Pharmacophore Discovery using the Inductive Logic Programming System Progol

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Abstract. This paper is a case study of a machine aided knowledge discovery process within the general area of drug design. More specifically, the paper describes a sequence of experiments in which an Inductive Logic Programming (ILP) system is used for pharmacophore discovery. Within drug design, a pharmacophore is a description of the substructure of a ligand (a small molecule) which is responsible for medicinal activity. This medicinal activity is produced by interaction between the ligand and a binding site on a target protein. ILP was chosen by the domain expert (first author) at Pfizer since active molecules are most naturally described, in relational terms, as requiring a substructure (pharmacophore) with various 3-D relations which hold among the atoms involved. The results described in this paper build on previous investigations into prediction of mutagenicity using ILP with a 2-D (bond connectivity only) representation of molecules. The case study supports general lessons for knowledge discovery, as well as more specific lessons for pharmacophore discovery, the use of ILP for 3-D problems, and for the particular medicinal activity of ACE inhibition, a treatment for hypertension.

Keywords: inductive logic programming, pharmacophore, structure-activity prediction

1. Introduction

This paper is a case study of a machine-aided knowledge discovery process within the general area of drug design. The case study focuses on three portions of the knowledge discovery task. The first is identification of a part of a larger task—in this case, drug design—for which machine learning might be useful. The selected subtask is pharmacophore discovery, which is recognized by chemists as an important problem in its own right. A pharmacophore is a 3-D substructure of a molecule that is responsible for its medicinal activity. More specifically, a pharmacophore is a set of atoms or chemical groups of interest—hydrophobic groups, hydrogen acceptors, hydrogen donors, or zinc sites—and their 3-D geometric arrangement. Pharmacophores are motivated and described more thoroughly in Section 2. The second portion of knowledge discovery that we address is the application of an ex-
isting machine learning algorithm to this selected task. Third, this paper considers the interaction between the users of the machine learning system and the domain expert, viewed as a client.

Our usage of the term knowledge discovery assumes a slightly stronger definition than the following taken from p.6 of [7].

Knowledge discovery in databases is the non-trivial process of identifying valid, novel, potentially useful, and ultimately understandable patterns in data.

In particular we assume that the knowledge involved is both declarative rather than procedural as well as being necessarily comprehensible and insightful to a domain expert. The latter condition is related to the view of the domain expert as a client who provides requirements for knowledge representation, much like the notion of requirement specification within software engineering. Within the present domain, the requirements that the knowledge should be both declarative and comprehensible stem from the fact that the knowledge involved should provide 3-dimensional structural insights to be used by a synthetic chemist involved in devising new drugs. Such relational knowledge descriptions are known within the drug design literature as pharmacophores. Successful applications of a machine learning technique in problems related to pharmacophore discovery have been discussed previously [12, 13]. The domain expert (first author) in the present study suggested a more explicit representation for pharmacophores (Section 2.2).

This paper describes a series of experiments providing insights at four different levels. First, regarding Angiotensin-Converting Enzyme (ACE) inhibition the experiments confirm an earlier proposal, generate an alternative proposal, and suggest that no other alternatives exist within the constraints provided by the domain expert. Second, they lead to a general methodology for pharmacophore discovery using Inductive Logic Programming (ILP). Third, the experiments indicate that ILP can be used successfully to learn 3-dimensional concepts and to deal naturally with the multiple instance problem [6] (see Section 2.3). Fourth, the experiments support four lessons regarding knowledge discovery in general.

Rediscovery Step An initial rediscovery step is useful when beginning work in a new problem domain. It can help build the confidence of a domain expert and can provide a thorough test of the encoding of domain or background knowledge.

A blindfold rediscovery step, in which the users of the machine learning system do not know the correct answer in advance, provides a particularly realistic test.

Mismatch of ML Heuristics with Problem Domains General purpose machine learning heuristics sometimes do not match particular problem domains. In the experiments reported in the present paper, the minimum description-length principle conflicts with a domain-specific preference for more complex pharmacophores.

Complete Search and Automatic Experiment Proposal Many machine learning systems return a single hypothesis for a given set of data, even when other
plausible hypotheses are available. The present work illustrates the value of instead performing a complete search for a set of plausible hypotheses. It also highlights the need for automatic proposal of experiments to discriminate between competing plausible hypotheses.

**Declarative Knowledge Representation** Using a declarative knowledge representation facilitates the development and debugging of background knowledge in collaboration with a domain expert.

These lessons are discussed in detail in Section 4, together with concomitant recommendations for research into knowledge discovery.

The paper is organized as follows. Section 2 describes in detail the problem of pharmacophore discovery, as well as describing other work on this problem and related problems. Section 3 describes the series of experiments regarding ACE inhibition. Section 4 discusses the contributions of this paper, including general lessons for research into knowledge discovery and particular lessons for inductive logic programming, for pharmacophore discovery, and for the study of ACE inhibition.

## 2. Background: Domain Description and Prior Work

### 2.1. Drug design process

Drug molecules work by binding (coming together in close association) to “target sites” within the body. These sites commonly are protein molecules, either enzymes or receptors. By interaction with these protein molecules, drugs can modulate their actions.

Typically, the process of drug design begins with the identification of an appropriate target with which drugs could interact to modulate disease. Closely connected with this process is the identification of a “lead” molecule or molecules. These molecules may be identified in a number of ways, for example from large scale empirical testing of available chemicals. They will have some activity, i.e., ability to interact with the target, but may do so only weakly and may possess other undesirable properties, for example metabolic instability. Chemists synthesize and test related molecules, possibly generating improved leads, until ultimately a molecule of the desired activity and properties is discovered. This molecule can then begin the long process of development, including safety and efficacy testing in clinical trials. If successful—and many are not—it finally will become a marketed product.

Computational techniques are used throughout this process, but rational drug design has concentrated on the section between the identification of the lead molecule and the entry of a candidate into development. This section of the process focuses on answering the question, “Why does the lead molecule possess the desired activity?” The general principles of drug activity are reasonably well understood, but answering this question for any specific case can be very difficult.

A ligand will bind with its target if it is complementary to it (see Figure 1). This complementarity consists of two parts:
Figure 1. A schematic representation of a drug/protein interaction, illustrating complementarity of shape and three complementary property interactions, one hydrophobic (green) and two hydrogen bonds (red).

**Complementarity of shape** This allows interaction between the drug and target over a large area. From a computational viewpoint, as we shall see below, shape complementarity is complicated by the fact that most drug molecules are flexible and thus can adopt a variety of shapes.

**Complementarity of properties** The strength of the interaction is determined by the ability to form a variety of weak interactions, primarily hydrophobic and electrostatic interactions (hydrogen bonds and interaction between oppositely charged groups). These interactions are individually weak, but their effects can sum to a strong overall interaction if they are in sufficient number and appropriately positioned.

Starting from a lead molecule, how does one develop candidate drugs? In some cases, the detailed structure of the target binding site is known, and this knowledge can be used directly in the design of improved molecules [31]. However, in the majority of cases, this information is unavailable and design must rely on what can be inferred from the structures of the ligands themselves and their biological activities. The approach, therefore, is to try to elucidate this “structure-activity relationship” (SAR) for the molecules. Analysis of how the structural differences of a set of ligands affects their activity can lead to the discovery of an SAR. This information can be used to suggest new molecules to make which should have enhanced activity.
2.2. Representation of the activity model

2.2.1. QSAR: advantages and limitations  Many ways have been used to represent the structure-activity relationships of molecules. The first to be developed—the so-called “traditional” quantitative structure-activity relationship (QSAR) methods—correlate properties calculated from the structures of the molecules with their activities. These properties can be properties of the whole molecule, such as partition coefficient, molecular volume, number of rings, etc, or, where the molecules share a common core, properties of the substructures at the positions of variation. Such models have been widely applied, and there are many examples of successful QSAR analyses [9]. While the correlations derived by such techniques can be used in the design of improved compounds, this is not always straightforward. Parameters such as electronic partial charges and connectivity index values are easy to calculate for a given structure, but it is much harder to design a molecule that will possess these values. Also, it is not always possible to relate the parameters to the principles of drug-receptor interaction described above. In addition, because QSAR methods operate on bulk molecular properties rather than explicit representations of the 3D structures of molecules, they do not take into account some structural information that can affect molecular activity. Nevertheless one advantage of traditional QSAR methods is that they avoid having to deal with the problem of molecular flexibility, which we now describe.

Molecules can adopt different shapes (conformations) by torsional rotations about bonds within the molecule. Molecules rapidly convert from one conformation to another, so that no single conformation can be isolated and tested for a given activity. Hence in general one does not know a priori which conformation of a molecule is an active conformation for a given form of activity. Each conformation is associated with an energy, which arises from interactions within the molecule and between the molecule and its environment. Only low-energy conformations are accessible at normal temperatures.

