

Revision Tutorial:

Animations, Transformations, Projections and Normalisation

1. Animating Objects

A cube in a graphics scene is defined by six square polygons. It is placed in the scene with its centre at $(5, 5, 10)$. In an animation sequence it shrinks by $1/100$ th of its size in each successive frame until it is too small to be seen. Determine the transformation matrix, which when applied to the co-ordinates of the vertices of the cube will achieve the shrinkage required in each frame.

2. Viewing transformations

In a viewer centred animation (*Translator's note*: this means first person shoot 'em up), the viewer is at the point $(10, 10, 10)$. The direction of view is $\mathbf{w} = (0.6, -0.2, 0.77)^T$. The horizontal direction to the right is $\mathbf{u} = (0.79, 0, -0.61)^T$.

Find the third unit vector \mathbf{v} making up the axis system. Your result for \mathbf{v} should point mainly upwards so if the y component you calculate is negative you have got the cross product the wrong way round.

Hence write down the viewing transformation matrix. If you've forgotten how to do this look in lecture notes on Scene Transformation and Animation, near the end.

3. Projection

The scene from the previous question is to be drawn in perspective projection on the plane $z = 2$. Find the required perspective projection matrix, and combined transformation and projection matrix.

A vertex of the scene has coordinate $(10, 10, 20, 1)$. Where does it project to?

4. Normalisation

The world coordinate window in the plane $z = 2$ is between $(x, y) = (-5, -5)$ and $(x, y) = (5, 5)$.

The window on the computer screen is of resolution 100 by 100 pixels, and the origin is in the top right hand side (bitmap organisation).

What is the pixel address of the vertex that was projected in the previous question?