

# Concurrency Control

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# Topic 21: Serialisability and Recoverability

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# Transactions: ACID properties

## ACID properties

database management systems (DBMS) implements indivisible tasks called transactions

<b>Atomicity</b>	all or nothing
<b>Consistency</b>	consistent before → consistent after
<b>Isolation</b>	independent of any other transaction
<b>Durability</b>	completed transaction are durable

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BEGIN TRANSACTION

```
UPDATE branch
SET cash=cash-10000.00
WHERE sortcode=56
```

```
UPDATE branch
SET cash=cash+10000.00
WHERE sortcode=34
```

COMMIT TRANSACTION

# Transactions: ACID properties

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UPDATE branch
SET cash=cash+10000.00
WHERE sortcode=34
```

COMMIT TRANSACTION

Note that if total cash is £137,246.12 before the transaction, then it will be the same after the transaction.

## Example Data

branch		
<u>sortcode</u>	bname	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

movement			
<u>mid</u>	no	amount	tdate
1000	100	2300.00	5/1/1999
1001	101	4000.00	5/1/1999
1002	100	-223.45	8/1/1999
1004	107	-100.00	11/1/1999
1005	103	145.50	12/1/1999
1006	100	10.23	15/1/1999
1007	107	345.56	15/1/1999
1008	101	1230.00	15/1/1999
1009	119	5600.00	18/1/1999

account				
<u>no</u>	type	cname	rate?	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

key branch(sortcode)

key branch(bname)

key movement(mid)

key account(no)

movement(no)  $\xRightarrow{fk}$  account(no)

account(sortcode)  $\xRightarrow{fk}$  branch(sortcode)

## Transaction Properties: Atomicity

```
BEGIN TRANSACTION
```

```
UPDATE branch
```

```
SET cash=cash -10000.00
```

```
WHERE sortcode=56
```

**CRASH**

Suppose that the system crashes half way through processing a cash transfer, and the first part of the transfer has been written to disc

- The database on disc is left in an inconsistent state, with £10,000 ‘missing’
- A DBMS implementing **Atomicity** of transactions would on restart **UNDO** the change to branch 56

## Transaction Properties: Consistency

```
BEGIN TRANSACTION
  DELETE FROM branch
  WHERE sortcode=56

  INSERT INTO account
  VALUES (100, 'Smith, J', 'deposit', 5.00, 34)
END TRANSACTION
```

Suppose that a user deletes branch with sortcode 56, and inserts a deposit account number 100 for John Smith at branch sortcode 34

- The database is left in an inconsistent state for two reasons
  - it has three accounts recorded for a branch that appears not to exist, and
  - it has two records for account number 100, with different details for the account
- A DBMS implementing **Consistency** of transactions would forbid both of these changes to the database



## Transaction Properties: Isolation

BEGIN TRANSACTION

```
UPDATE branch
SET    cash=cash-10000.00
WHERE sortcode=56
```

BEGIN TRANSACTION

```
SELECT SUM(cash) AS net_cash
FROM   branch
```

```
UPDATE branch
SET    cash=cash+10000.00
WHERE sortcode=34
```

END TRANSACTION

END TRANSACTION

Suppose that the system sums the cash in the bank in one transaction, half way through processing a cash transfer in another transaction

- The result of the summation of cash in the bank erroneously reports that £10,000 is missing
- A DBMS implementing **Isolation** of transactions ensures that transactions always report results based on the values of committed transactions

## Transaction Properties: Durability

```
BEGIN TRANSACTION
```

```
  UPDATE branch
```

```
  SET    cash=cash -10000.00
```

```
  WHERE sortcode=56
```

```
  UPDATE branch
```

```
  SET    cash=cash +10000.00
```

```
  WHERE sortcode=34
```

```
END TRANSACTION
```

**CRASH**

Suppose that the system crashes after informing the user that it has committed the transfer of cash, but has not yet written to disc the update to branch 34

- The database on disc is left in an inconsistent state, with £10,000 ‘missing’
- A DBMS implementing **Durability** of transactions would on restart complete the change to branch 34 (or alternatively never inform a user of commitment with writing the results to disc).

## SQL Conversion to Histories

branch		
<u>sortcode</u>	bname	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

```

BEGIN TRANSACTION T1
  UPDATE branch
  SET   cash=cash-10000.00
  WHERE sortcode=56

  UPDATE branch
  SET   cash=cash+10000.00
  WHERE sortcode=34
COMMIT TRANSACTION T1

```



$H_1 = r_1[b_{56}], \text{cash}=94340.45,$   
 $w_1[b_{56}], \text{cash}=84340.45,$   
 $r_1[b_{34}], \text{cash}=8900.67,$   
 $w_1[b_{34}], \text{cash}=18900.67, c_1$

history of transaction  $T_n$ 

- 1 Begin transaction  $b_n$  (only given if necessary for discussion)
- 2 Various read operations on objects  $r_n[o_j]$  and write operations  $w_n[o_j]$
- 3 Either  $c_n$  for the commitment of the transaction, or  $a_n$  for the abort of the transaction

## SQL Conversion to Histories

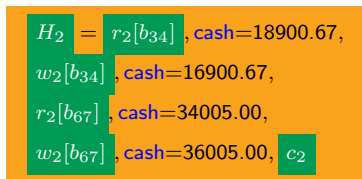
branch		
<u>sortcode</u>	bname	cash
56	'Wimbledon'	84340.45
34	'Goodge St'	18900.67
67	'Strand'	34005.00