Any sample of a given compound contains molecules in a variety of different conformations. The concentration of a given conformation in a sample is related by an inverse exponential function to the energy of that conformation, so only very low-energy conformations appear in significant concentration. Computational techniques are available for calculating the energy of a given conformation, and for searching the conformational space to identify the low-energy conformations [16]. Any one of these conformations could be the one which binds to the target protein. The larger and more flexible the molecule, the more low-energy conformations it will have. One of the key problems for the approaches that have been adopted to analyze and predict biological activity is how to take account for this flexibility. Traditional QSAR techniques ignore molecular flexibility by describing only non-3D properties of molecules—properties that do not vary as a molecule changes conformation.

2.2.2. 3D QSAR techniques  3D-QSAR methods work within a correlation framework, but use an explicit representation of the molecule. The input is a series of
molecules with a spread of activity. In this method the shape and electrostatic interactions are dealt with more directly via a calculated interaction with a “probe” atom or group at points on a three-dimensional grid which surrounds the molecules. Statistical methods are then used to identify those parts of the molecule which are responsible for activity. The analysis can be displayed graphically to aid in the design of new molecules. The major disadvantage with this method is that, in order to compare values at the calculated points between molecules, the conformation of the molecules and a common coordinate frame, or alignment, must be chosen in advance of the analysis. This is equivalent to deciding the manner in which the molecules interact with the target. If the molecules contain a large common structural element this alignment may be straightforward, but this is often not the case.

The COMPASS algorithm [12, 13] overcomes these problems by using a more sophisticated representation of molecular shape, neural network learning methods and adaptation of the alignments. The models produced can be used to predict the activity of new molecules, and, again, visual representations of the results can aid compound design. However, the interpretation of the neural network may not be easy. Furthermore, the difficulty of the human brain in imagining complex three-dimensional shapes makes it difficult to the design molecules that are very different structurally from the known examples.
2.2.3. **Pharmacophores** A very commonly used representation of biological activity, and the one used in the present work, is the pharmacophore. This is an abstraction of the molecular structure to the, usually, small number of key features which contribute the majority of the activity, together with their geometric arrangement represented by pairwise distances (see Figure 2). These features relate directly to the interactions (hydrophobic, electrostatic, etc.) described above. In this view, the remainder of the molecule is useful only as scaffold, holding the pharmacophore groups in the correct spatial positions. Many methods of pharmacophore identification have been described. In the active analogue approach [19], it is necessary to identify the equivalent pharmacophore groups in each molecule in advance. Conformations of each of a series of active molecules are then sought which place these groups in a common spatial arrangement. Multiple solutions can be found by this method, and the need to identify the groups in advance limits its utility. The more general DISCO method [18] uses a clique detection algorithm [3] to search for common sets of inter-feature distances within a group of active molecules. Tolerances on the distance matches account for the use of discrete conformations and uncertainties in the pharmacophore. Our experience has been that, although DISCO can perform well in many cases, there are difficulties in cases where either the number of compounds and/or the numbers of conformations for each compound is large. This has stimulated our exploration of alternative pharmacophore discovery methods.

An advantage of the pharmacophore representation is that it expresses biological activity in a language that is familiar to chemists within the pharmaceutical industry. These representations are also readily convertible into search queries of compound databases, which is an effective means of identifying additional active molecules [8]. Because of these advantages, we have adopted a data input and output representation that is similar to DISCO. The input to the learning algorithm is a set of conformations for each molecule in the set. These conformations can be generated by whichever method is appropriate. Output is a pharmacophore expressed in terms of features such as hydrogen bond acceptor, or hydrophobic group and the distance relationships between them.

Thus far we have motivated and described the pharmacophore discovery problem, including a description of other approaches to this and related problems. The present paper describes the first application of ILP to pharmacophore discovery. The following subsection sets this work in the context of earlier related applications of ILP.

2.3. **Related Work Using ILP**

Pharmacophore discovery can be viewed as a particular case of structure-activity prediction, the goal of which is to learn to predict the activities of molecules based on their structures. The earliest technique used for structure-activity prediction was linear regression, first employed for this task by Hansch and colleagues in 1962 [10]. In recent years ILP has been used successfully for structure-activity prediction, first with a "1-dimensional" feature-value representation similar to that used with linear regression, and later with a "2-dimensional" chemical structure representation. The
Figure 3. The family of analogues in the first ILP study. A) Template of 2-4-diamino-5(substituted-benzyl)pyrimidines R3, R4, and R5 are the three possible substitution positions. B) Example compound: R3 = –Cl; R4 = –NH2; R5 = –CH3

The present work on pharmacophore discovery builds on these earlier applications of ILP by moving to a more complex “3-dimensional” representation of molecules. The remainder of this section sets the present work in the context of the earlier applications of ILP to structure-activity prediction.

2.3.1. Learning with a 1D representation In ILP’s first successful application to structure-activity prediction [14], the Golem program [23] was applied to the problem of modeling the structure-activity relationships of trimethoprim analogues binding to dihydrofolate reductase. The training data consisted of 44 trimethoprim analogues and their observed inhibition of Escherichia coli dihydrofolate reductase. A further set of 11 compounds were used as unseen test data. Golem obtained rules that were statistically more accurate on the training data and also better on the test data than a previously published linear regression model. We refer to the representation used in this work, as well as with linear regression, as a “1-dimensional” representation because an example molecule is represented as a vector of variables describing either whole molecule properties or substituent groups on a common structural backbone. Such a representation was possible for this problem because all of the molecules shared a common structure; Figure 3 shows the shared structure, or template, for all the molecules, as well as one particular instance of the template.

2.3.2. Learning with a 2D representation In a more recent study [15] the 2D bond-and-atom molecular descriptions of 229 aromatic and heteroaromatic nitro
compounds taken from [5] were given to the ILP system Progol [21]. Such compounds frequently are mutagenic. It is of considerable interest to the pharmaceutical industry to determine which molecular features result in compounds having mutagenic activity. The problem of predicting mutagenicity is addressed by another paper in the present special issue [7]. The study was confined to the problem of obtaining structural descriptions that discriminate drugs with positive mutagenicity from those which have zero or negative mutagenicity. A set of 8 optimally compact rules were automatically discovered by Progol. These rules suggested 3 previously unknown features leading to mutagenicity. The molecules used in this study could not have been represented easily by a 1D feature-vector because they were a diverse set with no common structural backbone. Attempts to force the 2D representation into a set of features resulted in the generation of examples containing more than a million features each.

2.3.3. Challenges of a 3D Representation We have seen that ILP has been applied successfully to structure-activity prediction problems using 1D and 2D representations of molecules. Nevertheless, the 3D aspects of molecules (or their stereochemistry) is often crucial in determining molecular activity. Therefore the feeling of some chemists is that widespread successful application of ILP or any other machine learning technique to structure-activity prediction requires a 3D representation. The present paper reports the first attempt to use a 3D representation within ILP (a preliminary version of this work was presented at the Seventh International Workshop on Inductive Logic Programming [24]). The move to a 3D representation within ILP brings two important challenges, which we now summarize.

The first challenge is in choosing how to represent 3D geometric concepts in first-order logic. In summary, the approach taken in the present work is to represent geometry via pairwise distances between points. Of course if a hypothesis requires a precise floating point value for the distance between any two points, then few if any examples will be labeled positive by that hypothesis. Therefore we allow a degree of tolerance in the matching of distances. In the present work, the precise degree of tolerance is suggested by the domain expert, although another option is to let the learning algorithm itself vary the tolerance levels.

The second challenge is the multiple instance problem, a general issue first raised by Lathrop, Dietterich, and Lozano-Perez [6]. They also were motivated by the context of drug design (their neural network-based system COMPASS was described earlier in this section), and the problem is probably easiest to explain in this concrete context. As noted in the domain description earlier in this section, a molecule can take on a variety of 3D conformations, and it is quite possible that a molecule with a desired biological activity exhibits that activity in only one of its conformations. But because molecules rapidly interconvert between conformations, no single conformation can be isolated and tested. The set of conformations of a molecule corresponds to a set of examples, but we do not have sufficient knowledge to label each individual example as active or inactive—we can label only the set as a whole. Thus a hypothesis explaining activity should label a set active just if it predicts that at least one example in the set is active. In general terms, the multiple instance
problem occurs when individual examples cannot be labeled, but instead sets of examples are labeled, such that a set is labeled positive if and only if at least one member of the set is positive.

