Dr Bernhard Kainz b.kainz@imperial.ac.uk

Huxley 372

Intro

https://www.youtube.com/watch?v=wAu8w7n4LHM

- Please note that this course has been timetabled for 2 hours per week:
 - Tuesday 9-10, Zoom
 - Wednesday 9-10, MS Teams
- However, not all timetabled slots will be used every week so <u>please check the timetable</u> on the webpage for more information:

http://wp.doc.ic.ac.uk/bkainz/teaching/60005-co317-computergraphics/

- Printouts:
 - Lecture notes & tutorials:
 - Please print your own if you want a hardcopy
- Lectures:
 - All lectures have slides that are available via CATE
 - Some lectures (not all) have notes that are available via CATE
 - Lectures are pre-recorded, we will have a weekly Q&A session
- Tutorials:
 - All tutorials have sample solutions that are available a few days after the tutorial.

- Course overview:
 - Syllabus, timetable and news on

http://wp.doc.ic.ac.uk/bkainz/teaching/60005-co317-computergraphics/

- See notes on vector algebra revision (link)

- Course materials and notes:
 - Look at CATE for lecture notes, tutorials & coursework

Information for non DOC students

- Apply at https://dbc.doc.ic.ac.uk/externalreg/
- Your department's endorser will approve/reject your application
 - No access after a few days? Check status of approval and contact relevant person(s)
- Key Dates:
 - Exam registration opens end January for 2-3 weeks
 - Exams for DoC 3rd/4th year courses take place at the end of the Term in which the course is taught – courses that are co-scheduled on the time-table will have their exams co-scheduled
- If in doubt, read the guidelines available at the link above

Courseworks

- There will be six practical coursework tasks; three of them are assessed:
 - Task 1: Framework
 - Task 2: Transformations
 - Task 3: Illumination (assessed 40%)
 - Task 4: Color
 - Task 5: Texture & Render to Texture (assessed 10%)
 - Task 6: GPU ray tracing (50%)
- All practical courseworks require programming experience (very basic C)

Logistics

- 6 tasks, 3 assessed
 - 1-5 One per week
 - Task 6: 2 weeks
- Description and framework already available for all exercises, but
- Necessary knowledge in each lecture per week
- Submission electronically via CATE!

Effects previous year's SOLE and COVID-19

- Redesigned the coursework to better match the content of the lectures in each week
- Made the framework available to everybody through a browser implementation (no computing lab requirement anymore)
- Provide an open-source implementation of a custom OpenGL GLSL IDE
- Reduced the workload to three assessed tasks, revising assessment. Tasks 1,2,4 are voluntary. Removed one task that was not supported by all OpenGL versions
- One exam question will be based on what you learned during the coursework!
- Re-implemented the framework for the coursework for a second time:
 - It is now the most advanced teaching framework for computer graphics
- Everybody can use it now from their own laptops without needing to install anything: <u>http://shaderlabweb.doc.ic.ac.uk/</u>
- We listened to your SOLE feedback from the last years!
 - Please fill in SOLE at the end of this course!

CSL and TAs

- Course support leader:
 - Benjamin Hou benjamin.hou11@imperial.ac.uk
 - Samuel Budd
 - Hadrien Reynaud
 - Miguel Monteiro

Labs in 202 & 206

- Week 3: Wednesday 9-10
- Week 4: Wednesday 9-10
- Week 6: Wednesday 9-10
- Week 8: Wednesday 9-10