```

BEGIN TRANSACTION
  UPDATE branch
  SET   cash=cash -2000.00
  WHERE sortcode=34

  UPDATE branch
  SET   cash=cash +2000.00
  WHERE sortcode=67
COMMIT TRANSACTION

```

history of transaction  $T_n$ 

- Same pattern of transaction code gives same pattern of operations

# Serial Execution

## Serial Execution of Transactions

- Executing one transaction at a time
- Provided updates are recorded in stable storage at the time of  $c_i$ , must maintain the ACID properties

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## Possible Serial Executions

$H_1$	=	$r_1[b_{56}]$	,	$w_1[b_{56}]$	,	$r_1[b_{34}]$	,	$w_1[b_{34}]$	,	$c_1$
$H_2$	=	$r_2[b_{34}]$	,	$w_2[b_{34}]$	,	$r_2[b_{67}]$	,	$w_2[b_{67}]$	,	$c_2$

# Serial Execution

## Serial Execution of Transactions

- Executing one transaction at a time
- Provided updates are recorded in stable storage at the time of  $c_i$ , must maintain the ACID properties

## Possible Serial Executions

$$H_1 = r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1$$

$$H_2 = r_2[b_{34}], w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2$$

The only two possible serial executions are

$$H_{s12} = r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, r_2[b_{34}], w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2$$

$$H_{s21} = r_2[b_{34}], w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2, r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1$$

# Concurrent Execution

## Concurrent Execution of Transactions

- Interleaving of several transaction histories
- Order of operations within each history preserved



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## Concurrent Execution of Transactions

- Interleaving of several transaction histories
- Order of operations within each history preserved

$$\begin{array}{l} H_1 = r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1 \\ H_2 = r_2[b_{34}], w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2 \end{array}$$

# Concurrent Execution

## Concurrent Execution of Transactions

- Interleaving of several transaction histories
- Order of operations within each history preserved

$$\begin{array}{l}
 H_1 = r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1 \\
 H_2 = r_2[b_{34}], w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2
 \end{array}$$

Some possible concurrent executions are

$$\begin{array}{l}
 H_x = r_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2 \\
 H_y = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2, c_1 \\
 H_z = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, r_2[b_{67}], w_2[b_{67}], c_2
 \end{array}$$

# Which concurrent executions should be allowed?

Concurrency control → controlling interaction

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### serialisability

A concurrent execution of transactions should always have the same final result as some serial execution of those same transactions

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### serialisability

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### recoverability

No transaction commits depending on data that has been produced by another transaction that has yet to commit

# Which concurrent executions should be allowed?

Concurrency control → controlling interaction

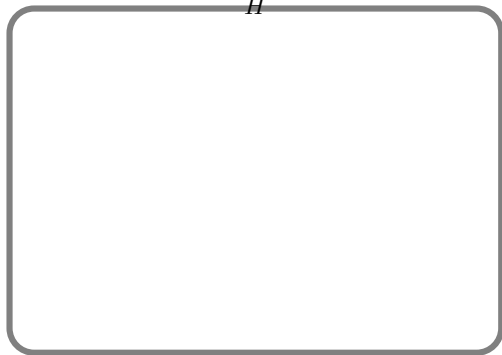
## serialisability

A concurrent execution of transactions should always have the same final result as some serial execution of those same transactions

## recoverability

No transaction commits depending on data that has been produced by another transaction that has yet to commit

$H$



$H$  set of all possible histories

# Which concurrent executions should be allowed?

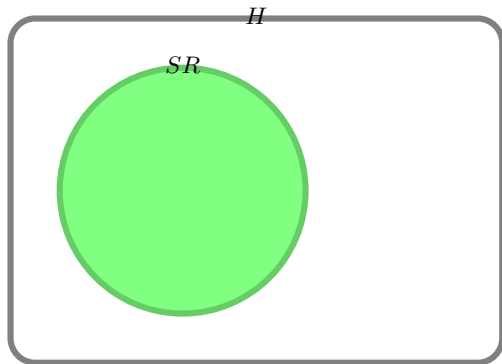
Concurrency control → controlling interaction

## serialisability

A concurrent execution of transactions should always have the same final result as some serial execution of those same transactions

## recoverability

No transaction commits depending on data that has been produced by another transaction that has yet to commit



$H$  set of all possible histories

$SR$  set of serialisable histories

# Which concurrent executions should be allowed?

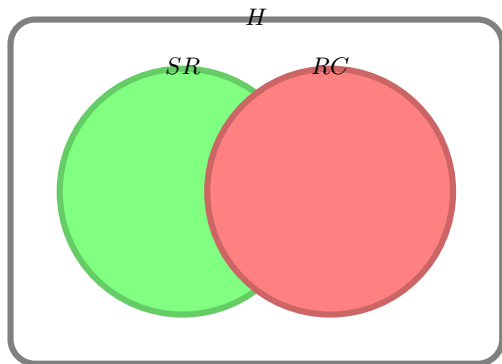
Concurrency control → controlling interaction

## serialisability

A concurrent execution of transactions should always have the same final result as some serial execution of those same transactions

## recoverability

No transaction commits depending on data that has been produced by another transaction that has yet to commit



$H$  set of all possible histories  
 $SR$  set of serialisable histories  
 $RC$  set of recoverable histories



## Quiz 21.1: Serialisability and Recoverability (1)

$$H_x = r_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2$$

Is  $H_x$

A

Not Serialisable, Not Recoverable

B

Not Serialisable, Recoverable

C

Serialisable, Not Recoverable

D

Serialisable, Recoverable

## Quiz 21.2: Serialisability and Recoverability (2)

$$H_y = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2, c_1$$

Is  $H_y$

A

Not Serialisable, Not Recoverable

B

Not Serialisable, Recoverable

C

Serialisable, Not Recoverable

D

Serialisable, Recoverable

## Quiz 21.3: Serialisability and Recoverability (3)

$$H_z = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, r_2[b_{67}], w_2[b_{67}], c_2$$

Is  $H_z$

A

Not Serialisable, Not Recoverable

B

Not Serialisable, Recoverable

C

Serialisable, Not Recoverable

D

Serialisable, Recoverable

## Topic 22: Anomalies in Transaction Execution

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## Anomaly 1: Lost Update

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1

BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$

$r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$



$r_1[b_{56}]$ , cash=94340.45,  $w_1[b_{56}]$ , cash=84340.45,  $r_1[b_{34}]$ , cash=8900.67,  
 $r_2[b_{34}]$ , cash=8900.67,  $w_1[b_{34}]$ , cash=18900.67,  $c_1$ ,  $w_2[b_{34}]$ , cash=6900.67,  
 $r_2[b_{67}]$ , cash=34005.00,  $w_2[b_{67}]$ , cash=36005.25,  $c_2$

## Anomaly 1: Lost Update

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1

BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$

$r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$



$r_1[b_{56}]$ , cash=94340.45,  $w_1[b_{56}]$ , cash=84340.45,  $r_1[b_{34}]$ , cash=8900.67,  
 $r_2[b_{34}]$ , cash=8900.67, **lost update**,  $c_1$ ,  $w_2[b_{34}]$ , cash=6900.67,  
 $r_2[b_{67}]$ , cash=34005.00,  $w_2[b_{67}]$ , cash=36005.25,  $c_2$

- serialisable

+ recoverable

$LU$  = set of histories with a lost update  
 $SR \cap LU = \emptyset$

## Anomaly 2: Inconsistent analysis

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1



$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$



$r_1[b_{56}]$ ,  $cash=94340.45$ ,  $w_1[b_{56}]$ ,  $cash=84340.45$ ,  $r_4[b_{56}]$ ,  $cash=84340.45$ ,  
 $r_4[b_{34}]$ ,  $cash=8900.67$ ,  $r_4[b_{67}]$ ,  $cash=34005.00$ ,  $r_1[b_{34}]$ ,  $cash=8900.67$ ,  
 $w_1[b_{34}]$ ,  $cash=18900.67$ ,  $c_1$ ,  $c_4$

BEGIN TRANSACTION T4  
 SELECT SUM(cash) FROM branch  
 COMMIT TRANSACTION T4



$H_4 = r_4[b_{56}]$ ,  $r_4[b_{34}]$ ,  $r_4[b_{67}]$ ,  $c_4$



– serialisable

+ recoverable

$IA$  = set of histories with an inconsistent analysis  
 $SR \cap IA = \emptyset$

## Anomaly 3: Dirty Reads

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1

BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2

$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$

$r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$

$r_1[b_{56}]$ , cash=94340.45,  $w_1[b_{56}]$ , cash=84340.45,  $r_2[b_{34}]$ , cash=8900.67,  
 $w_2[b_{34}]$ , cash=6900.67,  $r_1[b_{34}]$ , cash=6900.67,  $w_1[b_{34}]$ , cash=16900.67,  $c_1$ ,  
 $r_2[b_{67}]$ , cash=34005.00,  $w_2[b_{67}]$ , cash=36005.25,  $a_2$

+ serialisable

- recoverable

$DR$  = set of histories with a dirty read  
 $RC \cap DR \neq \emptyset$



## Quiz 22.1: Anomalies (1)

$$H_x = r_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2$$

Which anomaly does  $H_x$  suffer?

A

None

B

Lost Update

C

Inconsistent Analysis

D

Dirty Read

## Quiz 22.2: Anomalies (2)

$$H_y = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2, c_1$$

Which anomaly does  $H_y$  suffer?

A

None

B

Lost Update

C

Inconsistent Analysis

D

Dirty Read

## Quiz 22.3: Anomalies (3)

$$H_z = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, r_2[b_{67}], w_2[b_{67}], c_2$$

Which anomaly does  $H_z$  suffer?

A

None

B

Lost Update

C

Inconsistent Analysis

D

Dirty Read

## Account Table

account				
<u>no</u>	type	cname	rate?	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

## Anomaly 3: Dirty Reads (Recoverable Example)

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1



$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$



$r_1[b_{56}]$ , cash=94340.45,  $w_1[b_{56}]$ , cash=84340.45,  $r_2[b_{34}]$ , cash=8900.67,  
 $w_2[b_{34}]$ , cash=6900.67,  $r_1[b_{34}]$ , cash=6900.67,  $w_1[b_{34}]$ , cash=16900.67,  
 $r_2[b_{67}]$ , cash=34005.00,  $w_2[b_{67}]$ , cash=36005.25,  $c_2$ ,  $c_1$

BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



$r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$



## Anomaly 3: Dirty Reads (Recoverable Example)

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1



$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$



$r_1[b_{56}]$ , cash=94340.45,  $w_1[b_{56}]$ , cash=84340.45,  $r_2[b_{34}]$ , cash=8900.67,  
 $w_2[b_{34}]$ , cash=6900.67,  $r_1[b_{34}]$ , cash=6900.67,  $w_1[b_{34}]$ , cash=16900.67,  
 $r_2[b_{67}]$ , cash=34005.00,  $w_2[b_{67}]$ , cash=36005.25,  $c_2$ ,  $c_1$

BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



$r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$



+ serialisable

+ recoverable

$DR$  = set of histories with a dirty read  
 $RC \cap DR \neq \emptyset \wedge RC \cup DR = H$

## Anomaly 4: Dirty Writes