Lathrop, Deitterich, and Larano-Perez raise the multiple instance problem as a general machine learning problem, although they do cite any other real-world domains where it arises. We can support their claim of its generality by citing at least one additional domain. In recent work Saith et al. [27] used C4.5 to learn a decision tree for choosing embryos to return to a mother’s womb after in vitro fertilization. Under British law only three embryos can be implanted at one time, although as many as eight may be available. To maximize the probability of success, doctors wish to choose the most viable embryos—those most likely to lead to a healthy pregnancy—and a decision tree for choosing embryos can be learned from previous cases. But again examples are grouped into sets, this time into sets of three. A set is labeled positive just if at least one of the embryos in the set (without our ability to know which one) results in success—parents taking home a baby—and negative otherwise.

The form of uncertainty embodied in the multiple instance problem did not arise in earlier ILP applications using a 1D or 2D representation of molecules, because only whole-molecule properties (e.g., molecular weight) and aspects of the (bond-and-atom) molecular structure were represented. A 3D representation provides additional information that can be central to molecular activity, yet this additional information is inherently disjunctive in that a molecule can adopt any of several low-energy conformations. The approach to the multiple instance problem that is taken in the present work is different from approaches taken in either of the other two aforementioned papers. In the work on COMPASS, an entirely new neural network algorithm had to be developed. In the work on in vitro fertilization using decision-tree techniques, examples within a set were averaged (using mean, median, or mode values of features as deemed appropriate) to yield a single example instead. It turns out that a relational representation allows the multiple instance problem to be addressed in a surprisingly straightforward way, without the need to develop a new learning algorithm tailored to the problem and without the loss of information that can come from averaging over examples in a set. Section 4.2 describes the general approach, building on details given in Section 3.6 for the specific case of pharmacophore discovery.

3. Experimentation

This section describes a sequence of four experiments using the ILP system Progol [21] to discover a pharmacophore for ACE inhibition. ACE (Angiotensin-Converting Enzyme) inhibitors are a widely-used form of medication for hypertension. Progol is used in such a way that it returns human-comprehensible pharmacophore descriptions which also can be visualized. The techniques used in these experiments appear to be of sufficient generality to apply to other problems of pharmacophore discovery. We begin this section with an overview of Progol, providing
only the level of detail needed to understand the experiments, and an overview of
the sequence of experiments.

3.1. Progol

Because Progol is an ILP system, it learns first-order definite clause theories, or
logic programs. Progol takes as input positive examples and (if available) negative
examples of a target concept, as well as a background theory, all in Horn clause
form. An example is redundant if it is positive and is already provable from the
background theory, and an example is contradictory if it is negative and is provable
from the background theory. Progol removes any redundant examples and
expects the user to remove contradictory examples. In addition to examples and a
background theory, Progol takes as input a description of the hypothesis space, in
the form of a specification of the kinds of clauses that are acceptable. In learning
a single clause, Progol performs a complete search of the hypothesis space, using
pruning similar to that used in A* [25], to find a clause $c$ that maximizes a com-
pression function. The compression function is $f(c) = P(c) - N(c) - L(c)$, where
$P(c)$ is the number of positive examples that can be proven by the clause $c$ taken
together with the background theory, $N(c)$ is the number of negative examples that
can be proven in the same way, and $L(c)$ is the size (number of literals) of $c$. In
addition, the user may specify a maximum acceptable value of $N(c)$ (such as 0, in
a noise-free case), which Progol will respect.

Progol takes a greedy set cover approach to learning multiple clause theories.
Nevertheless, this issue is of little consequence for the present paper because we
adopt a one-clause representation of pharmacophores, described later in this section.
A multiple clauses theory for ACE inhibition therefore would represent a disjunction
of pharmacophores, such that a molecule is an ACE inhibitor just if it exhibits
at least one of the pharmacophores. A disjunction of pharmacophores suggests
multiple binding sites, such that binding to any of the sites produces the desired
biological activity. Such a multiple-clause theory is not desired for ACE inhibition
or for most pharmacophore discovery problems.

Progol's search is a refinement graph search [28], but this and most details about
Progol are beyond the scope of this paper. Nevertheless, two further aspects of
Progol's operation are important for this paper. Rather than providing a technical
discussion of these aspects, we provide a high-level description together with a
discussion of their significance for the problem of pharmacophore discovery. In this
discussion we consider single-clause learning only.

During learning, Progol focuses on a single positive example and constructs a
"bottom" clause containing everything, subject to language constraints, that is
true of that positive example according to the background theory. For theoretical
reasons [21], the bottom clause can be used to direct Progol's search without
sacrificing completeness. For the problem of pharmacophore discovery, the bottom
clause effectively identifies all the potential pharmacophobic points in the first ac-
tive molecule, and also records the distance between each pair of these points. The
search then proceeds by beginning with them "empty" pharmacophore (0 points)
and constructing progressively more complex pharmacophores from the points and
distances in the bottom clause. The constructed pharmacophores are tested on
the remaining molecules. This approach of basing a search on a “bottom” clause
gives Progol significant efficiency advantages for the problem of pharmacophore
discovery, because it substantially prunes the search space before the search even
begins.

The second aspect of Progol that is significant for the problem of pharmacophore
discovery is its complete search. Progol is guaranteed to find all clauses that max-
imize the compression function. For the problem of pharmacophore identification,
this means Progol will find all potential pharmacophores (given the hypothesis
language and background knowledge provided) that are consistent with the data.
Hence, not only does Progol provide a user with potential pharmacophores, but it
also tells the user that no other pharmacophore is possible within the constraints
given.

It was the decision of the domain expert (first author) at Pfizer to use ILP for
pharmacophore discovery since a pharmacophore is most easily described through
the use of 3D relations, which are easily represented using logic programs. We
expect that relational learning systems other than Progol could be applied suc-
cessfully in this domain as well. Progol was chosen in part simply because it was
developed by some of the present authors and therefore would be easier to mod-
ify if necessary. Nevertheless, Progol’s complete search based on a bottom clause
turns out to be particularly well-suited to pharmacophore discovery; this match is
discussed in Sections 4.2 and 4.3.

3.2. Overview of the Experiments

A pharmacophore was proposed for ACE inhibition eleven years ago by Mayer et
al., [19]. Earlier modeling studies had also investigated the ACE pharmacophore,
but based on a small number of compounds [11, 1]. The first experiment described
in the present paper was a blindfold test to see whether Progol could rediscover
the pharmacophore proposed by Mayer et al., given their particular assumptions
(regarding the active 3D conformations and zinc-binding geometry, described in
the next subsection). The test was a blindfold test in that the knowledge engineers
were not told in advance the proposed pharmacophore.

In most pharmacophore discovery applications, a particular active 3D confor-
mation for each molecule cannot be assumed, but rather it can be assumed only that for
any active molecule at least one of its low-energy conformations (see Section 2.1) is
active. The second experiment was designed to test whether Progol could discover a
new pharmacophore and/or re-discover the original proposed pharmacophore when
provided with multiple low-energy 3D conformations for each molecule. It was not
evident that Progol would, or even should, rediscover the original proposed phar-
macophore in such an experiment, because the conformations used by Mayer et
al., are not all energy-minimized, nor are their zinc-binding geometries ideal. In
this experiment Progol in fact was unable to identify any pharmacophore common
to all ACE inhibitors. Several possible explanations for this were considered. In
the end, the knowledge engineers found in their encoding of chemical background knowledge an apparently incorrect assumption they had made. This assumption appeared to be the reason for failure to find any pharmacophore. This type of 'failed' experiment usually is not reported in applications papers. We include the description of this experiment, as well as the next experiment, because they are instructive regarding the knowledge engineering issues that often arise in a real machine learning application.

In the third experiment, Progol identified a single pharmacophore, distinct from the original proposed pharmacophore. Nevertheless, this new pharmacophore was deemed unreasonable by the domain expert. It is unreasonable because the points in the pharmacophore are too close to each other and are likely to give rise to “steric hindrance.” After careful consultation with the domain expert, it was discovered that the assumption in Experiment 2 deemed incorrect by the knowledge engineers actually was correct, but that another incorrect assumption was encoded in the background theory. This incorrect assumption was responsible for Progol proposing no reasonable potential pharmacophore.

In the final experiment, with the debugged background theory, Progol identified 28 potential pharmacophores, but many arose from only small perturbations in the geometries of others. The set of 28 pharmacophores can be condensed into a pair of distinct proposed pharmacophores for ACE inhibition. One of these pharmacophores is the same (modulo a small geometric perturbation) as the pharmacophore found in the first experiment, thus confirming the proposal of Mayer et al. [19]. The second is an interesting alternative that deserves further attention. Furthermore, because Progol performs a complete search, this result says that there are no further alternatives to these two pharmacophores, given the constraints imposed.

