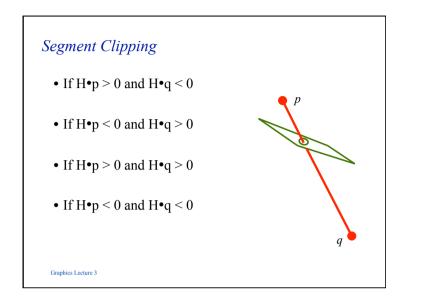
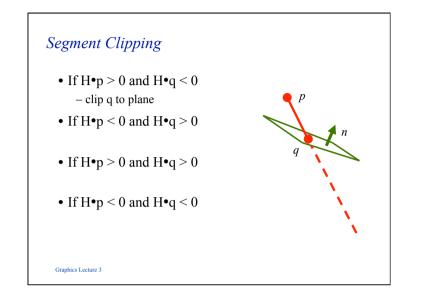


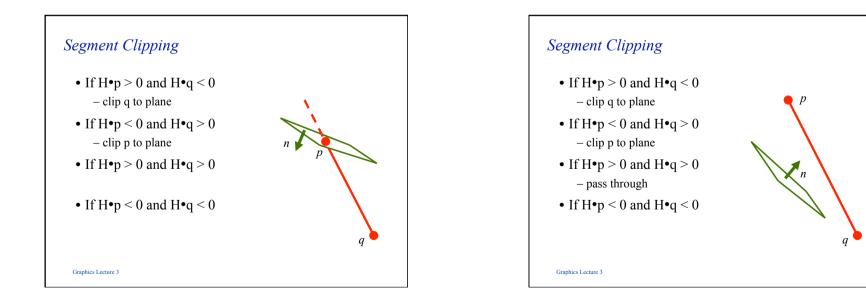
### *Line – Plane Intersection*

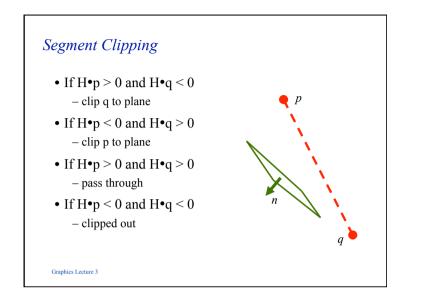
- Compute the intersection between the line and plane for any vector p lying on the plane n•p = 0
- Let the intersection point be  $\mu p_1 + (1-\mu)p_0$  and assume that v is a point on the plane, a vector in the plane is given by  $\mu p_1 + (1-\mu)p_0 - v$
- Thus  $\mathbf{n} \cdot (\mu \mathbf{p}_1 + (1-\mu)\mathbf{p}_0 \mathbf{v}) = 0$  and we can solve this for  $\mu_i$  and hence find the point of intersection
- We then replace  $\mathbf{p}_0$  with the intersection point

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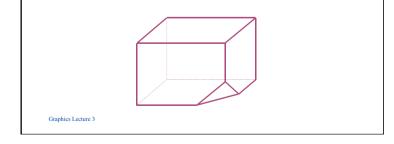


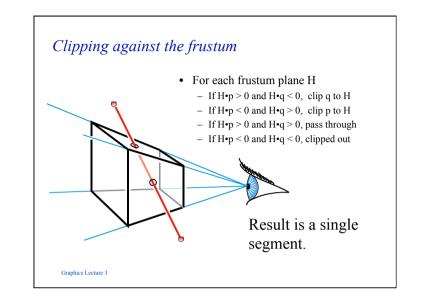


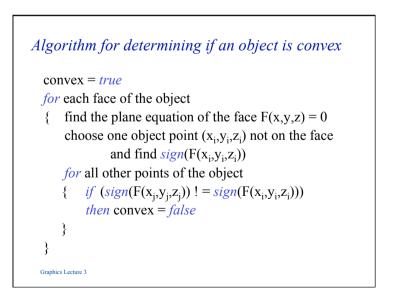


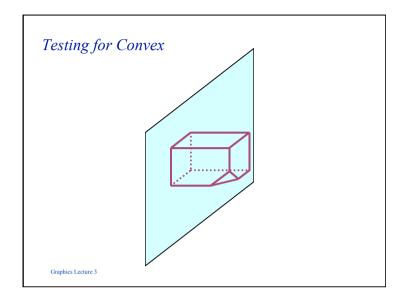


- 1. A line joining any two points on the boundary lies inside the object.
- 2. The object is the intersection of planar halfspaces.