```

BEGIN TRANSACTION T5
UPDATE account
SET rate=5.5
WHERE type='deposit'
COMMIT TRANSACTION T5
  
```



$H_5 = w_5[a_{101}], \text{rate}=5.5,$   
 $w_5[a_{119}], \text{rate}=5.5, c_5$



$w_6[a_{101}], \text{rate}=6.0, w_5[a_{101}], \text{rate}=5.5, w_5[a_{119}], \text{rate}=5.5,$   
 $w_6[a_{119}], \text{rate}=6.0, c_5, c_6$

```

BEGIN TRANSACTION T6
UPDATE account
SET rate=6.0
WHERE type='deposit'
COMMIT TRANSACTION T6
  
```



$H_6 = w_6[a_{101}], \text{rate}=6.0,$   
 $w_6[a_{119}], \text{rate}=6.0, c_6$



$w_6[a_{101}], \text{rate}=6.0, w_5[a_{101}], \text{rate}=5.5, w_5[a_{119}], \text{rate}=5.5,$   
 $w_6[a_{119}], \text{rate}=6.0, c_5, c_6$

## Anomaly 4: Dirty Writes

BEGIN TRANSACTION T5  
 UPDATE account  
 SET rate=5.5  
 WHERE type='deposit'  
 COMMIT TRANSACTION T5



$H_5 = w_5[a_{101}], \text{rate}=5.5,$   
 $w_5[a_{119}], \text{rate}=5.5, c_5$



$w_6[a_{101}], \text{rate}=6.0, w_5[a_{101}], \text{rate}=5.5, w_5[a_{119}], \text{rate}=5.5,$   
 $w_6[a_{119}], \text{rate}=6.0, c_5, c_6$

BEGIN TRANSACTION T6  
 UPDATE account  
 SET rate=6.0  
 WHERE type='deposit'  
 COMMIT TRANSACTION T6



$H_6 = w_6[a_{101}], \text{rate}=6.0,$   
 $w_6[a_{119}], \text{rate}=6.0, c_6$



- serialisable

+ recoverable

$WR = \text{set of histories with a dirty write}$   
 $SR \cap WR \neq \emptyset$



# Patterns of operations associated with Anomalies

Anomaly	Set	Pattern	Problem
Dirty Write	$DW$	$w_1[o] \prec w_2[o] \prec e_1$	Sometimes not $SR$
Dirty Read	$DR$	$w_1[o] \prec r_2[o] \prec e_1$	Sometimes not $RC$
Inconsistent Analysis	$IA$	$r_1[o_a] \prec w_2[o_a], w_2[o_b] \prec r_1[o_b]$	Not $SR$
Lost Update	$LU$	$r_1[o] \prec w_2[o] \prec w_1[o]$	Not $SR$

## Notation

- $e_i$  means either  $c_i$  or  $a_i$  occurring
- $op_a \prec op_b$  mean  $op_a$  occurs before  $op_b$  in a history

## Worksheet: Anomalies

rental\_charge

$$H_1 = r_1[d_{1000}], w_1[d_{1000}], r_1[d_{1001}], w_1[d_{1001}], r_1[d_{1002}], w_1[d_{1002}]$$

transfer\_charge

$$H_2 = r_2[d_{1000}], w_2[d_{1000}], r_2[d_{1002}], w_2[d_{1002}]$$

total\_charge

$$H_3 = r_3[d_{1000}], r_3[d_{1001}], r_3[d_{1002}]$$

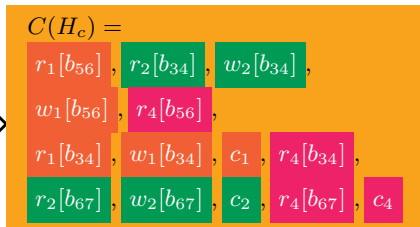
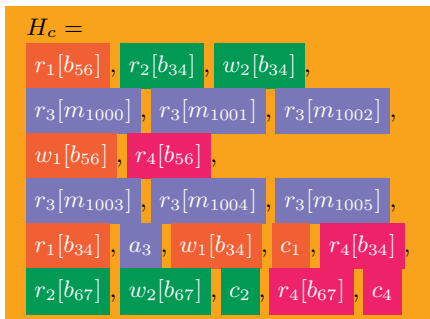
## Topic 23: Serialisable Execution

P.J. McBrien

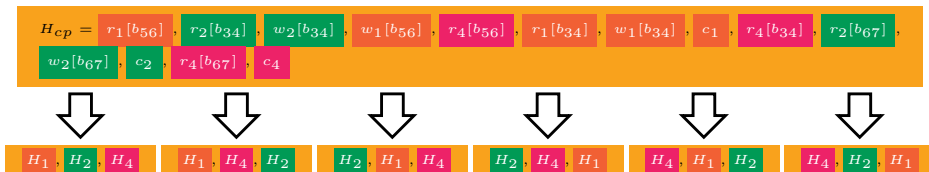
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## Serialisable Transaction Execution

- Solve anomalies  $\rightarrow H \equiv$  serial execution
- Only interested in the **committed projection**



## Possible Serial Equivalents



- how to determine that histories are equivalent?
- how to check this during execution?

## Conflicts: Potential For Problems

## conflict

A **conflict** occurs when there is an interaction between two transactions

- $r_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$   
or
- $w_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$

*Only consider pairs where there is no third operation  $rw_z[o]$  between the pair of operations that conflicts with both*

## conflicts

$H_x =$	$r_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$w_2[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$
$H_y =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$	$c_1$
$H_z =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$

Conflicts

## Conflicts: Potential For Problems

## conflict

A **conflict** occurs when there is an interaction between two transactions

- $r_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$   
or
- $w_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$

*Only consider pairs where there is no third operation  $rw_z[o]$  between the pair of operations that conflicts with both*

## conflicts

$H_x =$	$r_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$w_2[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$
$H_y =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$	$c_1$
$H_z =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$

## Conflicts

- $w_2[b_{34}] \rightarrow r_1[b_{34}]$  T1 reads from T2 in  $H_y, H_z$

## Conflicts: Potential For Problems

## conflict

A **conflict** occurs when there is an interaction between two transactions

- $r_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$   
or
- $w_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$

*Only consider pairs where there is no third operation  $rw_z[o]$  between the pair of operations that conflicts with both*

## conflicts

$H_x =$	$r_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$w_2[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$
$H_y =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$	$c_1$
$H_z =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$

## Conflicts

- $w_2[b_{34}] \rightarrow r_1[b_{34}]$  T1 reads from T2 in  $H_y, H_z$
- $w_1[b_{34}] \rightarrow w_2[b_{34}]$  T2 writes over T1 in  $H_x$



## Conflicts: Potential For Problems

## conflict

A **conflict** occurs when there is an interaction between two transactions

- $r_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$   
or
- $w_x[o]$  and  $w_y[o]$  are in  $H$  where  $x \neq y$

*Only consider pairs where there is no third operation  $rw_z[o]$  between the pair of operations that conflicts with both*

## conflicts

$H_x =$	$r_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$w_2[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$
$H_y =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$	$c_1$
$H_z =$	$r_2[b_{34}]$	$w_2[b_{34}]$	$r_1[b_{56}]$	$w_1[b_{56}]$	$r_1[b_{34}]$	$w_1[b_{34}]$	$c_1$	$r_2[b_{67}]$	$w_2[b_{67}]$	$c_2$

## Conflicts

- $w_2[b_{34}] \rightarrow r_1[b_{34}]$  T1 reads from T2 in  $H_y, H_z$
- $w_1[b_{34}] \rightarrow w_2[b_{34}]$  T2 writes over T1 in  $H_x$
- $r_2[b_{34}] \rightarrow w_1[b_{34}]$  T1 writes after T2 reads in  $H_x$

## Quiz 23.1: Conflicts

 $H_w =$ 
 $r_2[a_{100}], w_2[a_{100}], r_2[a_{107}], r_1[a_{119}], w_1[a_{119}], r_1[a_{107}], w_1[a_{107}], c_1, w_2[a_{107}], c_2$ 

Which of the following is not a conflict in  $H_w$ ?

A

 $r_2[a_{107}] \rightarrow r_1[a_{107}]$ 

B

 $r_2[a_{107}] \rightarrow w_1[a_{107}]$ 

C

 $r_1[a_{107}] \rightarrow w_2[a_{107}]$ 

D

 $w_1[a_{107}] \rightarrow w_2[a_{107}]$

# Conflict Equivalence and Conflict Serialisable

## Conflict Equivalence

Two histories  $H_i$  and  $H_j$  are **conflict equivalent** if:

- 1 Contain the same set of operations
- 2 Order conflicts (of non-aborted transactions) in the same way.

## Conflict Serialisable

a history  $H$  is **conflict serialisable (CSR)** if  $C(H) \equiv_{CE}$  a serial history

## Failure to be conflict serialisable

$H_x =$   $r_2[b_{34}]$ ,  $r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$

Contains conflicts  $r_2[b_{34}]$   $\rightarrow$   $w_1[b_{34}]$  and  $w_1[b_{34}]$   $\rightarrow$   $w_2[b_{34}]$  and so is not conflict equivalent to  $H_1, H_2$  nor  $H_2, H_1$ , and hence is not conflict serialisable.

# Serialisation Graph

## Serialisation Graph

A **serialisation graph**  $SG(H)$  contains a node for each transaction in  $H$ , and an edge  $T_i \rightarrow T_j$  if there is some object  $o$  for which a conflict  $rw_i[o] \rightarrow rw_j[o]$  exists in  $H$ . If  $SG(H)$  is acyclic, then  $H$  is conflict serialisable.

## Demonstrating that a History is CSR

Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

# Serialisation Graph

## Serialisation Graph

A **serialisation graph**  $SG(H)$  contains a node for each transaction in  $H$ , and an edge  $T_i \rightarrow T_j$  if there is some object  $o$  for which a conflict  $rw_i[o] \rightarrow rw_j[o]$  exists in  $H$ . If  $SG(H)$  is acyclic, then  $H$  is conflict serialisable.

## Demonstrating that a History is CSR

Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}]$   $\rightarrow$   $r_1[b_{34}]$ ,

$SG(H_{cp})$

# Serialisation Graph

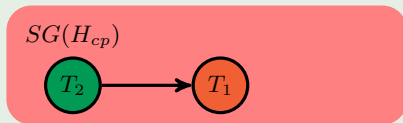
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Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}]$   $\rightarrow$   $r_1[b_{34}]$ ,



# Serialisation Graph

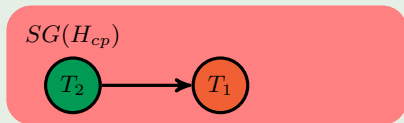
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## Demonstrating that a History is CSR

Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}]$   $\rightarrow$   $r_1[b_{34}]$ ,  $w_1[b_{56}]$   $\rightarrow$   $r_4[b_{56}]$ ,



# Serialisation Graph

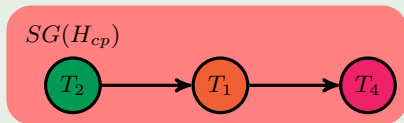
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A **serialisation graph**  $SG(H)$  contains a node for each transaction in  $H$ , and an edge  $T_i \rightarrow T_j$  if there is some object  $o$  for which a conflict  $rw_i[o] \rightarrow rw_j[o]$  exists in  $H$ . If  $SG(H)$  is acyclic, then  $H$  is conflict serialisable.

## Demonstrating that a History is CSR

Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}]$   $\rightarrow$   $r_1[b_{34}]$ ,  $w_1[b_{56}]$   $\rightarrow$   $r_4[b_{56}]$ ,





# Serialisation Graph

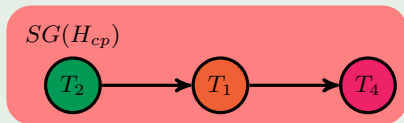
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Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}]$   $\rightarrow$   $r_1[b_{34}]$ ,  $w_1[b_{56}]$   $\rightarrow$   $r_4[b_{56}]$ ,  $w_1[b_{34}]$   $\rightarrow$   $r_4[b_{34}]$ ,



# Serialisation Graph

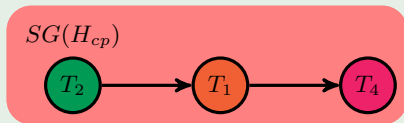
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A **serialisation graph**  $SG(H)$  contains a node for each transaction in  $H$ , and an edge  $T_i \rightarrow T_j$  if there is some object  $o$  for which a conflict  $rw_i[o] \rightarrow rw_j[o]$  exists in  $H$ . If  $SG(H)$  is acyclic, then  $H$  is conflict serialisable.

## Demonstrating that a History is CSR

Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}] \rightarrow r_1[b_{34}]$ ,  $w_1[b_{56}] \rightarrow r_4[b_{56}]$ ,  $w_1[b_{34}] \rightarrow r_4[b_{34}]$ ,  
 $w_2[b_{67}] \rightarrow r_4[b_{67}]$



## Serialisation Graph

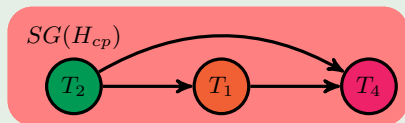
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## Demonstrating that a History is CSR

Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}] \rightarrow r_1[b_{34}]$ ,  $w_1[b_{56}] \rightarrow r_4[b_{56}]$ ,  $w_1[b_{34}] \rightarrow r_4[b_{34}]$ ,  
 $w_2[b_{67}] \rightarrow r_4[b_{67}]$



# Serialisation Graph

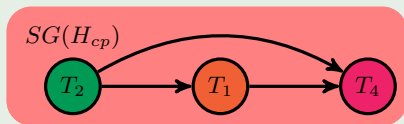
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A **serialisation graph**  $SG(H)$  contains a node for each transaction in  $H$ , and an edge  $T_i \rightarrow T_j$  if there is some object  $o$  for which a conflict  $rw_i[o] \rightarrow rw_j[o]$  exists in  $H$ . If  $SG(H)$  is acyclic, then  $H$  is conflict serialisable.

## Demonstrating that a History is CSR

Given  $H_{cp} =$   $r_1[b_{56}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $w_1[b_{56}]$ ,  $r_4[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  
 $c_1$ ,  $r_4[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $r_4[b_{67}]$ ,  $c_4$

Conflicts are  $w_2[b_{34}] \rightarrow r_1[b_{34}]$ ,  $w_1[b_{56}] \rightarrow r_4[b_{56}]$ ,  $w_1[b_{34}] \rightarrow r_4[b_{34}]$ ,  
 $w_2[b_{67}] \rightarrow r_4[b_{67}]$



$SG(H_{cp})$  is acyclic, therefore  $H_{cp}$  is CSR. Serialisation order  $T_2, T_1, T_4$

## Worksheet: Serialisability

$$H_1 = r_1[o_1], w_1[o_1], w_1[o_2], w_1[o_3], c_1$$

$$H_2 = r_2[o_2], w_2[o_2], w_2[o_1], c_2$$

$$H_3 = r_3[o_1], w_3[o_1], w_3[o_2], c_3$$

$$H = r_1[o_1], w_1[o_1], r_2[o_2], w_2[o_2], w_2[o_1], c_2, w_1[o_2], r_3[o_1], w_3[o_1], w_3[o_2], c_3, w_1[o_3], c_1$$

# Review of Serialisable Histories

RC



RC recoverable

SR serialisable

SR

# Review of Serialisable Histories

RC



RC recoverable

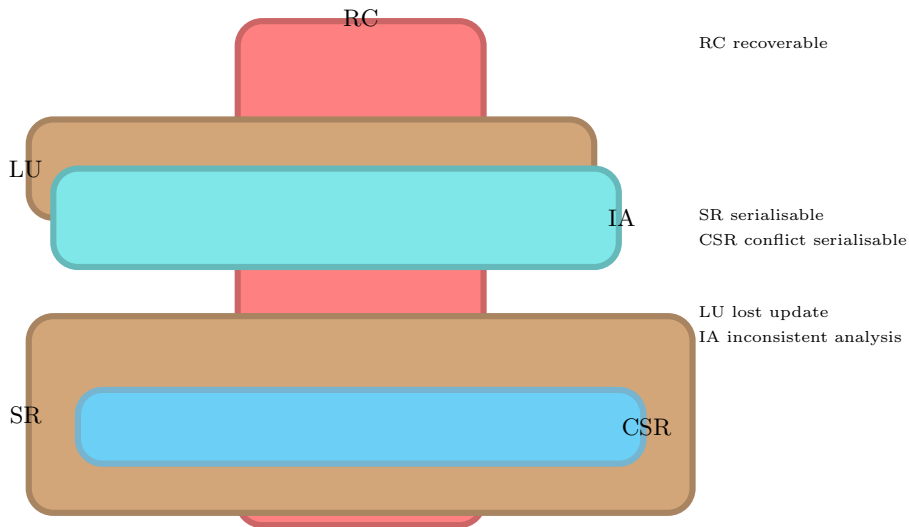
SR serialisable

CSR conflict serialisable

SR

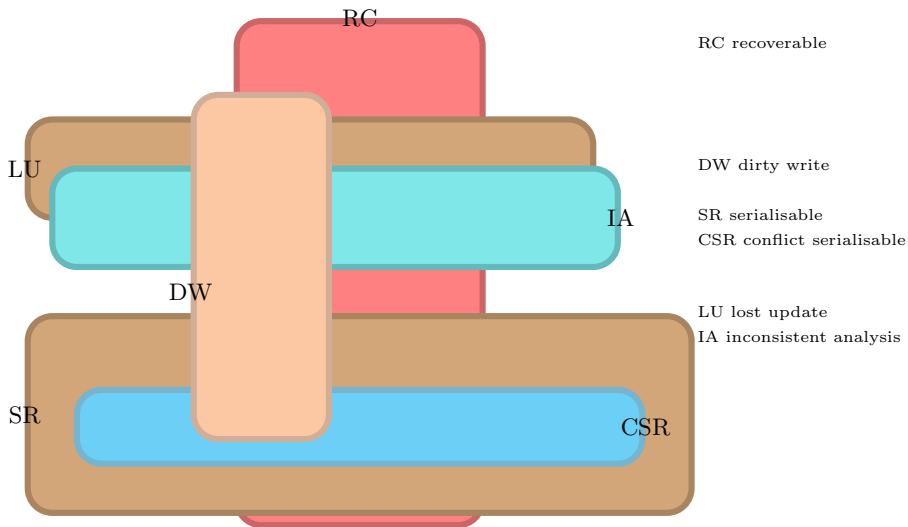
CSR

## Review of Serialisable Histories





## Review of Serialisable Histories



## Topic 24: Recoverable Execution

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# Recoverability

- Serialisability necessary for isolation and consistency of committed transactions
- Recoverability necessary for isolation and consistency when there are also aborted transactions

## Recoverable execution

A **recoverable (RC)** history  $H$  has no transaction committing before another transaction from which it read

## Execution avoiding cascading aborts

A history which **avoids cascading aborts (ACA)** does not read from a non-committed transaction

## Strict execution

A **strict (ST)** history does not read from a non-committed transaction nor write over a non-committed transaction

$$ST \subset ACA \subset RC$$

## Non-recoverable executions