framework

http://shaderlabweb.doc.ic.ac.uk/

starting the framwork

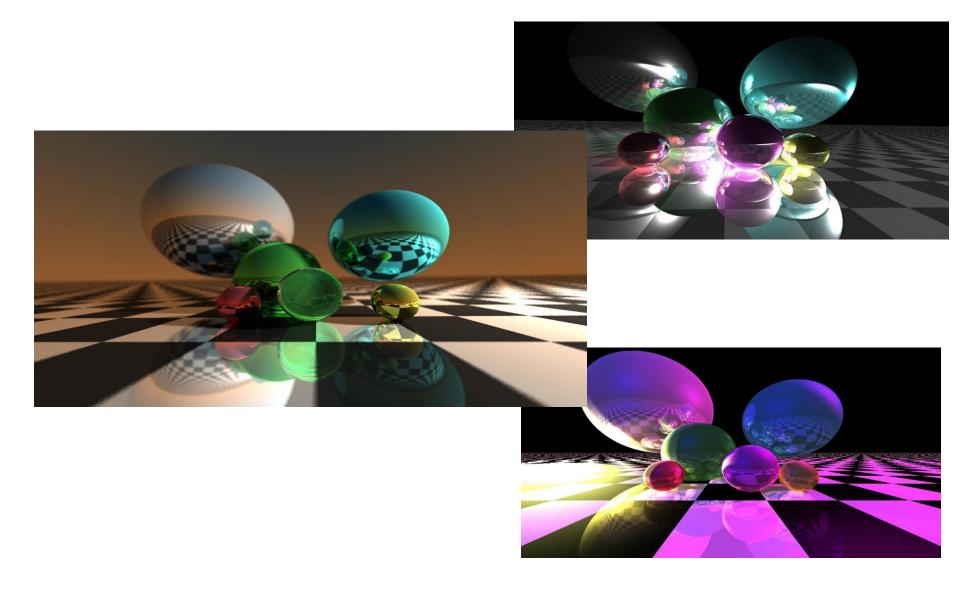
- Open a browser (preferably Chrome)
- Enter http://shaderlabweb.doc.ic.ac.uk/

Tasks

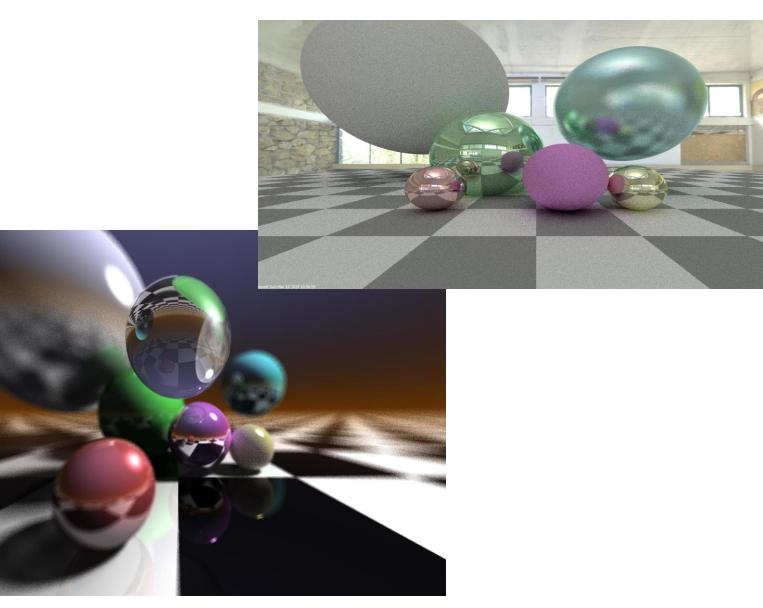
• Task 1: Get familiar with the framework

	fi	ramebuffer 🔶 So	creen size render quad	
		^	↓	
Save/load json files	Vertex shader 🔶 Frag	gment shader	Vertex shader	→ Fragment shader
ShaderLabWeb Save State Load Sta	ite	\sim .		Imperial College London
Log Camera Model Uniforms 122945.030 122	Base Pase. Comple & Link Bhaders	<pre>1 attribute vec3 vertex_wor 2 attribute vec3 nermal_wor 3 attribute vec3 texturdeo 4 uniform mat4 mMatrix; 6 uniform mat4 mMatrix; 7 uniform mat4 pMatrix; 8 varying vec3 normal; 10 void main() {</pre>	lošpace; ndinate_input; vMatrix * aMatrix * vec4(vertex_worldipace, 1.0); vertex_cam5pace;	
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		☑ Link to program		

Student solutions



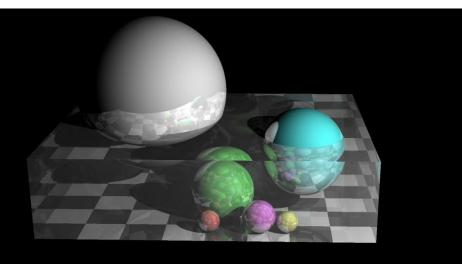
Student solutions



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Student solutions









Have fun!

Interactive Computer Graphics: Lecture 1

3D graphical scenes: Projections and Transformations

Two dimensional graphics

- The lowest level of graphics processing operates directly on the pixels in a window provided by the operating system.
- Typical Primitives are:

SetPixel(int x, int y, int colour); DrawLine(int xs, int ys, int xf, int yf);

• etc.