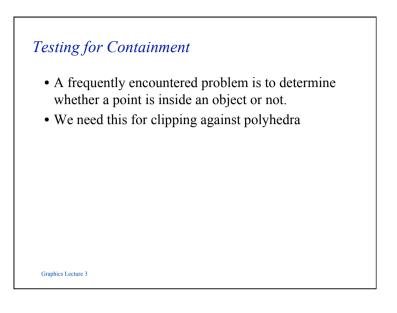








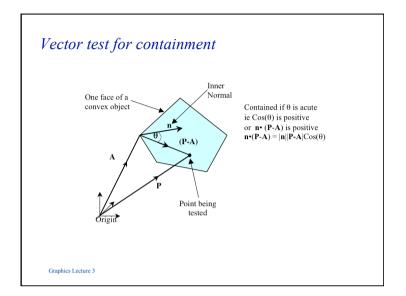
# Algorithm for Containment let the test point be $(x_t, y_t, z_t)$ contained = true for each face of the object { find the plane equation of the face F(x,y,z) = 0choose one object point $(x_i, y_i, z_i)$ not on the face and find $sign(F(x_i, y_i, z_i))$ if $(sign(F(x_t, y_t, z_t)) != sign(F(x_i, y_i, z_i)))$ then contained = false } Graphics Letter 3

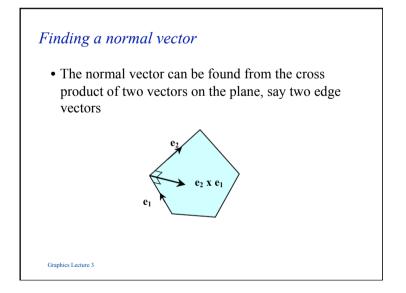


### Vector formulation

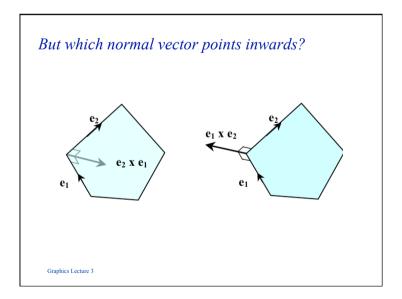
- The same test can be expressed in vector form.
- This avoids the need to calculate the Cartesian equation of the plane, if, in our model we store the normal **n** vector to each face of our object.

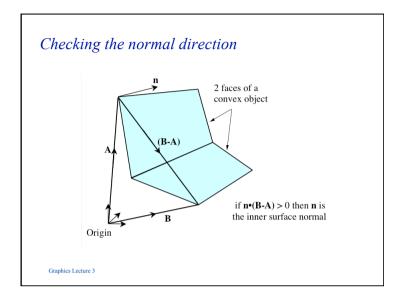
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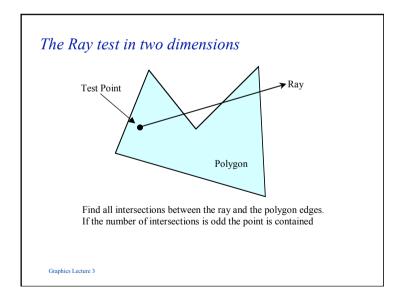


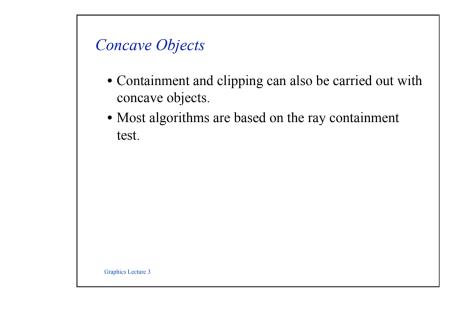


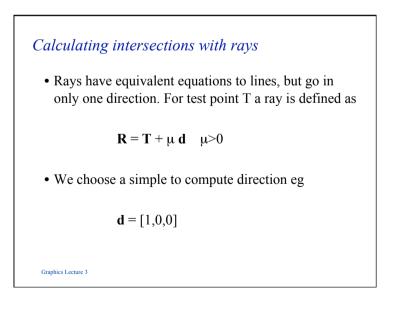
# **Normal vector to a face** • The vector formulation does not require us to find the plane equation of a face, but it does require us to find a normal vector to the plane; same thing really since for plane Ax + By + Cz + D = 0 a normal vector is n = (A, B, C)

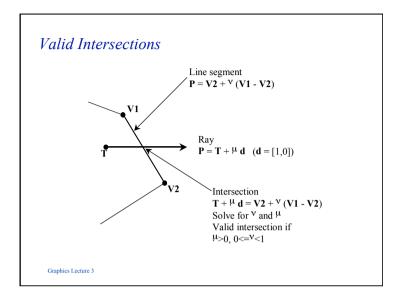






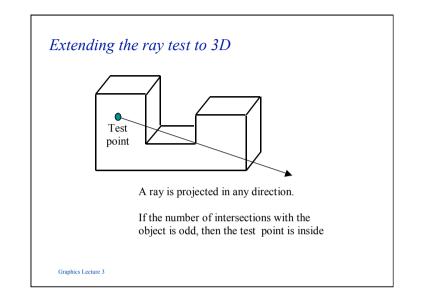








- There are two stages:
  - 1. Compute the intersection of the ray with the plane of each face.
  - 2. If the intersection is in the positive part of the ray ( $\mu$ >0) check whether the intersection point is contained in the face.



## *The plane of a face*

- Unfortunately the plane of a face does not in general line up with the Cartesian axes, so the second part is not a two dimensional problem.
- However, containment is invariant under orthographic projection, so it can be simply reduced to two dimensions.

Graphics Lecture 3

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