```

BEGIN TRANSACTION T1
UPDATE branch
SET cash=cash-10000.00
WHERE sortcode=56
UPDATE branch
SET cash=cash+10000.00
WHERE sortcode=34
COMMIT TRANSACTION T1
  
```

```

BEGIN TRANSACTION T4
SELECT SUM(cash) FROM branch
COMMIT TRANSACTION T4
  
```


 $H_1 = r_1[b_{56}], w_1[b_{56}], a_1$ 
 $H_4 = r_4[b_{56}], r_4[b_{34}], r_4[b_{67}], c_4$ 

 $H_c = r_1[b_{56}], \text{cash}=94340.45, w_1[b_{56}], \text{cash}=84340.45, r_4[b_{56}], \text{cash}=84340.45, r_4[b_{34}], \text{cash}=8900.67, r_4[b_{67}], \text{cash}=34005.00, c_4, a_1$ 
 $H_c \notin RC$

## Cascading Aborts

```

BEGIN TRANSACTION T1
UPDATE branch
SET cash=cash-10000.00
WHERE sortcode=56
UPDATE branch
SET cash=cash+10000.00
WHERE sortcode=34
COMMIT TRANSACTION T1
  
```

```

BEGIN TRANSACTION T4
SELECT SUM(cash) FROM branch
COMMIT TRANSACTION T4
  
```


 $H_1 = r_1[b_{56}], w_1[b_{56}], a_1$ 
 $H_4 = r_4[b_{56}], r_4[b_{34}], r_4[b_{67}], c_4$ 

 $H_c = r_1[b_{56}], \text{cash}=94340.45, w_1[b_{56}], \text{cash}=84340.45, r_4[b_{56}], \text{cash}=84340.45, r_4[b_{34}], \text{cash}=8900.67, r_4[b_{67}], \text{cash}=34005.00, a_1, a_4$ 
 $H_c \in RC$   
 $H_c \notin ACA$

## Strict Execution