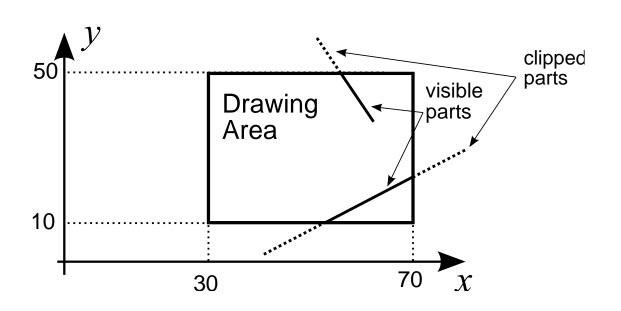
World coordinate systems

- To achieve *device independence* when drawing objects we can define a **world coordinate system.**
- This will define our drawing area in units that are suited to the application:
 - meters
 - light years
 - microns
 - etc



We can give our window 'World Coordinates' and draw objects using them.

SetWindow(30, 10, 70, 50) DrawLine(40, 3, 90, 30) DrawLine(50, 60, 60, 40)



To make the conversion

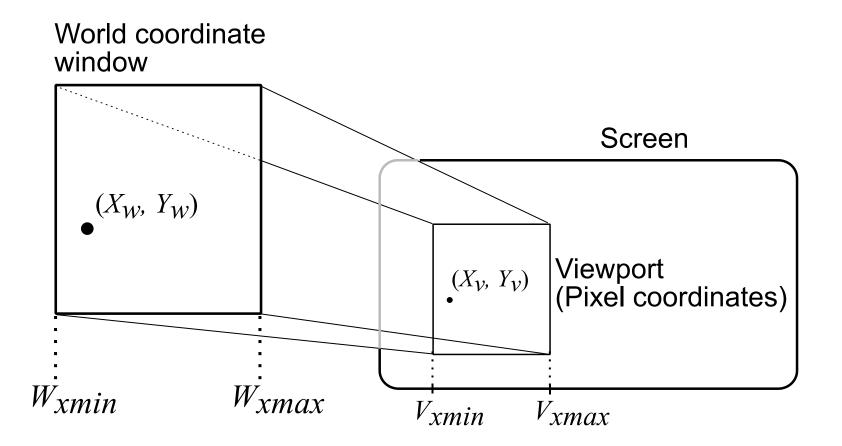


we need a process of normalisation

First we must ask the operating system* for the pixel addresses of the corners of the area we are using.

Then we can translate our world coordinates to pixel coordinates.

*making a 'system call' through the API



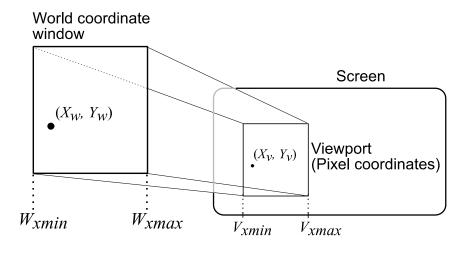
• Having defined our world coordinates, and obtained our device coordinates we relate the two by simple ratios:

$$\frac{(X_w - W_{xmin})}{(W_{xmax} - W_{xmin})} = \frac{(X_v - V_{xmin})}{(V_{xmax} - V_{xmin})}$$

• Rearranging, we get:

$$X_v = \frac{(X_w - W_{xmin})(V_{xmax} - V_{xmin})}{W_{xmax} - W_{xmin}} + V_{xmin}$$

• with a similar expression for *Y_v*



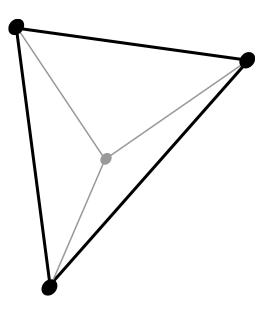
- So we have two equations for calculating pixel coordinates (X_{ν}, Y_{ν}) .
- We can simplify them to form a simple pair of linear equations:

 $X_v = AX_w + B$ $Y_v = CY_w + D$

• Here *A*, *B*, *C* and *D* are constants that define the normalisation. *A*, *B*, *C*, *D* are found from the known values of W_{xmin} , V_{xmin} , ...