3.3. Experiment 1: a Blindfold Test

The first experiment was a blindfold test of Progol’s ability to learn a pharmacophore. The knowledge engineers were provided with data and relevant chemical information, but they were not told the proposed pharmacophore. This experiment tested the following hypothesis.

**Hypothesis 1:** Given the conformations and zinc binding sites proposed in [19], as well as definitions of hydrogen acceptors and hydrogen donors, Progol will re-discover the pharmacophore proposed in [19].

3.3.1. Data  The data used in this experiment consisted of 28 compounds known to exhibit the activity of ACE inhibition. These 28 compounds were taken from [19]. Compounds vary in size from 23 atoms to 78 atoms. The compounds were identified by the names m1, m2, ..., m28. Their activity as ACE inhibitors was asserted to Progol via first-order atomic formulae, or Prolog-style facts, of the form active(m1), active(m2), ..., active(m28). Note that no negative examples were used, although negative examples can be incorporated easily if they are available. The size of this data set is typical of data sets used by computational chemists.
3.3.2. **Background Knowledge**  The background knowledge used in this experiment can be divided into the following three types.

1. compound-specific knowledge
2. general chemical and geometric knowledge
3. constraints on legitimate pharmacophores

**Compound-specific knowledge**

Compound-specific knowledge included the atom and bond structure of each compound, as well as its 3-dimensional conformation. This information was represented by first-order atomic formulae, or Prolog-style facts. A fact of the form

\[
\text{atm}(m1,a1,o,2,3.43,-3.12,0.05)
\]

asserts that molecule \( m1 \) has an atom which we will call \( a1 \) that is an oxygen, is \( sp2 \)-hybridized (a detail that turns out to be of no consequence), that is at position \((3.43,-3.12,0.05)\) in three-dimensional space, for the given conformation and orientation of the molecule. The 3D grid is in units of Angstroms. Other atom types include \( c \) for carbon, \( n \) for nitrogen, \( h \) for hydrogen, \( s \) for sulphur, and \( p \) for phosphorus. A fact of the form

\[
\text{bond}(m1,a2,a3,2)
\]

asserts that molecule \( m1 \) has a bond between atoms \( a2 \) and \( a3 \), and that bond is a double bond.

As noted in Section 2.1, molecules can arrange themselves in a number of 3D conformations. In this experiment, for each molecule the background knowledge recorded only the conformation that Mayer et al. believed permits binding (and thus exhibits the activity of ACE inhibition). For later experiments, the assumption that the Mayer et al. conformation is the active one was removed, and multiple low-energy conformations were used for each molecule.

**General Chemical and Geometric Knowledge**

Binding into a metalloproteinas such as ACE often involves formation of a traditional (covalent) bond to a metal ion. But more generally, binding almost always involves the formation of weaker hydrogen bonds. Hydrogen bonds are simply the attraction between a hydrogen atom with a slight positive charge and an atom such as oxygen or nitrogen with a slight negative charge. A hydrogen atom bears a positive charge if it is covalently bonded to a more electronegative atom, such as oxygen or nitrogen, that draws the shared electron pair (constituting the covalent bond) away from the hydrogen atom; this also has the effect of giving the other atom a partial negative charge. For example, water has a higher boiling point than substances such as propane or butane partially because of hydrogen bonds that form between the oxygen atom of one water molecule and a hydrogen atom of another water molecule, holding the two molecules together. The hydrogen atom in a hydrogen bond is called a hydroxgen donor, while the other atom is called a hydroxgen acceptor.
We can now describe the general chemical knowledge supplied by the domain expert. The expert noted that hydrogen donors and acceptors are potentially important for any pharmacophore discovery task, and metal ion sites are potentially relevant to any task (such as this one) involving a metalloproteinase. Furthermore, hydrophobic (water repelling) groups such as benzene or alkane chains or rings are often important for pharmacophore discovery, particularly if one is interested in high degrees of activity. It was straightforward to encode in definite clause form the expert’s definitions for all these potentially relevant items. The expert suggested that because the molecules in our data set are all active, but without degrees of activity specified (so they do not necessarily all have extremely high activity), hydrophobic groups were less likely to be useful. Hence we ignore hydrophobic groups in the discussion of this experiment until the end. In addition, the expert requested that a pharmacophore be expressed as its points (hydrogen donors, hydrogen acceptors, and zinc sites) and their geometric arrangement, described by the pairwise distances among them. A molecule is said to exhibit the pharmacophore if it has atoms or groups that match with each of the points in the pharmacophore, such that all pairwise distances agree with the pharmacophore distances to within one Angstrom. Finally, the expert noted that pharmacophores generally have at least three points but rarely more than five points.

**Constraints on Pharmacophore Descriptions**

Given the requirements of the domain expert, the following clause would be an acceptable description of a pharmacophore.

\[
\text{active}(X) :- \text{hdonor}(X,A), \text{hacc}(X,B), \text{zincsite}(X,C), \text{dist}(X,A,B,3.0,1.0), \\
\text{dist}(X,A,C,4.0,1.0), \text{dist}(X,B,C,5.0,1.0)
\]

This clause asserts that a molecule \(X\) is active if it has a hydrogen donor \(A\), a hydrogen acceptor \(B\), and a zinc site \(C\), such that the distance between \(A\) and \(B\) is 3.0 +/- 1.0 Angstroms, the distance between \(A\) and \(C\) is 4.0 +/- 1.0 Angstroms, and the distance between \(B\) and \(C\) is 5.0 +/- 1.0 Angstroms.

In general, the head of any clause describing a pharmacophore should be \(\text{active}(X)\), while the body should specify the points of the pharmacophore via the predicates \(\text{hdonor}, \text{hacc},\) and \(\text{zincsite}\), and should also specify the distance between each pair of points via the \(\text{dist}\) predicate. Furthermore, the clause should specify at least three points for the pharmacophore. These constraints are specified within Prolog; the Prolog input file is available from the contact author on request.

In fact, at the outset of this experiment it was not possible to encode domain-specific constraints such as these in Prolog. This experiment motivated a general change to the Prolog interface and algorithm. This general change is the capability to express a declarative bias, a restriction on acceptable hypothesis that goes beyond the language bias imposed by the representation vocabulary. A user can now write arbitrary Prolog clauses to specify explicitly which kinds of clauses within the given vocabulary are or are not acceptable as hypotheses. Already these general constructs have proven useful in a variety of other applications of Prolog as well as the current one. Full details of the mechanism for expressing declarative bias are beyond the scope of this paper but can be found in [29].
3.4. Methodology

Having specified the data and the background knowledge, the methodology for this blindfold trial was nearly as simple as, “(1) Run Progol with the data and background knowledge given, and (2) compare the result with the proposed pharmacophore of Mayer et al.” Only one modification was made to this methodology, which we now motivate. The motivation is applicable to not only Progol but any compression-driven or MDL-like algorithm.

A mismatch exists between Progol’s compression heuristic (and compression-driven search in general) and pharmacophore search. In general, larger pharmacophores that are common to a set of active molecules are more interesting than smaller ones, because large shared structures are less likely to occur by chance. Furthermore, the existence of a large shared structure implies the existence of several smaller shared structures. For example, if 28 molecules share a four-point pharmacophore then they share four three-point pharmacophores which can each be obtained by deleting one point from the four-point pharmacophore. Yet although the larger pharmacophores are of greater interest, their representations are textually longer and therefore compression scores them as less interesting. The result is that Progol will never return the larger pharmacophores. This mismatch between compression and pharmacophore search extends beyond pharmacophore search to any application domain where textually longer hypotheses are a priori less likely to be consistent with random data, that is, less likely to be true by chance.

The mismatch between compression and pharmacophore search was addressed by the following change to the methodology. Progol was run repeatedly, first to search for three-point pharmacophores, then four-point pharmacophores, etc. In general with such an approach, once a number n is reached such that no n-point pharmacophore is found, the search can be terminated—if no n-point pharmacophore exists then no (n + 1)-point pharmacophore exists. This approach can be viewed as a manual wrapper around Progol. A manual wrapper is one of the potential solutions mentioned in Section 4 when a general machine learning heuristic does not match a particular problem domain.

3.5. The result

In the experiment Progol found four three-point pharmacophores and one four-point pharmacophore that are common to all 28 ACE inhibitors. The four three-point pharmacophores are all obtained from the four-point pharmacophore by omitting one point, so it is clear that the four-point pharmacophore is the most interesting. No potential five-point pharmacophore appears in more than 10 of the 28 ACE inhibitors. The one that appears in 10 of the 28 results from adding one point to the four-point pharmacophore. No other five-point pharmacophore appears in more than 4 of the 28 molecules.