```

BEGIN TRANSACTION T5
UPDATE account
SET rate=5.5
WHERE type='deposit'
COMMIT TRANSACTION T5
  
```



$H_5 = w_5[a_{101}], \text{rate}=5.5,$   
 $w_5[a_{119}], \text{rate}=5.5, a_5$



$H_c = w_6[a_{101}], \text{rate}=6.0, w_5[a_{101}], \text{rate}=5.5,$   
 $w_5[a_{119}], \text{rate}=5.5, w_6[a_{119}], \text{rate}=6.0, a_5, c_6$

```

BEGIN TRANSACTION T6
UPDATE account
SET rate=6.0
WHERE type='deposit'
COMMIT TRANSACTION T6
  
```



$H_6 = w_6[a_{101}], \text{rate}=6.0,$   
 $w_6[a_{119}], \text{rate}=6.0, c_6$



$H_c \in ACA$   
 $H_c \notin ST$

## Quiz 24.1: Recoverability (1)

$$H_x = r_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2$$

Which describes the recoverability of  $H_x$ ?

A

Non-recoverable

B

Recoverable

C

Avoids Cascading Aborts

D

Strict

## Quiz 24.2: Recoverability (2)

$$H_y = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2, c_1$$

Which describes the recoverability of  $H_y$ ?

A

Non-recoverable

B

Recoverable

C

Avoids Cascading Aborts

D

Strict



## Quiz 24.3: Recoverability (3)

$$H_z = r_2[b_{34}], w_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], c_1, r_2[b_{67}], w_2[b_{67}], c_2$$

Which describes the recoverability of  $H_z$ ?

**A**  
Non-recoverable

**B**  
Recoverable

**C**  
Avoids Cascading Aborts

**D**  
Strict

## Quiz 24.4: Recoverability (4)

$$H_w = r_2[b_{34}], r_1[b_{56}], w_1[b_{56}], r_1[b_{34}], w_1[b_{34}], w_2[b_{34}], r_2[b_{67}], w_2[b_{67}], c_2, c_1$$

Which describes the recoverability of  $H_w$ ?

A

Non-recoverable

B

Recoverable

C

Avoids Cascading Aborts

D

Strict

## Worksheet: Recoverability

$$H_w = r_2[o_1], r_2[o_2], w_2[o_2], r_1[o_2], w_2[o_1], r_2[o_3], c_2, c_1$$

$$H_x = r_2[o_1], r_2[o_2], w_2[o_1], w_2[o_2], w_1[o_1], w_1[o_2], c_1, r_2[o_3], c_2$$

$$H_y = r_2[o_1], r_2[o_2], w_2[o_2], r_1[o_2], w_2[o_1], c_1, r_2[o_3], c_2$$

$$H_z = r_2[o_1], w_1[o_1], r_2[o_2], w_2[o_2], r_2[o_3], c_2, r_1[o_2], w_1[o_2], w_1[o_3], c_1$$

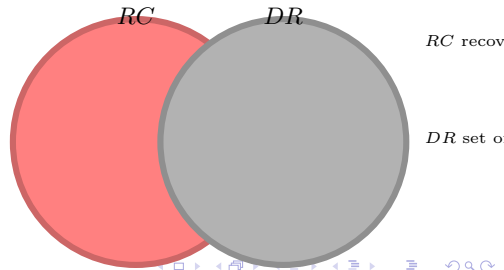
## Review of Recoverable Histories

Non-recoverable  $\rightarrow$  Dirty Read

For a history to be non-recoverable, it must contain a dirty read  $DR$

Thus  $H = RC \cup DR$

However, a dirty read does not imply a history is non-recoverable



## Review of Recoverable Histories

### Non-recoverable $\rightarrow$ Dirty Read

For a history to be non-recoverable, it must contain a dirty read  $DR$

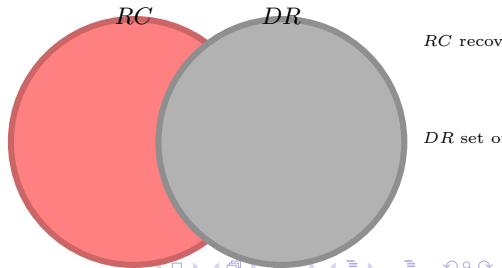
Thus  $H = RC \cup DR$

However, a dirty read does not imply a history is non-recoverable

### No Dirty Read $\rightarrow$ Recoverable

A history that contains no dirty read must be recoverable, and **avoids cascading aborts (ACA)** at the commit of a transaction.

Thus  $ACA = RC - DR$  and  $ACA \subset RC$



## Review of Recoverable Histories

### Non-recoverable $\rightarrow$ Dirty Read

For a history to be non-recoverable, it must contain a dirty read  $DR$

Thus  $H = RC \cup DR$

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A history that contains no dirty read must be recoverable, and **avoids cascading aborts (ACA)** at the commit of a transaction.

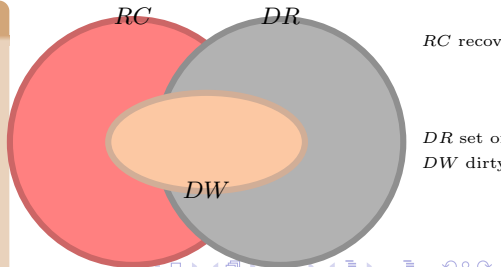
Thus  $ACA = RC - DR$  and  $ACA \subset RC$

### Dirty Write $\not\leftrightarrow$ Recoverable

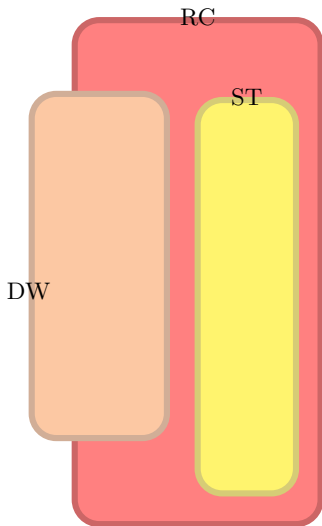
A dirty writes and recoverability do not imply anything about each other

However, dirty writes make executing recovery complex, and can lead to non-serialisable executions. A **strict (ST)** history has no dirty reads or dirty writes.

Thus  $ST = ACA - DW$  and  $ST \subset ACA$