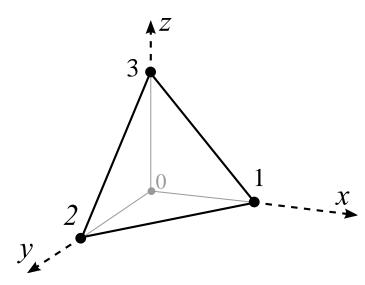
Polygon rendering

- Many graphics applications use scenes built out of planar polyhedra.
- These are three dimensional objects whose faces are all planar polygons (often called <u>faces</u> or <u>facets</u>).



Representing planar polygons

- In order to represent planar polygons in the computer we need a mixture of different data:
 - Numerical Data
 - Actual 3D coordinates of vertices, etc.
 - Topological Data
 - · Details of what is connected to what.

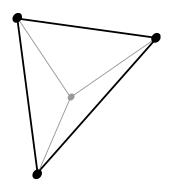


Vertex data		
Index	Location	
0	(0, 0, 0)	
1	(1, 0, 0)	
2	(0, 1, 0)	
3	(0, 0, 1)	

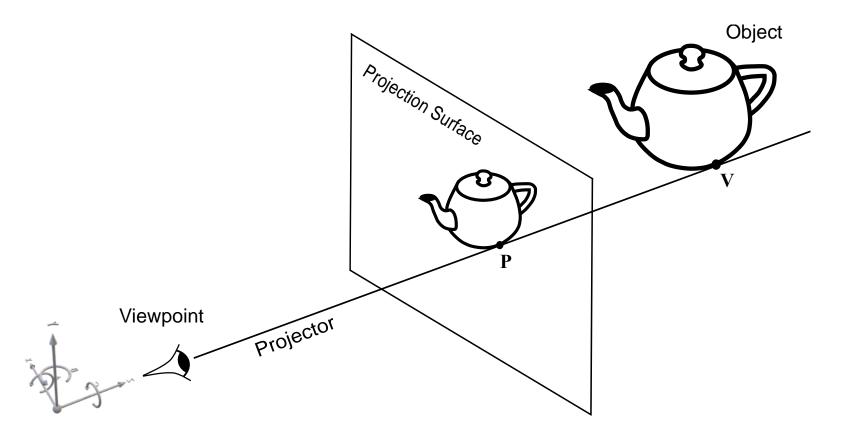
Face data			
Index	Vertices		
0	013		
1	021		
2	032		
3	123		

Projections of wire frame models

- Wire frame models simply include points and lines.
- In order to draw a 3D wire frame model we must:
 - First convert the points to a 2D representation.
 - Then we can use simple drawing primitives to draw them.
- The conversion from 3D into 2D is a projection.



Projection



The projector takes a point on the object to a point on 2D projection surface.

Non-linear projections

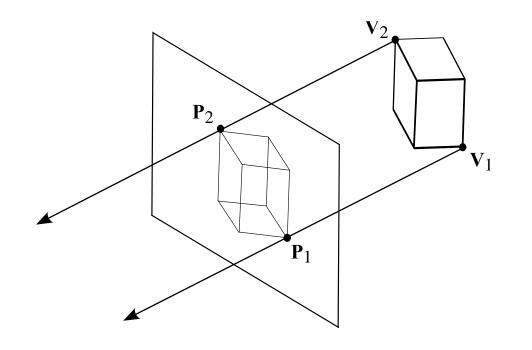
- In general it is possible to project onto any surface:
 - Sphere
 - Cone
 - Etc.
- or to use curved projectors, for example to produce lens effects.
- But we will only consider linear projections onto a flat (planar) surface.

Orthographic projection

- This is the simplest form of projection, and effective in many cases.
- Make simplifying assumptions:
 - The viewpoint is at $z = -\infty$
 - The plane of projection is z = 0
- So all projectors have the same direction:

$$\mathbf{d} = \left(\begin{array}{c} 0\\ 0\\ -1 \end{array}\right)$$

Orthographic projection onto z = 0



Each projection line has equation

$$\mathbf{P} = \mathbf{V} + \mu \, \mathbf{d}$$

where

$$\mathbf{d} = \left(\begin{array}{c} 0\\ 0\\ -1 \end{array}\right)$$

Calculating an orthographic projection

• Substitute $\mathbf{d} = (0, 0, -1)^{T}$ into the projector vector equation:

$$\mathbf{P} = \mathbf{V} + \mu \mathbf{d}$$

• Gives Cartesian equations for each component

$$P_x = V_x + 0 \qquad P_y = V_y + 0 \qquad P_z = V_z - \mu$$

• Projection plane is $z = 0 \Rightarrow P_z = 0$

Calculating an orthographic projection (cont.)

