## Tutorial 7: Ray Tracing

A solid modelling system uses the following primitives:
Cylinder $\quad: \mathbf{C}_{\mathbf{1}}, \mathbf{C}_{\mathbf{2}}$, r
Sphere : C, r
Box : A, $\mathbf{e}_{1}, \mathbf{e}_{\mathbf{2}}, \mathbf{e}_{3}$


The system is to draw the scene in orthographic projection. The viewing direction is parallel to the z axis: ( $0,0,1$ ).

1. Assuming a ray starts from a pixel with location $\left(x_{p i x}, y_{p i x}\right)$, devise a test for each primitive to identify simple cases when the ray cannot intersect it.
2. Use your tests to decide if the following rays:

| $\left(x_{p i x}, y_{p i x}\right)$ |  |
| :--- | :--- |
| Ray 1 | $(32,52)$ |
| Ray 2 | $(32,58)$ |

can be ruled out from intersecting the following objects:

| $\mathbf{C}_{\mathbf{1}}$ | $\mathbf{C}_{\mathbf{2}}$ |  |  |
| :--- | :--- | :--- | :--- |
| Cylinder 1 | $(20,50,50)$ | $(50,50,50)$ | 10 |
| Cylinder 2 | $(35,55,40)$ | $(35,55,60)$ | 5 |


| C | r |  |
| :--- | :--- | :--- |
| Sphere 1 | $(20,50,50)$ | 10 |


| $\mathbf{A}$ |  | $\mathbf{e}_{1}$ | $\mathbf{e}_{2}$ |  |
| :--- | :--- | :--- | :--- | :--- |
| Box 1 | $(35,45,40)$ | $(15,0,0)$ | $(0,15,0)$ | $(0,0,20)$ |
| Box 2 | $(30,55,40)$ | $(5,0,0)$ | $(0,-5,0)$ | $(0,0,20)$ |

3. For rays that intersect in Q 2 , what is the surface normal at the point of intersection?
4. Devise a suitable general test for use in perspective projection.