## Review of Serialisable and Recoverable Histories

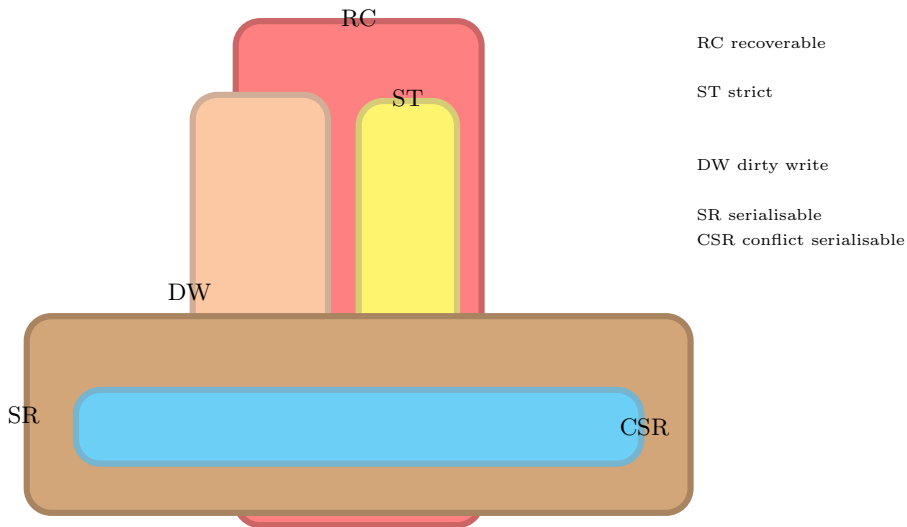


RC recoverable

ST strict

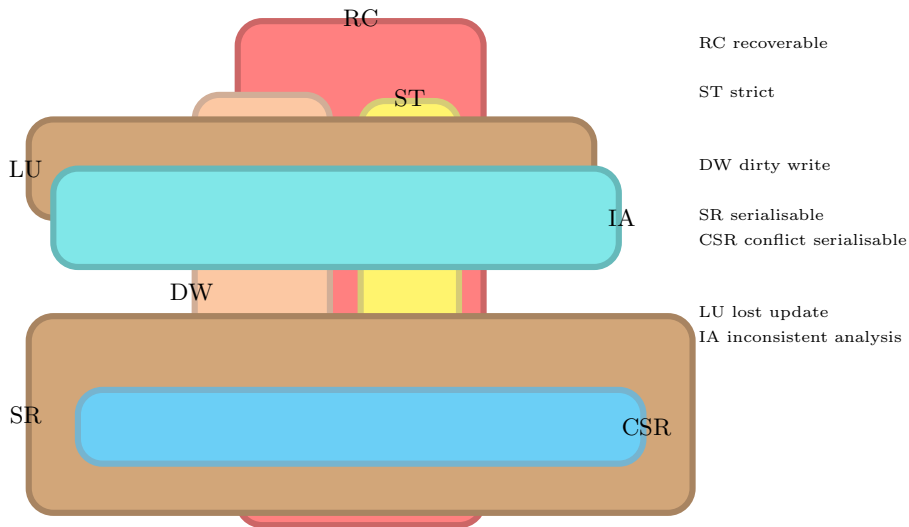
DW dirty write

## Review of Serialisable and Recoverable Histories





## Review of Serialisable and Recoverable Histories



# Topic 25: Concurrency Control

P.J. McBrien

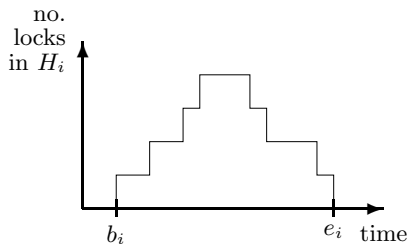
Imperial College London

# Maintaining Serialisability and Recoverability

- **two-phase locking (2PL)**
  - conflict based
  - uses **locks** to prevent problems
  - common technique
- **time-stamping**
  - add a timestamp to each object
  - write sets timestamp to that of transaction
  - may only read or write objects with earlier timestamp
  - abort when object has new timestamp
  - common technique
- **optimistic concurrency control**
  - do nothing until commit
  - at commit, inspect history for problems
  - good if few conflicts

# The 2PL Protocol

- 1 read locks  $rl[o], \dots, r[o], \dots, ru[o]$
- 2 write locks  $wl[o], \dots, w[o], \dots, wu[o]$
- 3 Two phases
  - i growing phase
  - ii shrinking phase
- 4 refuse  $rl_i[o]$  if  $wl_j[o]$  already held  
refuse  $wl_i[o]$  if  $rl_j[o]$  or  $wl_j[o]$  already held
- 5  $rl_i[o]$  or  $wl_i[o]$  refused  $\rightarrow$  delay  $T_i$



## Quiz 25.1: Two Phase Locking (2PL)

Which history is not valid in 2PL?

A

$rl_1[a_{107}]$ ,  $r_1[a_{107}]$ ,  $wl_1[a_{107}]$ ,  $w_1[a_{107}]$ ,  $wu_1[a_{107}]$ ,  $ru_1[a_{107}]$

B

$wl_1[a_{107}]$ ,  $wl_1[a_{100}]$ ,  $r_1[a_{107}]$ ,  $w_1[a_{107}]$ ,  $r_1[a_{100}]$ ,  $w_1[a_{100}]$ ,  $wu_1[a_{100}]$ ,  $wu_1[a_{107}]$

C

$wl_1[a_{107}]$ ,  $r_1[a_{107}]$ ,  $w_1[a_{107}]$ ,  $wu_1[a_{107}]$ ,  $wl_1[a_{100}]$ ,  $r_1[a_{100}]$ ,  $w_1[a_{100}]$ ,  $wu_1[a_{100}]$

D

$wl_1[a_{107}]$ ,  $r_1[a_{107}]$ ,  $w_1[a_{107}]$ ,  $wl_1[a_{100}]$ ,  $r_1[a_{100}]$ ,  $wu_1[a_{107}]$ ,  $w_1[a_{100}]$ ,  $wu_1[a_{100}]$

## Lost Update Anomaly

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1



$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$



$r_1[b_{56}]$ , cash=94340.45,  $w_1[b_{56}]$ , cash=84340.45,  $r_1[b_{34}]$ , cash=8900.67,  
 $r_2[b_{34}]$ , cash=8900.67,  $w_1[b_{34}]$ , cash=18900.67,  $c_1$ ,  $w_2[b_{34}]$ , cash=6900.67,  
 $r_2[b_{67}]$ , cash=34005.00,  $w_2[b_{67}]$ , cash=36005.25,  $c_2$

BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



$r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$



## Lost Update Anomaly

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1



$r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$



BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



$r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$



$r_1[b_{56}]$ , cash=94340.45,  $w_1[b_{56}]$ , cash=84340.45,  $r_1[b_{34}]$ , cash=8900.67,  
 $r_2[b_{34}]$ , cash=8900.67, **lost update**,  $c_1$ ,  $w_2[b_{34}]$ , cash=6900.67,  
 $r_2[b_{67}]$ , cash=34005.00,  $w_2[b_{67}]$ , cash=36005.25,  $c_2$

## Lost Update Anomaly with 2PL

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1



$b_1$ ,  $wl_1[b_{56}]$ ,  $r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $wl_1[b_{34}]$ ,  
 $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$ ,  $wu_1[b_{56}]$ ,  $wu_1[b_{34}]$



BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



$b_2$ ,  $wl_2[b_{34}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $wl_2[b_{67}]$ ,  
 $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $wu_2[b_{34}]$ ,  $wu_2[b_{67}]$



$b_1$ ,  $wl_1[b_{56}]$ ,  $r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $wl_1[b_{34}]$ ,  $r_1[b_{34}]$ ,  $b_2$ ,  $wl_2[b_{34}]$ ,  $r_2[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$ ,  