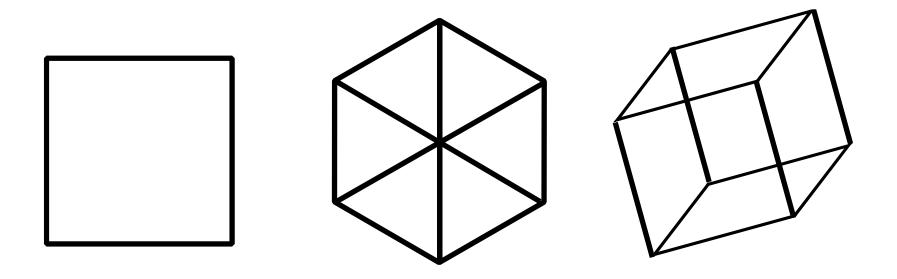
• So the projected location on the screen is

$$\mathbf{P} = \begin{pmatrix} Vx\\Vy\\0 \end{pmatrix}$$

• i.e. we simply take the 3D *x* and *y* components of the vertex!

Orthographic projections of a cube

• Looking at a face, a vertex and a more general view...



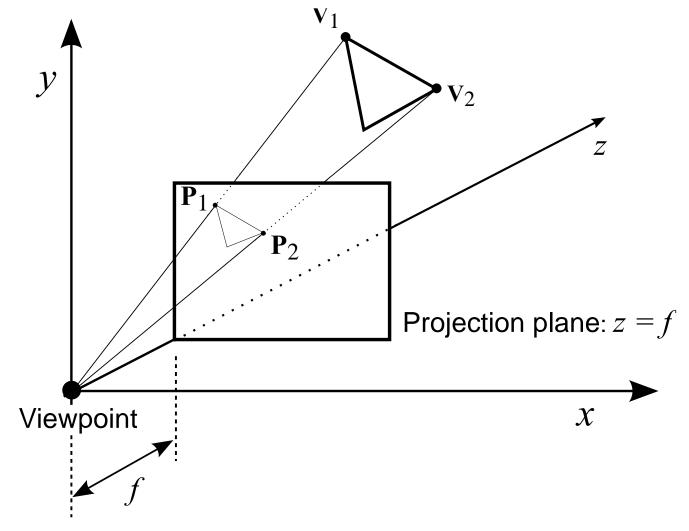
Perspective projection

• Orthographic projection is fine in cases where we are not worried about depth

- e.g. when most objects are at the same distance from the viewer

- However, for close work particularly computer games it will not do.
- Instead, we use *perspective projection*.

Canonical form for perspective projection



Calculating perspective projection

The perspective projector equation from vertex ${\bf V}$ is

$$\mathbf{P} = \mu \mathbf{V}$$

because all projectors go through the origin. At the projected point we have $P_z = f$.