It is a straightforward matter to translate clauses of a pre-defined form, such as those representing pharmacophores, into English; Progol has the necessary instructions to do so. Therefore, we present the Progol-generated English description of
the four-point pharmacophore here. This four-point pharmacophore was judged equivalent to the Mayer et al. proposed pharmacophore by the domain expert.

Molecule A is an ACE inhibitor if:
- molecule A can bind to zinc at a site B, and
- molecule A contains a hydrogen acceptor C, and
- the distance between B and C is $7.9 \pm 1.0$ Angstroms, and
- molecule A contains a hydrogen acceptor D, and
- the distance between B and D is $8.5 \pm 1.0$ Angstroms, and
- the distance between C and D is $2.1 \pm 1.0$ Angstroms, and
- molecule A contains a hydrogen acceptor E, and
- the distance between B and E is $4.9 \pm 1.0$ Angstroms, and
- the distance between C and E is $3.1 \pm 1.0$ Angstroms, and
- the distance between D and E is $3.8 \pm 1.0$ Angstroms.
The ability to generate an English description of the found pharmacophore, in a form commonly used by chemists, is a significant advantage of this approach. In addition, this approach makes visualization a relatively simple matter. Because the pharmacophore is also represented as a logical clause, a logic programming query can be executed to identify the pharmacophoric points within each molecule. Once these points are identified, each molecule can be displayed with the instance of the pharmacophore highlighted and labeled. Figure 4 shows two of the 28 molecules with the points of this pharmacophore labeled; notice that the labels correspond to the variable names in the English description of the pharmacophore.

This experiment confirmed the hypothesis that Prolog can re-discover the Mayer et al. pharmacophore given their original assumptions regarding the active conformation and the zinc site. In addition, another result of the experiment was a thoroughly-tested background theory for use in the further experiments.

In closing this section, we recall the earlier mention of hydrophobic groups. A variation of the experiment was run, allowing the inclusion of hydrophobic groups in the pharmacophore. The result was that no pharmacophore of three or more points, where at least one point is a hydrophobic group, appeared in all 28 molecules.

3.6. Experiment 2: Multiple Conformations and Multiple Zinc Sites

We have already identified the two shortcomings of the previous blindfold trial in assessing our approach to pharmacophore discovery. The first shortcoming is the unrealistic assumption of a single known active conformation for each active molecule. In a realistic experiment, a set of the lowest energy conformations should be used instead, and the only assumption should be that the molecule will exhibit the desired activity in at least one of these conformations. These low-energy conformations can be estimated by a computational chemist using molecular modeling software. The second shortcoming is the assumption of a single known site for the zinc ion in ACE relative to the active molecule during binding. In a realistic experiment, a set of possible sites should be used instead. A zinc site is identified by first finding a functional group within the molecule that is capable of binding to zinc, and then calculating where the zinc ion should be in geometric relationship to this group for binding to occur. Sufficient chemical knowledge exists to identify both the functional groups that can bind to zinc and the geometry of ideal binding. The experiment we now describe implemented these changes and tested the following hypothesis.

**Hypothesis 2:** Given the ten lowest energy conformations for each ACE inhibitor (as estimated by a computational chemist using molecular modeling software), and given potential zinc sites as computed according to general chemistry knowledge, Prolog will identify at least one pharmacophore for ACE inhibition.

The data for this experiment was the same as for the previous one. Only the background knowledge changed for this experiment. We now describe this background knowledge.
3.6.1. The Background Knowledge  Again we divide the background knowledge into three parts: compound-specific knowledge, general chemical and geometric knowledge, and constraints on the hypothesis.

Compound-specific Knowledge

Compound-specific knowledge was encoded in the same way as for Experiment 1, except that an additional argument was added to each fact to specify the conformation. The structure of a molecule was repeated for each conformation, and a given atom of the molecule might have a different location in each conformation. For example, the following facts give the details of atom $aI$ in conformation $cI$ and $cI0$ of molecule $m28$. The second argument of each fact provides the unique conformation identifier.

$\text{atom}(m28,c1,a1,n,am,-0.79,-3.78,4.13).$

$\text{atom}(m28,c10,a1,n,am,-1.34,-4.05,0.77).$

General Chemical and Geometric Knowledge

The additional chemical knowledge used in this experiment concerned zinc binding. The domain expert described five functional groups that can bind to zinc, four of which appear in the molecules in the given data set. Functional groups turn out to be surprisingly natural to represent in definite clause form. Code for these functional groups is available from the contact author and in an on-line appendix.

Further chemical knowledge from the domain expert specified where the zinc must be located relative to the functional group. For example, for a thiol group (Figure 5) the ideal binding geometry locates zinc at 2.4 Angstroms from the sulphur atom to which it binds, at a 97 degree angle to the $C - S$ (carbon-sulphur) bond, and at a torsion angle to the $R - C - S$ plane of 0 or 180 degrees, plus or minus at most 60 degrees.

In addition to this chemical knowledge, geometric knowledge was encoded to compute the zinc site. The same code was used to compute the zinc site relative to each functional group that can bind to zinc. In each case points analogous to $R$, $C$, and $S$ for thiol were used together with ideal bond length, bond angle, and torsion angle(s) for the given group in order to compute an ideal zinc site. Sites within 2 Angstroms of another atom in the molecule were eliminated, because these would not be possible due to steric hindrance (crowding).

Constraints on Pharmacophore Descriptions

Given the addition of conformational information, the following is an example of an acceptable clausal representation of a pharmacophore.

$\text{active}(X) :- \text{hdonor}(X,Y,A), \text{hacc}(X,Y,B), \text{zincsite}(X,Y,C),$
$\text{dist}(X,Y,A,B,3.0,1.0), \text{dist}(X,Y,A,C,4.0,1.0),$
$\text{dist}(X,Y,B,C,5.0,1.0).$

This clause asserts that a molecule $X$ is active if it has a conformation $Y$, and it has a hydrogen donor $A$, a hydrogen acceptor $B$, and a zincsite $C$, such that the distance between $A$ and $B$ within conformation $Y$ is 3.0 +/- 1.0 Angstroms, the distance between $A$ and $C$ within conformation $Y$ is 4.0 +/- 1.0 Angstroms, and the distance between $B$ and $C$ within conformation $Y$ is 5.0 +/- 1.0 Angstroms.
Figure 5. Ideal geometry for a thiol group binding to zinc. The length of the sulphur–zinc bond is 2.4 Angstroms, and the carbon–sulphur–zinc angle is 97 degrees. The torsion angle is most easily described by example. A torsion angle of 0 or 180 has zinc in the plane defined by the sulphur, carbon, and R (the next connected atom in the rest of the molecule); by default, 0 degrees is taken to have the zinc and R in the same side (half-plane) of the sulphur–carbon bond. A 90 degree torsion angle has the zinc coming directly out from the page. Thus in the figure the torsion angle is 180 degrees.

In general, the same requirements as before were placed on clauses, with one additional requirement: the conformational variable in the body literals must be the same throughout the clause. Without this requirement, Prolog might return a clause of the following form.

\[
\text{active}(X) :- \text{hdonor}(X,Y,A), \text{hacc}(X,Y,B), \text{zincsite}(X,Y,C), \\
\text{dist}(X,Y,A,B,3.0,1.0), \text{dist}(X,Z,A,C,4.0,1.0), \\
\text{dist}(X,W,B,C,5.0,1.0)
\]

Notice that the conformational variables in the last two literals are distinct from the conformational variable, Y, in the rest of the clause. Such a clause is easier to satisfy since we need only find some conformation in which the distance between A and B is roughly 3 Angstroms, some (possibly different) conformation with a distance of roughly 4 Angstroms between A and C and some (possibly different again) conformation with a distance of roughly 5 Angstroms between B and C. Such a clause does not represent a true pharmacophore.

3.6.2. The Result The result of the experiment was that no pharmacophore appeared in all 28 ACE inhibitors. Specifically, no pharmacophore appeared in more than 26 of the ACE inhibitors. This result seemed to indicate that Hypothesis 2 was false and that Prolog could not successfully meet the challenges of pharmacophore prediction with multiple conformations. Nevertheless, before considering
Hypothesis 2 to be disproven, an examination of the possible reasons for this result was in order. The following are the potential alternative explanations identified by the authors on first seeing the result.

1. For the two unexplained ACE inhibitors, perhaps additional stereoisomers\(^3\) were included in the sample that was tested for activity. Such mixtures are common because often it is difficult to isolate a stereoisomer.