 $wu_1[b_{56}]$ ,  $wu_1[b_{34}]$ ,  $w_2[b_{34}]$ ,  $wl_2[b_{67}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $wu_2[b_{34}]$ ,  $wu_2[b_{67}]$

Lost Update history not permitted by 2PL, since  $wl_2[b_{34}]$  not granted



## Lost Update Anomaly with 2PL

BEGIN TRANSACTION T1  
 EXEC move\_cash(56,34,10000.00)  
 COMMIT TRANSACTION T1



$b_1$ ,  $wl_1[b_{56}]$ ,  $r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $wl_1[b_{34}]$ ,  
 $r_1[b_{34}]$ ,  $w_1[b_{34}]$ ,  $c_1$ ,  $wu_1[b_{56}]$ ,  $wu_1[b_{34}]$



BEGIN TRANSACTION T2  
 EXEC move\_cash(34,67,2000.00)  
 COMMIT TRANSACTION T2



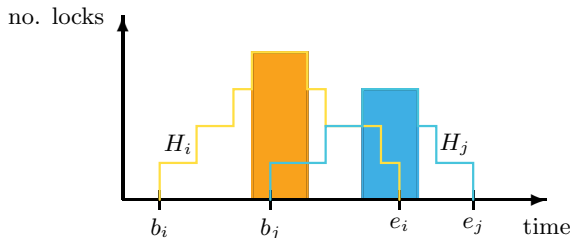
$b_2$ ,  $wl_2[b_{34}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $wl_2[b_{67}]$ ,  
 $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $wu_2[b_{34}]$ ,  $wu_2[b_{67}]$



$b_1$ ,  $wl_1[b_{56}]$ ,  $r_1[b_{56}]$ ,  $w_1[b_{56}]$ ,  $wl_1[b_{34}]$ ,  $r_1[b_{34}]$ ,  $b_2$ ,  $w_1[b_{34}]$ ,  $c_1$ ,  $wu_1[b_{56}]$ ,  $wu_1[b_{34}]$ ,  
 $wl_2[b_{34}]$ ,  $r_2[b_{34}]$ ,  $w_2[b_{34}]$ ,  $wl_2[b_{67}]$ ,  $r_2[b_{67}]$ ,  $w_2[b_{67}]$ ,  $c_2$ ,  $wu_2[b_{34}]$ ,  $wu_2[b_{67}]$

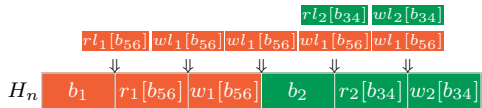
2PL causes T2 to be delayed

## Why does 2PL Work?



- two-phase rule  $\rightarrow$  maximum lock period
- can re-time history so all operations take place during maximum lock period
- CSR since *all* conflicts prevented during maximum lock period

## Deadlock Detection: WFG with No Cycle = No Deadlock

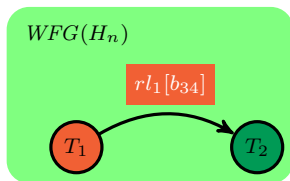
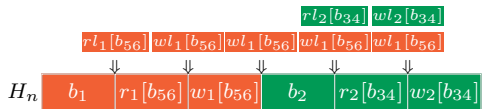


$WFG(H_n)$

$T_1$

$T_2$

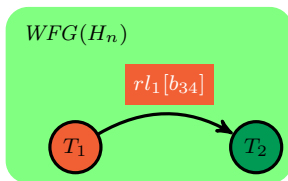
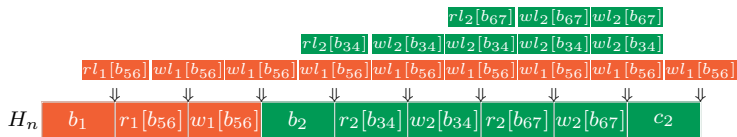
## Deadlock Detection: WFG with No Cycle = No Deadlock



$H_1$  attempts  $r_1[b_{34}]$ , but is refused since  $H_2$  has a write-lock, and so is put on WFG

- **waits-for graph (WFG)**
- describes which transactions waits for others

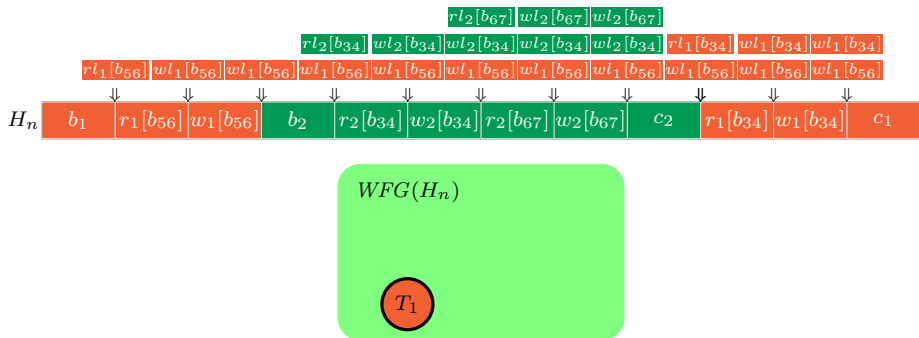
## Deadlock Detection: WFG with No Cycle = No Deadlock



$H_2$  can proceed to complete its execution, after which it will have released all its locks

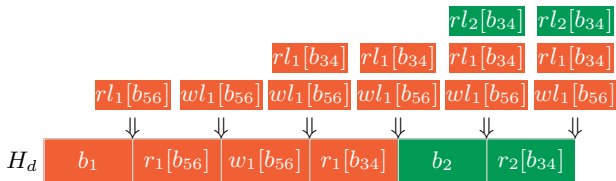
- **waits-for graph (WFG)**
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# Deadlock Detection: WFG with No Cycle = No Deadlock

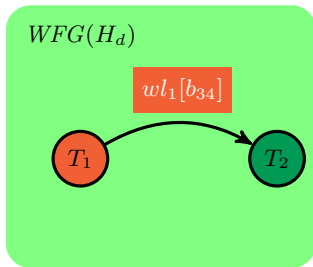
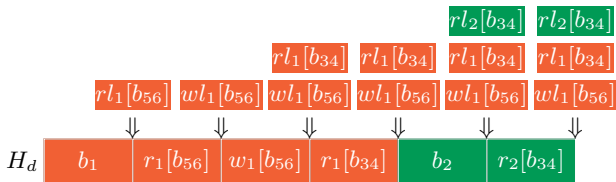


$H_1$  may now proceed to completion

## Deadlock Detection: WFG with Cycle = Deadlock



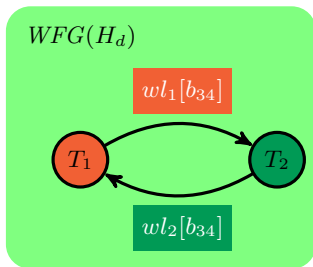
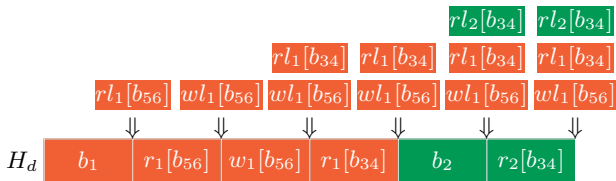
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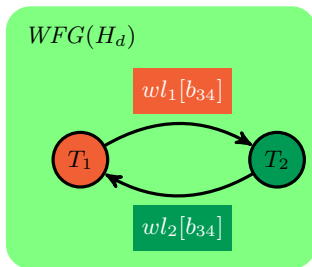
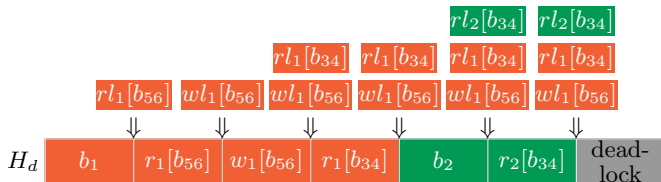


## Deadlock Detection: WFG with Cycle = Deadlock



$H_2$  attempts  $w_2[b_{34}]$ , but is refused since  $H_1$  has a read-lock, and so is put on WFG

## Deadlock Detection: WFG with Cycle = Deadlock



Cycle in WFG means DB in a deadlock state, must abort either  $H_1$  or  $H_2$

## Worksheet: Deadlocks

$$H_1 = w_1[o_1], r_1[o_2], r_1[o_4]$$

$$H_2 = r_2[o_3], r_2[o_2], r_2[o_1]$$

$$H_3 = r_3[o_4], w_3[o_4], r_3[o_3], w_3[o_3]$$

# Transaction Isolation Levels

- Do we always need ACID properties?

```
BEGIN TRANSACTION T3
  SELECT DISTINCT no
  FROM movement
  WHERE amount >= 1000.00
COMMIT TRANSACTION T3
```

- Some transactions only need ‘approximate’ results  
*e.g.* Management overview  
*e.g.* Estimates
- May execute these transactions at a ‘lower’ level of concurrency control  
*SQL allows you to vary the level of concurrency control*