Let the value of μ at this point be μ_p

$$\mu_p = P_z/V_z = f/V_z$$

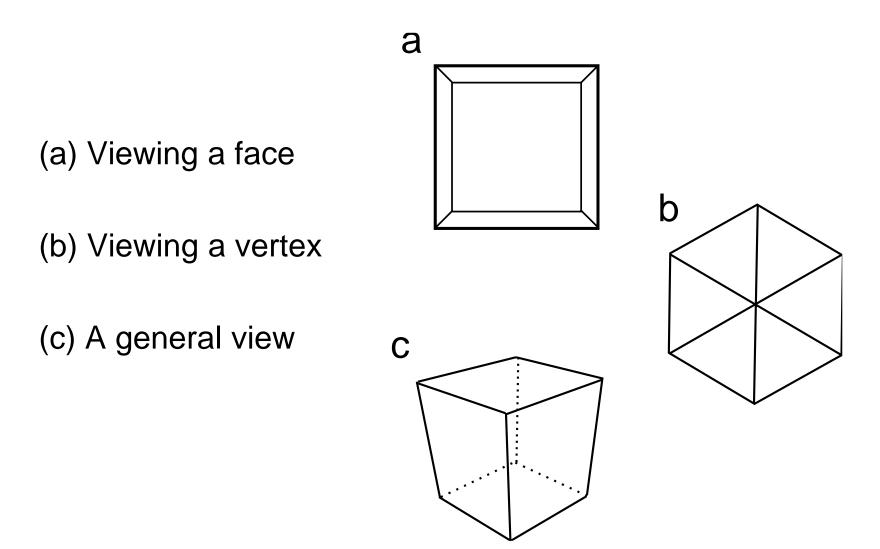
and

$$P_x = \mu_p V_x \,, \quad P_y = \mu_p V_y$$

Therefore

$$P_x = fV_x/V_z , \quad P_y = fV_y/V_z$$

Perspective projections of a cube



Problem break

Given that the viewing plane is at z = 5, what point on the view plane corresponds to the 3D vertex

$$\mathbf{V} = \begin{pmatrix} 10\\10\\10 \end{pmatrix}$$

when we use the different projections:

- 1. Perspective
- 2. Orthographic

Problem break

Given that the viewing plane is at z = 5, what point on the view plane corresponds to the 3D vertex

$$\mathbf{V} = \begin{pmatrix} 10\\10\\10 \end{pmatrix}$$

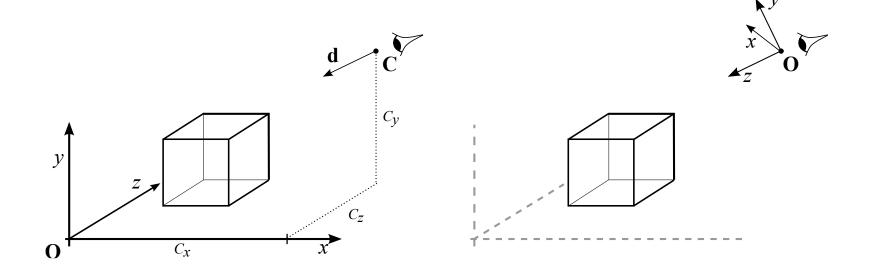
when we use the different projections:

- 1. Perspective $P_x = fV_x/V_z = 5$ and $P_y = fV_y/V_z = 5$
- 2. Orthographic $P_x = 10$ and $P_y = 10$

The need for transformations

- Graphics scenes are defined in a particular coordinate system.
- We want to draw a graphics scene from any angle
- **<u>But</u>** to draw a graphics scene, it is a lot easier to have:
 - The viewpoint at the origin
 - The *z*-zaxis as the direction of view
- Hence, we need to be able to transform the coordinates of a graphics scene.

Transformation of viewpoint



Before transformation

After transformation

Other transformations

- We also need transformations for other purposes:
 - Animating Objects
 - e.g. flying titles, rotating, shrinking etc.
 - Multiple Instances
 - the same object may appear at different places or different
 - sizes
 - Reflections and other special effects

Matrix transformations of points

To transform points we use matrix multiplications, e.g. to make an object at the origin twice as big we could use:

$$\begin{pmatrix} x'\\y'\\z' \end{pmatrix} = \begin{pmatrix} 2 & 0 & 0\\0 & 2 & 0\\0 & 0 & 2 \end{pmatrix} \begin{pmatrix} x\\y\\z \end{pmatrix}$$

which, when multiplied out, gives:

$$x' = 2x \quad y' = 2y \quad z' = 2z$$

Translation by matrix multiplication

• Many of our transformations will require translation of the points. For example if we want to move all the points two units along the *x*-axis we would require

$$\begin{array}{rcl}
x' &=& x+2\\ y' &=& y\\ z' &=& z\end{array}$$

• But how can we do this with a matrix? I.e.

$$\begin{pmatrix} & ? \\ & \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} x+2 \\ y \\ z \end{pmatrix}$$

... can't be done

Homogenous coordinates

- The answer is to use 4D homogenous coordinates.
- They have a 4th ordinate allowing us to use the last column for translation

$$\begin{pmatrix} x'\\y'\\z'\\1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 2\\ 0 & 1 & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x\\y\\z\\1 \end{pmatrix}$$

• which, when multiplied out, gives:

$$x' = x + 2 \quad y' = y \quad z' = z$$

General homogenous coordinates

- In most cases the last ordinate will be 1
- But in general, it is a scale factor.

