obtained from w by writing out its a 's, and then its b 's, in order. For example:

$$f_M(ababaa) = aaabb$$

You may use pseudo-code or a flow-chart (state) diagram; in the latter case you should explain your notation for instructions.

You may use several tapes, and you can assume that square 0 of each tape is implicitly marked.

- What is meant by the term "standard Turing machine"?
 - What does the following standard Turing machine N do?
(ie. What is its input/output function?)



- The Universal Turing machine U can be made a standard Turing machine. So can M and N above. (assume M Halts & Fails if its input word is not in $\{a, b\}$. So they have codes, namely $\text{code}(U)$, $\text{code}(M)$, $\text{code}(N)$. Calculate

$$f_U(\text{Code}(U)*\text{code}(M)*\text{babba})$$

$$f_U(\text{code}(U)*\text{code}(N)*)$$

$$f_U\text{code}(U)*\text{code}(U)*\text{code}(N)*c$$