



Rasterization

- Determine which pixels are drawn into the framebuffer
- Interpolate parameters (colors, texture coordinates, etc.)











| Barycentric coordinates |
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| • Barycentric coordinates describe a point p as an affine combination of the triangle vertices |
| $\mathbf{p}(\alpha,\beta,\gamma) = \alpha \mathbf{a} + \beta \mathbf{b} + \gamma \mathbf{c}$ $\alpha + \beta + \gamma = 1$ |
| For any point p inside the triangle (a, b, c): 0 < α < 1 0 < β < 1 |
| $0 < \gamma < 1$ |
| • Point on an edge: one coefficient is 0 |
| • Vertex: two coefficients are 0, remaining one is 1 |
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Edge equations

- Given a triangle with vertices (x_a, y_a) , (x_b, y_b) , and (x_o, y_2) .
- The line equations of the edges of the triangle are:

$$f_{ab}(x,y) = (y_a - y_b)x + (x_b - x_a)y + x_ay_b - x_by_a$$

$$f_{bc}(x,y) = (y_b - y_c)x + (x_c - x_b)y + x_by_c - x_cy_a$$

$$f_{ca}(x,y) = (y_c - y_a)x + (x_a - x_c)y + x_cy_a - x_ay_c$$





- Remember that: $f(x,y) = 0 \Leftrightarrow kf(x,y) = 0$
- A barycentric coordinate (e.g. β) is a signed distance from a line (e.g. the line that goes through **ac**)
- For a given point **p**, we would like to compute its barycentric coordinate β using an implicit edge equation.
- We need to choose k such that $kf_{ac}(x,y) = \beta$

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Barycentric Coordinates

• In general, the barycentric coordinates for point **p** are:

$$\alpha = \frac{f_{bc}(x,y)}{f_{bc}(x_c,y_c)} \qquad \beta = \frac{f_{ac}(x,y)}{f_{ac}(x_b,y_b)} \qquad \gamma = 1 - \alpha - \beta$$

• Given a point **p** with cartesian coordinates (*x*, *y*), we can compute its barycentric coordinates (α, β, γ) as above.

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Barycentric Coordinates

- We would like to choose k such that: $kf_{ac}(x,y) = \beta$
- We know that $\beta = 1$ at point **b**:

$$kf_{ac}(x,y) = 1 \Leftrightarrow k = \frac{1}{f_{ac}(x_b,y_b)}$$

• The barycentric coordinate β for point **p** is:

$$\beta = \frac{f_{ac}(x, y)}{f_{ac}(x_b, y_b)}$$

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Triangle Rasterization

- Many different ways to generate fragments for a triangle
- Checking (α, β, γ) is one method, e.g.
 (0< α <1 && 0< β <1 && 0< γ <1)
- In practice, the graphics hardware use optimized methods:
 - fixed point precision (not floating-point)
 - incremental (use results from previous pixel)
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Triangle Rasterization

• We can use barycentric coordinates to rasterize and color triangles

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• The color c varies smoothly within the triangle
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Visibility: Two triangles

- Things get more complicated with multiple triangles
- Fragments might overlap in screen space!

















• Example:

– fragment from green triangle has z value of 0.7







The Z-Buffer Algorithm

- Let CB be color (frame) buffer, ZB be zbuffer
- Initialize z-buffer contents to 1.0 (far away)

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• For each triangle T
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-Rasterize T to generate fragments
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-For each fragment F with screen
position (x,y,z) and color value C
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• If (z < ZB[x,y]) then
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- Update color: CB[x,y] = C
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- Update depth: ZB[x,y] = z
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*The Depth Buffer (Z-Buffer)*Many fragments might map to the same pixel location How to track their z-values? Solution: z-buffer (2D buffer, same size as image)



*Z-buffer Algorithm Properties*What makes this method nice?

simple (faciliates hardware implementation)
handles intersections
handles cycles
draw opaque polygons in any order



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- One major problem with rasterization is called alias effects, e.g straight lines or triangle boundaries look jagged
- These are caused by undersampling, and can cause unreal visual artefacts.
- It also occurs in texture mapping





Anti-Aliasing

- The solution to aliasing problems is to apply a degree of blurring to the boundary such that the effect is reduced.
- The most successful technique is called <u>Supersampling</u>

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Supersampling

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- The basic idea is to compute the picture at a higher resolution to that of the display area.
- Supersamples are averaged to find the pixel value.
- This has the effect of blurring boundaries, but leaving coherent areas of colour unchanged



Limitations of Supersampling

- Supersampling works well for scenes made up of filled polygons.
- However, it does require a lot of extra computation.
- It does not work for line drawings.



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- The more common (and much faster) way of dealing with alias effects is to use a 'filter' to blur the image.
- This essentially takes an average over a small region around each pixel









Pros and Cons of Convolution filtering

- Advantages:
 - It is very fast and can be done in hardware
 - Generally applicable
- Disadvantages:
 - It does degrade the image while enhancing its visual appearance.



Anti-Aliasing textures

Similar

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- When we identify a point in the texture map we return an average of texture map around the point.
- Scaling needs to be applied so that the less the samples taken the bigger the local area where averaging is done.

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