Homogeneous Cartesian $(p_x, p_y, p_z, s) \iff \left(\frac{p_x}{s}, \frac{p_y}{s}, \frac{p_z}{s}\right)$

Affine transformations

- Affine transformations are those that preserve parallel lines.
- Most transformations we require are affine, the most important being:
 - Scaling
 - Rotation
 - Translation
- Other more complex transforms can be built from these.
- An example of a non-affine transformation:
 - Perspective projection (parallels not preserved).

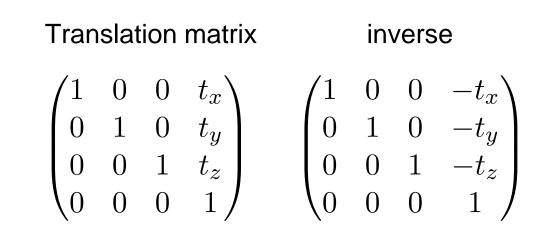
Translation with a matrix

• We can apply a general translation by (t_x, t_y, t_z) to the points of a scene by using the following matrix multiplication

$$\begin{pmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} p_x \\ p_y \\ p_z \\ 1 \end{pmatrix} = \begin{pmatrix} p_x + t_x \\ p_y + t_y \\ p_z + t_z \\ 1 \end{pmatrix}$$

Inverting a translation

• Since we know what a translation matrix physically does, we can write down its inversion directly, e.g.



Can you show that the product of these matrices is the identity?

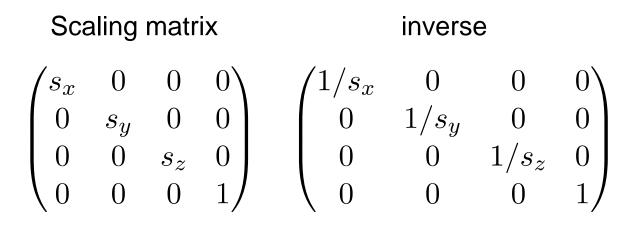
Scaling with a matrix

- Scaling simply multiplies each ordinate by a scaling factor.
- It can be done with the following homogenous matrix:

$$\begin{pmatrix} s_x & 0 & 0 & 0\\ 0 & s_y & 0 & 0\\ 0 & 0 & s_z & 0\\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} p_x \\ p_y \\ p_z \\ 1 \end{pmatrix} = \begin{pmatrix} s_x p_x \\ s_y p_y \\ s_z p_z \\ 1 \end{pmatrix}$$

Inverting a scaling

• To invert a scaling we simply divide the individual ordinates by the scale factor.



Combining transformations

- Suppose we want to make an object centred at the origin twice as big and then move it so that the centre is at (5, 5, 20).
- The transformation is a scaling followed by a translation:

$$\begin{pmatrix} x'\\y'\\z'\\1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 5\\0 & 1 & 0 & 5\\0 & 0 & 1 & 20\\0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 2 & 0 & 0 & 0\\0 & 2 & 0 & 0\\0 & 0 & 2 & 0\\0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x\\y\\z\\1 \end{pmatrix}$$

Combined transformations

- We can multiply out the transformation matrices
- This gives us a single matrix which we can use to apply both transformations to any point

$$\begin{pmatrix} x'\\y'\\z'\\1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 0 & 5\\0 & 2 & 0 & 5\\0 & 0 & 2 & 20\\0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x\\y\\z\\1 \end{pmatrix}$$

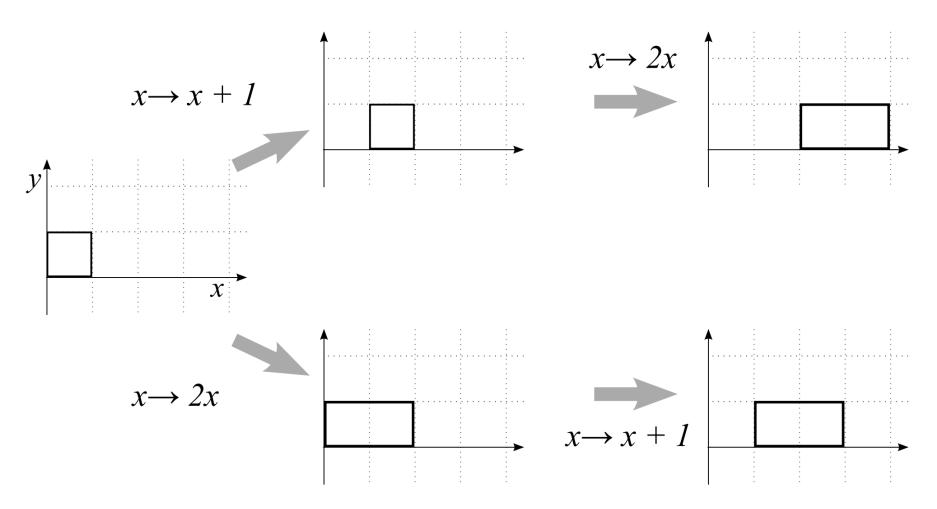
Careful: Transformations are not commutative