2. Perhaps some low-energy conformations were omitted for the 2 unexplained ACE inhibitors.

3. An error may have been made in the background theory.

The first possible explanation was ruled out by the domain expert after a review of the methodology for testing the 28 compounds for ACE inhibition. The second possible explanation also was ruled out by the domain expert, for the following reason. While some additional conformations could be added for some of the molecules in the data set, the two unexplained molecules are small and rigid, so that no other relatively low-energy conformations are possible.

Within the background theory the following assumption had been made by the knowledge engineers without checking with the domain expert.

**Co-reference Assumption** A hydrogen acceptor within a pharmacophore cannot also be the atom that binds to zinc.

The co-reference assumption could have dramatic consequences, because oxygen is generally a hydrogen acceptor and also can bind to zinc when it appears in one of two common functional groups—carbonyls and carboxylates. Recognition of the co-reference assumption led to Experiment 3, which we now describe.

### 3.7. Experiment 3

The data and background knowledge for Experiment 3 were the same as for Experiment 2, with the exception that an atom could now be used as both a hydrogen acceptor and the atom that binds to zinc within a pharmacophore. The result of this Experiment was that a single four-point pharmacophore was found; it is shown here.

Molecule A is an ACE inhibitor if for some conformation B:

- A contains a hydrogen acceptor C,
- A contains a hydrogen acceptor D,
- the distance between C and D within conformation B is 3.2 +/- 1.0 Angstroms,
- A contains a hydrogen acceptor E,
- the distance between C and E within conformation B is 4.0 +/- 1.0 Angstroms,
- A can bind to zinc at a site F,
- the distance between C and F within conformation B is 3.9 +/- 1.0 Angstroms,
- the distance between D and F within conformation B is 2.0 +/- 1.0 Angstroms,
- the distance between E and F within conformation B is 3.1 +/- 1.0 Angstroms.
Nevertheless, this pharmacophore was judged by the domain expert to be unreasonable because the zinc site is too close to the hydrogen acceptors. Further conversation revealed that the co-reference assumption, although not checked with the domain expert, actually is sensible. Therefore this assumption was reinstated.

On closer examination, a problem was identified with the definition of thiol. The definition of thiol initially required that the carbon atom single-bonded to sulphur must also be bonded to two hydrogen atoms. Such bonding is unnecessary and the definition was amended accordingly. Both of the unexplained ACE inhibitors contain thiol groups in which the carbon is not bonded to two hydrogens. This error was found while sitting with the chemist in front of the computer and together going through the code defining the functional groups that can bind to zinc. Such a mode of debugging was facilitated by the declarative nature of the code. This correction to the background theory lead to Experiment 4.

3.8. Experiment 4

In Experiment 4, the data and background knowledge were the same as for Experiment 3, except for the changes just described. The result of Experiment 4 was that 28 pharmacophores were found to appear in all 28 ACE inhibitors. These form two groups that can be represented by one pharmacophore each. The criterion for grouping is that any pharmacophore in the group can be converted to the representative pharmacophore by modifying its distances by less than one Angstrom. The two pharmacophores are as follows.

**Molecule A is an ACE inhibitor if for some conformation B:**
- A contains a hydrogen acceptor C,
- A contains a hydrogen acceptor D,
- the distance between C and D within conformation B is 3.2 +/- 1.0 Angstroms,
- A contains a hydrogen acceptor E,
- the distance between C and E within conformation B is 4.0 +/- 1.0 Angstroms,
- the distance between D and E within conformation B is 2.2 +/- 1.0 Angstroms,
- A can bind to zinc at a site F,
- the distance between C and F within conformation B is 5.5 +/- 1.0 Angstroms,
- the distance between D and F within conformation B is 7.1 +/- 1.0 Angstroms,
- the distance between E and F within conformation B is 8.5 +/- 1.0 Angstroms.

**Molecule A is an ACE inhibitor if for some conformation B:**
- A contains a hydrogen acceptor C,
- A contains a hydrogen acceptor D,
- the distance between C and D within conformation B is 3.2 +/- 1.0 Angstroms,
- A contains a hydrogen acceptor E,
- the distance between C and E within conformation B is 4.0 +/- 1.0 Angstroms,
- the distance between D and E within conformation B is 2.2 +/- 1.0 Angstroms,
- A can bind to zinc at a site F,
- the distance between C and F within conformation B is 3.9 +/- 1.0 Angstroms,
- the distance between D and F within conformation B is 6.1 +/- 1.0 Angstroms,
- the distance between E and F within conformation B is 7.3 +/- 1.0 Angstroms.

The two pharmacophores differ in the position of the zinc site relative to the hydrogen acceptors. This result provides three items of information about ACE inhibition. First, it confirms the Mayer et al. result. Even though the Mayer et al.
zinc sites do not obey ideal binding geometry and even though some of their conformations are not energy-minimized, their result is valid when using ideal binding geometries and energy-minimized conformations. Second, the result provides an alternative potential pharmacophore that merits further investigation. A recently published modeling study of ACE inhibition based on superposition of a small number of conformationally constrained inhibitors [2] also identified two models differing primarily at the zinc site. The models appear similar to ours, but there is insufficient information in the paper to enable a detailed comparison. The third item of information the result provides is that these two pharmacophores are the only ones possible given the assumptions encoded in our background theory.

For machine learning methods that perform a complete search, as Progol does, computational complexity is a particular concern. The analysis in the appendix indicates that the most important variables are the number of potential zinc sites and the number of conformations. Nevertheless, the run time of Progol in Experiment 4 was only 20.4 minutes on a Sun SPARC 20. Two decisions helped keep the runtime low. First, zinc sites and pairwise distances between potential pharmacophoric points were precomputed. This avoided unnecessary repetition of costly (though still polynomial-time) computations. Second, three-point pharmacophores were first discovered by Progol, and these were combined by Progol into four point pharmacophores. It should be noted that this second decision actually increases the worst-case time complexity, although in practice it is a significant time saver. Without implementing this second decision, it can be shown (see appendix) that the worst-case time complexity of Progol on a pharmacophore discovery problem (assuming a pharmacophore has at most 5 points) is $O(n^3cm^2p^5)$, where $n$ is the number of potential pharmacophoric points in the molecule with the fewest such points, $c$ is the number of conformations for this molecule, $m$ is the total number of conformations for all other molecules, and $p$ is the number of potential pharmacophoric points in the molecule with the most such points. Clearly this bound is polynomial but quite high. The experiment suggests that in practice the runtime is much lower than this worst-case bound. Finally, it is worth noting that large total numbers of molecules and conformations are not terribly damaging to this approach even in the worst case, since the algorithm's time complexity is linear in $m$. The most damaging number in the worst case is $p$, the number of potential pharmacophoric points in the molecule with the most such points. This number is particularly high when multiple hypothesized points, such as zinc sites, must be computed. To the extend that conclusions can be drawn from a worst-case bound, this bound indicates that pharmacophore discovery problems where hypothesized sites are unnecessary should lead to lower run times.

4. Scientific Contributions

The series of experiments described in this paper provide insights at four different levels. First, regarding Angiotensin-Converting Enzyme (ACE) inhibition the experiments confirm an earlier proposal, provide an alternative proposal, and suggest that no other alternatives exist within the constraints provided by the domain
expert. Second, they lead to a general methodology for pharmacophore discovery using Inuctive Logic Programming (ILP). Third, the experiments indicate that ILP can be used successfully to learn 3-dimensional concepts and to deal naturally with the multiple instance problem [6] (see Section 2.3.3). Fourth, the experiments support four lessons regarding knowledge discovery in general. We now discuss these contributions in further detail in reverse order, beginning with the most general contributions.

4.1. Lessons and Recommendations for Knowledge Discovery

4.1.1. Lesson 1: Rediscovery Step The first lesson from the experiments reported in this paper is the value of an initial rediscovery step when beginning work in a new problem domain. In the present work, Experiment 1 is an attempt to rediscover a proposed pharmacophore for ACE inhibition, given particular assumptions made by the original proponents. A rediscovery step is useful for at least two reasons. First, it builds the confidence of the domain expert. Even if the domain expert is not skeptical, a successful rediscovery can help to generate further enthusiasm about potential benefits. Second, a rediscovery step provides a thorough test of the encoding of domain or background knowledge. Both of the potential benefits of a rediscovery step can be fully achieved only if it is carried out as a “blindfold trial,” in which the users of the machine learning algorithm do not know the target concept. Experiment 1 in the present work was conducted as a blindfold trial. If a blindfold trial initially is unsuccessful, the failure may be due simply to bugs in the background knowledge. If so, this will be easier to determine with a test case where the domain expert knows what the answer should be than in a case of de novo discovery.

