## Computer Systems - Architecture Tutorial 2 - Representations of Integers

1. Convert 188 into binary, octal and hexadecimal.
2. Convert $\mathrm{ABC}_{16}$ into binary, octal and decimal.
3. Add the following two 20-bit binary numbers. Spaces embedded in the numbers are for readability only.

| 1st number | 1111 | 0000 | 1111 | 0000 | 1111 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2nd number | 1010 | 1010 | 1011 | 1111 | 1111 |

4. Using the two numbers in question 3, subtract the second binary number above from the first.
5. What is the square of $10101{ }_{2}$ in base 2 ?
6. What is 145 in base 1 (Unary) ?
7. How many natural numbers can be represented by
(i) 8 -bits
(ii) 10 -bits
(iii) 16-bits
8. For an 8-bit group, work out the representation for $-37{ }_{10}$ in
(i) sign \& magnitude
(ii) one's complement
(iii) two's complement
(iv) excess- 256
(v) excess-128
9. For a 10-bit group, what range of integers can be represented using
(i) sign \& magnitude
(ii) one's complement
(iii) two's complement
(iv) excess-512
10. Subtract the following 12-bit two's complement numbers (2nd from 1st)

$$
101010101011
$$

$-\underline{101100001101}$
What is the result in decimal?
12. Express $98765_{10}$ in binary coded decimal (BCD)
13. Translate the following 6-character string $\mathrm{A}:=\mathrm{q}^{*} \mathrm{t}$ to 8 -bit ASCII codes (List your codes as binary and hex values).

## Solutions

This page is upside down to discourage you from peeking.
Remember to show your working and to carry out your conversions and calculations without a calculator.

1. $\quad 188_{10}=1011_{-} 1100_{2}=274_{8}=\mathrm{BC}_{16}$
2. $\quad \mathrm{ABC}_{16}=1010 \_1011_{-} 1100_{8}=5274_{8}=2748_{10}$
3. $\operatorname{Sum}=1 \_1001 \_1011 \_1011 \_0000 \_1110$
4. $\quad$ Diff $=$ 0100_0110_0011_0001_0000
5. $\quad$ Square $=1 \_1011 \_1001$
6. $1_{-1111_{-} 1111_{1}}$
7. 

(i) $2^{8}=256, \quad$ (ii) $2^{10}=1024$, (iii) $2^{16}=65536$
8. (i) 1010_0101, (ii) 1101_1010, (iii) 1101_1011, (iv) 1101_1011, (v) 0101_1011
9. (i) -511 to +511 , (ii) -511 to +511 , (iii) -512 to +511 , (iv) -512 to +511
10. 1111_1001_1110 = decimal -98
11. 1001_1000_0111_0110_0101
12.

| Char | A | : | = | q | * | t |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Binary | 01000001 | 00111010 | 00111101 | 01110001 | 00101010 | 01110100 |
| Hex | 41 | 3 A | 3 D | $7 \quad 1$ | 2 A | 74 |