- The order of applying transformations matters:
- In general

$T \bullet S$ is not the same as $S \bullet T$

• Check this for the transformation matrices on the last two slides

The order of transformations is significant



The results at the end of each route are different.

Graphics Lecture 1: Slide 60

Rotation

- To define a rotation, we need an axis and an angle.
- The simplest rotations are about the Cartesian axes.
- For example:

 $-R_{v}$

 $-R_{z}$

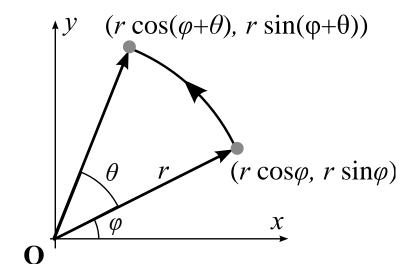
- $-R_x$ Rotate about the *x*-axis
 - Rotate about the y-axis
 - Rotate about the *z*-axis

Rotation matrices

By θ about each of the axes

$$\mathcal{R}_{x} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$
$$\mathcal{R}_{y} = \begin{pmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$
$$\mathcal{R}_{z} = \begin{pmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Example: Derivation of \mathcal{R}_{T}



z-axis goes into page

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} r \cos \varphi \\ r \sin \varphi \end{pmatrix}$$

$$\rightarrow \begin{pmatrix} r \cos(\varphi + \theta) \\ r \sin(\varphi + \theta) \end{pmatrix}$$

$$= \begin{pmatrix} r \cos \varphi \cos \theta - r \sin \varphi \sin \theta \\ r \cos \varphi \sin \theta + r \sin \varphi \cos \theta \end{pmatrix}$$

$$= \begin{pmatrix} x \cos \theta - y \sin \theta \\ x \sin \theta + y \cos \theta \end{pmatrix}$$

$$= \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$\downarrow \qquad \downarrow$$

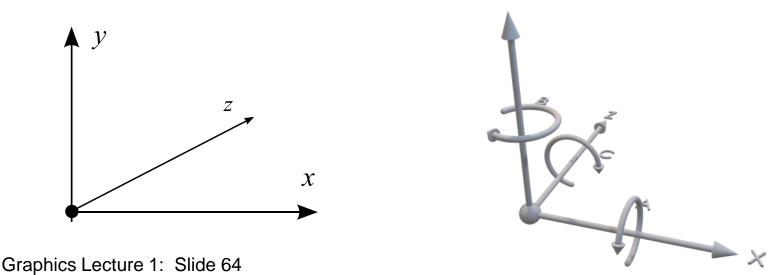
$$\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$\downarrow \qquad \downarrow$$

$$\begin{pmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Rotations have a direction

- Note the following about the matrix formulations given in these notes:
 - We will stick to a left-handed coordinate system
 - Rotation is anti-clockwise when looking along the axis of rotation (in the previous slide, the z-axis goes into the page).
 - Rotation is clockwise when looking back towards the origin from the positive side of the axis



Inverting rotation

Inverting a rotation by angle θ



Rotating through angle $-\theta$

•i.e. we can use the following relations to help us find the inverse of a rotation:

 $\cos(-\theta) = \cos(\theta)$ and $\sin(-\theta) = -\sin(\theta)$

Inverting rotation

• So for example:

RotationInverse $\mathcal{R}_z(\theta)$ $\mathcal{R}_z(-\theta)$ $\begin{pmatrix} \cos \theta & -\sin \theta & 0 & 0\\ \sin \theta & \cos \theta & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{pmatrix}$ $\begin{pmatrix} \cos \theta & \sin \theta & 0 & 0\\ -\sin \theta & \cos \theta & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{pmatrix}$