The use of blindfold trials is not original with this work. To our knowledge the first use of a blindfold trial in knowledge discovery by machine learning occurs in the work on meta-Dendral [4], where the task was to learn to identify particular organic compounds from within a family of compounds (e.g., estrogens) given their mass spectrometry readings. Although the authors do not explicitly state that their trials were blindfold trials, this seems evident given their discussion. Initial information (background knowledge) was elicited from experts and provided to meta-Dendral, and the expert was then asked to judge the acceptability of the meta-Dendral results. We suspect there are a number of other cases where blindfold rediscovery steps have been used, but they simply do not get discussed explicitly very often [26].

**Recommendation 1** We recommend further study into the efficacy of blindfold trials when beginning to apply machine learning to a new application domain. It is hoped that such study also will lead to recommendations regarding the best procedure to follow. For example, if the rediscovery step initially is unsuccessful, how should the researchers proceed? Also, should a new application begin with two rediscovery tasks, the first of which is not blindfold and is used to develop the approach, while the second is a blindfold test?
4.1.2. Lesson 2: Mismatch between ML Heuristics and Problem Domains  General purpose machine learning heuristics sometimes do not match particular problem domains. In the present work the MDL principle conflicts with chemists’ intuition that the most complex pharmacophore common to all active molecules is most likely to be correct, since it is the least likely to be present due to chance alone. The following three approaches can be taken when a mismatch occurs between general heuristics and a particular problem domain.

Wrapper  This is the approach taken in the present work. We have used the machine learning algorithm in a way that allows us to give preference to more complex pharmacophores. A wrapper can either be automatic, in the form of a program that repeatedly calls the machine learning algorithm, or manual, as in the present work.

Domain-specific Heuristic  An algorithm can be modified to make use of an alternative, domain-specific heuristic. More generally, machine learning systems can be built which allow a user to plug in domain-specific heuristics. These heuristics might modify how the search is done or might simply modify the scoring of hypotheses. For example Srinivasan and Camacho [30] describe an ILP algorithm that minimizes a user-defined cost function.

New General Heuristic  Work within one or more domains might cause an algorithm designer to see an alternative general-purpose heuristic that is better suited to a number of domains. For example Muggleton [22] recently has designed a heuristic that trades coverage of positive examples with specificity (measured according to a random, unlabeled data set). Desirable hypotheses have high coverage over the positive examples but relatively low coverage over the random data. It appears likely that use of this heuristic in place of MDL would eliminate the mismatch in the present work and possibly other problem domains, although this has not yet been tested.

Recommendation 2  We recommend further investigation into the mismatches that arise when applying general-purpose machine learning heuristics to new problem domains. Can the heuristics be improved to circumvent some such mismatches? Would we obtain better knowledge discovery systems if we allowed specialized problem-dependent heuristics to be specified for each new problem domain, or are there major benefits that come from committing a system to a general-purpose heuristic?

4.1.3. Lesson 3: Complete Search and Automatic Experiment Proposal  Many machine learning algorithms return a single hypothesis for a given set of data, even when other plausible hypotheses are available. In some cases it may be possible to encode user-defined criteria for acceptable hypotheses or to score hypotheses according to user-defined criteria. In such cases it can be advantageous to return multiple hypotheses that meet the given criteria or that achieve a high score. This occurs in the present paper, where two pharmacophores for ACE inhibition are
found. In addition, if the algorithm performs a complete search, it is possible to
assert that no other reasonable hypotheses exist, given the user’s criteria. When
multiple hypotheses are returned, however, we run the risk of providing a client
with too many solutions. It might be possible in such situations for the machine
learning algorithm to propose experiments that can distinguish between competing
hypotheses. For example, in the present work if the ILP system Progol had access
to a database of compounds, it potentially could search the database for compounds
possessing one but not both of the competing pharmacophores for ACE inhibition.
It could then propose testing one or more of these compounds for ACE inhibition,
to distinguish between the two competing pharmacophore hypotheses.

Recommendation 3  We recommend a research program to test the following
claim.

Claim: Automatic proposal of experiments by a machine learning system to dis-
tinguish between competing hypotheses is feasible for real-world applications.

4.1.4. Lesson 4: Declarative Knowledge Representation  Because of the nature
of ILP systems, the background knowledge we employed was largely declarative.
We consider it only “largely declarative” because even Prolog code can sometimes
be written in a less declarative, more procedural form. For example, one part of
our background knowledge computes potential sites for a zinc atom given the de-
scriptions of chemical groups that can bind to zinc. This portion of the background
knowledge is highly procedural, although written in Prolog, and includes code for
intersecting planes and spheres, for Gaussian elimination in 3 variables, etc. Fortunately,
writing and debugging this portion of the code did not require interaction
with the chemist. By contrast, the part of the background knowledge that defines
chemical groups that can bind to zinc was highly declarative, being almost a direct
translation of pictorial descriptions provided by the chemist. As a result, where am-
biguities or questions arose, or where debugging was necessary, these issues could
be addressed by actually going through that portion of the background knowledge
with the chemist. In addition to a declarative representation for background knowl-
dge, having a declarative representation for hypotheses made it a single day’s task
to write code both to translate hypotheses into English and to display molecules
with the pharmacophore highlighted.

The preceding discussion raises the point that expressions and portions of code
cannot be labeled declarative or non-declarative simply because of the representation
language employed. As a first attempt at an improved definition, which we hope
may stimulate further discussion, we propose the following.

Definition 1. A portion of code in some representation language is declarative
if it is isomorphic to a comprehensible expression in natural language.

To make crisp the notion of isomorphic, we require the existence of a translator
from the representation language into some natural language. The notion of com-
prehensible is inherently subjective, but an objective test could be achieved by (1)
asking a sample of people to read the natural language description and (2) testing their comprehension. Notice that with this formulation the relationship to natural language is a property of the representation language, whereas comprehensibility is a property of both the representation language (with its translation procedure) and the particular portion of code.

We have admitted that part of the background knowledge in the present work was not particularly declarative. Another shortcoming in the present work is in the declarative bias, or the specification of the form of acceptable hypotheses. This was declarative to the extent that it specified the form of Prolog clauses, but it could have been written in a more declarative style that described pharmacophores directly. We see improvement in the form of the declarative bias as an area for further work with Prolog in particular.

For machine learning systems that take explicit background knowledge (e.g. meta-Dendral, AQ [20], ILP systems), it is widely accepted that a substantial knowledge engineering effort often is required to encode this knowledge. But we believe that a substantial knowledge engineering effort is required for the application of many machine learning systems that do not take explicit background knowledge as input, such as decision tree learners. In the case of such algorithms, knowledge engineering issues still arise with code that users invariably write for precomputing various features. We believe that the value of a declarative representation applies to these types of machine learning algorithms as well, since developing the code that precomputes interesting domain-specific features may require a high degree of interaction with a domain expert.

**Recommendation 4** We recommend further study into the relative merits of declarative vs. non-declarative background knowledge. This investigation should not be limited to ILP systems; we believe it could involve all manner of machine learning systems. Such an investigation requires a carefully designed definition of declarative—it appears to be much easier to label pieces of code as “declarative” or “undeclarative” than to formulate a definitive set of criteria distinguishing between the two. In addition, we recommend further investigation into general kinds of background knowledge that might be re-usable across domains and across different types of learning algorithms, thus easing the burden of the knowledge engineering effort. For example, we hypothesize that background knowledge for geometric concepts might be useful across a wide variety of domains. Even more specific background knowledge, such as chemical knowledge, might apply to a variety of problem areas.

### 4.2. Lessons for Prolog Users and for ILP

The first lesson from the present work for ILP is that 3D concepts can be learned if geometry is represented logically by pairwise distances between points of interest. This could be useful in a variety of other domains as well, for example, machining of tools. It should be noted that as the geometric concepts grow more complex, additional detail may be necessary, for example, to capture orientation or to distinguish between mirror images.
The second lesson is that Progol, and probably other relational learning algorithms, can be used without modification to address the multiple instance problem (Section 2.3.3). The present work shows that the multiple instance problem can be addressed naturally within ILP, without the need to develop a new learning algorithm tailored to the problem and without the loss of information that comes from averaging over examples in a set. The general approach is based on an “instance” predicate. The following generic form for hypotheses for multiple instance problems can be used.

\[
\text{positive}(X) \leftarrow \text{instance}(X, Y), \text{pos-properties}(Y)
\]

A set \(X\) is asserted to be \(\text{positive}\) just if it has an instance \(Y\) such \(Y\) has the properties required for a label of \(\text{positive}\). For illustration, in the present work the variable \(X\) would stand for an example molecule under consideration, and the variable \(Y\) would stand for a conformation of that molecule. In some cases it may be possible to avoid the need for an explicit instance predicate by including both variables \(X\) and \(Y\) as arguments in the literal or literals describing the properties required for a \(\text{positive}\) label. This was done in the present work (Section 3.6).

Both Progol’s success with a 3D problem and its natural fit to the multiple instance problem depend on the first-order definite clause representation, rather than on the details of Progol itself. Therefore we expect that these properties would apply to a variety of other ILP systems as well. The obvious directions for further work are to apply ILP systems to other 3D problems and to other domains that exhibit the multiple instance problem.

### 4.3. Lessons for Pharmacophore Discovery

In addition to Progol’s general suitability to 3D concepts and the multiple instance problem, and its output of declarative hypotheses, Progol has one additional feature that makes it particularly effective for pharmacophore discovery. This feature is Progol’s focus on a “seed” positive example. The use of a seed example can eliminate many needless portions of a search space, particularly if the smallest or “simplest” example is chosen as the seed. For illustration, one type of atom that sometimes is of interest in a pharmacophore is a \textit{hydrogen donor}, for our purposes defined simply as a hydrogen bonded to an atom other than carbon. But in the present work the seed example actually had no hydrogen donors at all. As a result all hypotheses involving hydrogen donors were automatically omitted from the search.\(^4\) We expect that the use of a seed molecule is a general idea can be incorporated into other approaches to pharmacophore discovery as well in order to reduce their time complexities.

We believe the experiments described in Section 3 demonstrate the potential of relational learning in general and Progol in particular for pharmacophore discovery. We intend to apply the methodology detailed in Section 3 to other pharmacophore discovery problems, and to investigate the use of automatically-proposed experiments where multiple plausible pharmacophores are generated. We encourage other machine learning researchers to repeat our results with Progol, to apply their own
4.4. Lessons Regarding ACE inhibition

As is the case for many enzymes, it has not yet been possible to determine the binding site for ACE. Hence the question of the most likely pharmacophore for ACE inhibition remains open and of interest to researchers. The present work provides further confirmation for an earlier proposal by Mayer et al. [19], using energy-minimized conformations (according to Tripos’ Sybyl and Advanced Computation packages) and using ideal binding geometries for zinc. But the present work also proposes an alternative. Specifically, the alternative places the zinc site at a location more than one Angstrom closer to the triangle of hydrogen acceptors than does the original pharmacophore. Furthermore, given the assumptions provided by the chemists, no other potential pharmacophore exists.

There is no a priori reason to believe one of the proposed pharmacophores over the other. Subsequent to the experiments described in Section 3, we have tested eight additional ACE inhibitors published more recently [17]. These tests confirm our earlier results in that all eight new ACE inhibitors exhibit both pharmacophores. Unfortunately, the new test cases do not distinguish between the two pharmacophores. The reason it has been difficult to distinguish between the pharmacophores is that the binding geometries for chemical groups that can bind to zinc are symmetric. Every ACE inhibitor we have examined thus far has a chemical group which can bind to zinc either at a location oriented away from the triangle of hydrogen acceptors—and thus corresponding to the first pharmacophore—or oriented toward the hydrogen acceptors and corresponding to the second pharmacophore. It should be possible, though time-consuming, to carefully design and synthesize compounds with only one of the two pharmacophores, and then to test such compounds for ACE inhibition. We hope to do so as a first step into investigating the requirements for the automatic proposal of experiments within pharmacophore discovery.

5. Conclusion

This paper has presented a case study of a machine aided knowledge discovery process within the general area of drug design. Within drug design, the particular problem of pharmacophore discovery was isolated, and the ILP system Prolog was applied to the problem of identifying potential pharmacophores for ACE inhibition. The domain of pharmacophore discovery presented a natural “next step” beyond previous applications of ILP to structure-activity prediction within drug design. The case study reported in this paper supports four general lessons for knowledge discovery, as well as more specific lessons for pharmacophore discovery, for ILP, and for ACE inhibition. The general lessons for knowledge discovery are as follows.
1. An initial rediscovery step is a useful tool when approaching a new application domain.

2. General ML heuristics may fail to match the details of an application domain, but it may be possible to apply a heuristic-based algorithm in spite of the mismatch.

3. A complete search for all plausible hypotheses can provide useful information to a user, although experimentation may be required to choose between competing hypotheses.

4. A declarative knowledge representation facilitates the development and debugging of background knowledge in collaboration with a domain expert, as well as the communication of final results.

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Appendix Analysis of time complexity

In this section we present a worst-case analysis of the time complexity of Progol when running on the pharmacophore discovery problem. (An average-case analysis is an interesting goal for further work.) For clarity, we refer to the Progol algorithm tailored (via background knowledge) to this problem as the Progol-Pharmacophore, or PP, Algorithm. The analysis assumes that the maximum number of points in a pharmacophore is at most five.

For simplicity, the following analysis also assumes that the distances between all pairs of potential pharmacophoric points within all molecules have been precomputed. It is straightforward to show that this pre-computation can be done in time at most \(O(jk^2c)\), where \(j\) is the number of molecules in the data set, \(k\) is the maximum number of atoms in any molecule in the data set, and the constant \(c\) is the
size (number of atoms) of the largest pharmacophoric point of interest. Although in theory this pre-computation time can be greater than the pharmacophore discovery time, in practice the time for pre-computation typically is less than the time for pharmacophore discovery. A bound on the total time for the process can of course be obtained by summing the bound on pre-computation time and the bound on discovery time.

**Theorem 1** Assume that pharmacophores of interest have at most five points, and the distances between all pairs of pharmacophoric points within each molecule have already been computed. The Prolog-Pharmacophore (PP) Algorithm uses $O(n^3 c m^p)$ computation steps, where $n$ is the number of potential pharmacophoric points in the molecule with the fewest such points, $c$ is the number of conformations for this molecule, $m$ is the total number of conformations for all other molecules, and $p$ is the number of potential pharmacophoric points in the molecule with the most such points.

**Proof:** The PP Algorithm first identifies the molecule with the fewest pharmacophoric points (time $O(m p)$) and builds a bottom clause for it (time $O(cn)$). Call this molecule mol. For each conformation of mol and each triple of potential pharmacophoric points in this conformation of mol, the algorithm constructs a potential pharmacophore. There are $cn^3$ such potential pharmacophores. Each potential pharmacophore must be checked against all other conformations of all other molecules in the worst case. The number of checks is at most $m$, and the time to perform a check is $O(p^3)$, since all potential pharmacophoric points in a given conformation of a given molecule must be tried against the three points in the pharmacophore, in the worst case. Actually checking that the distances agree to within the specified tolerance can be done in constant time, given that all distances are pre-computed and given a standard Prolog indexing scheme.

In the next stage, four point pharmacophores are sought, and then five point pharmacophores. In each stage the analysis is the same as above, except that the exponents are incremented. This yields a total time bound of $O(cn^5 m p^5)$.

It is worth noting that the implementation actually used in the experiments reported in this paper first computed three-point pharmacophores and then used these to construct four point pharmacophores, etc. It can be shown that in the worst-case this approach requires time $O(cn^{12} m p^{12})$, although in practice it has proven to be significantly faster than the direct approach analyzed above. This observation suggests an average-case time complexity analysis as an important topic for further research.

Finally, we suspect that if the number of points in the target pharmacophore is unbounded, then the pharmacophore discovery problem is NP-hard. But this is an interesting question for further work. If one takes an idealized version of the problem, where the pairwise distances between potential pharmacophoric points in molecules do not have to obey geometric and chemical laws, then one can show the problem is NP-hard by a reduction from the maximum clique problem. But the reduction requires constructing two idealized molecules for any given graph, and it is unclear that the molecules so constructed obey geometric and chemical laws.
Notes

1. The term ligand is used for molecules which bind to the protein binding site. A ligand may be highly active against a target, but might not a “drug,” because of a lack of other required properties such as metabolic stability (wont be broken down within the body), safety (a ligand may be toxic), or an ability to diffuse from the gut into the bloodstream if a requirement is that the drug can be taken by mouth.

2. The experiments reported in this paper were run using the Prolog version of Progol, P- Progol 2.3. This and a C version of Progol are available by anonymous ftp to the site ftp: coulibox.ac.uk in the directory pub/Packages/JLP.

3. Two molecules are stereoisomers if they have the same atom and bond structure but different 3D arrangements, and it is not possible to convert from one to the other without breaking a bond.

4. We simply chose the first example supplied by the chemist as the seed example, and it was fortuitous that this happened to be one of the smaller molecules and to have no hydrogen donors. But a program could be written to examine a data set initially and select a seed example that is likely to yield a reduced search.

References


