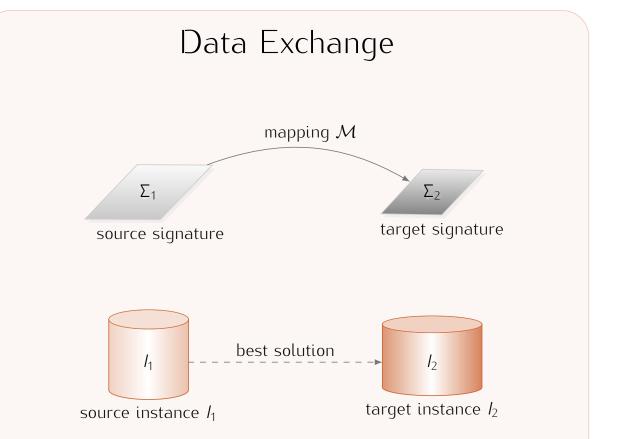
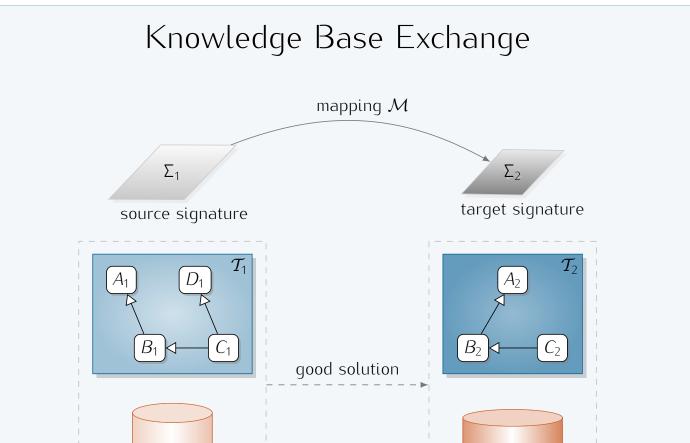
Description Logic Knowledge Base Exchange

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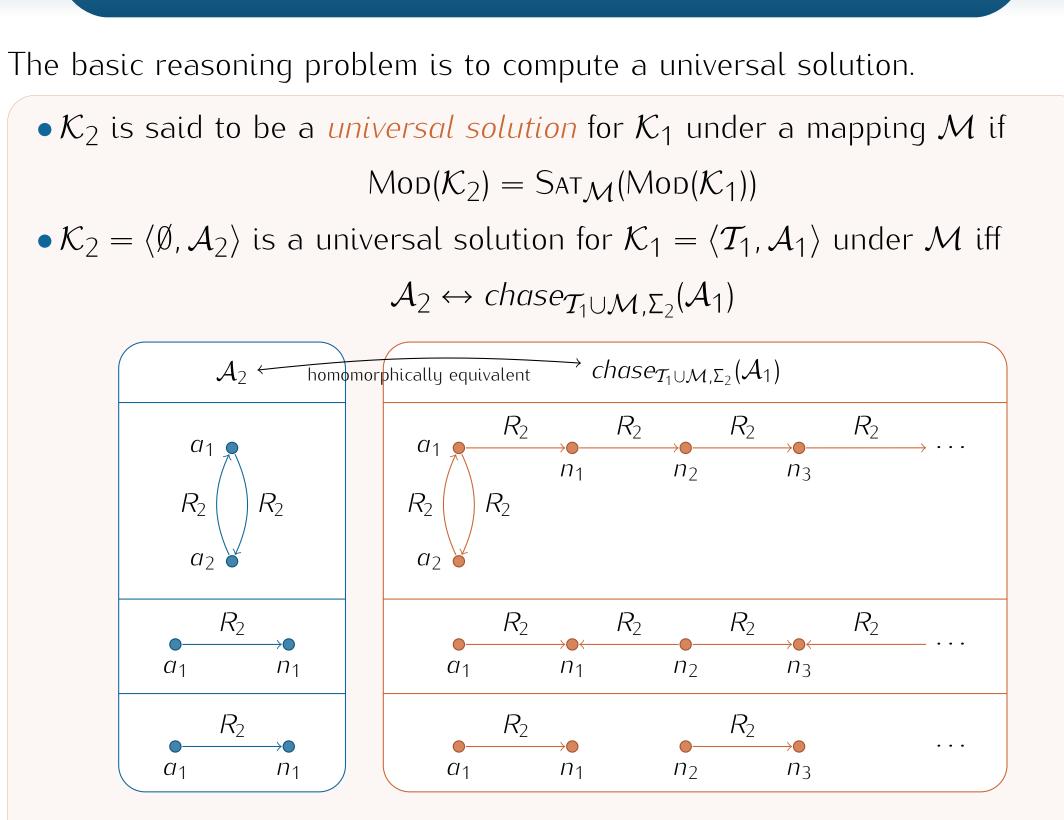
Data Exchange vs. Knowledge Base Exchange

Knowledge Base Exchange is a special case of Data Exchange with incomplete information.





(Computing) KB Solutions



Each database instance is *complete*, i.e., every fact is either true or false, therefore, represents *exactly one* possible instance (itself).

Data Exchange Example

Let $\mathcal{M} = \{ \forall a, t. (\text{AuthorOf}(a, t) \rightarrow \exists g. \text{BookInfo}(t, a, g)) \},$ $I_1 = \{ \text{AuthorOf}(\text{nabokov}, \text{lolita}),$ $\text{AuthorOf}(\text{tolkien}, \text{lotr}) \}.$ Then $I_2 = \{ \text{BookInfo}(\text{lolita}, \text{nabokov}, n_1),$ $\text{BookInfo}(\text{lotr}, \text{tolkien}, n_2) \}$ is a universal solution. \mathcal{A}_1 \mathcal{A}_2 source KB \mathcal{K}_1 target KB \mathcal{K}_2

A Description Logic (DL) Knowledge Base consists of*incomplete data* given as an ABox and

• *structural rules* for completing data given as a TBox, therefore, is a compact representation of (possibly infinitely) *many* actual instances.

Knowledge Base Exchange Example

Let $\mathcal{M} = \{ \exists AuthorOf^- \sqsubseteq \exists BookGenre, AuthorOf^- \sqsubseteq WrittenBy, TaxNumber \sqsubseteq SSN \},$

- $\mathcal{T}_1 = \{ \exists AuthorOf \sqsubseteq Author, Author \sqsubseteq \exists TaxNumber \}, \}$
- $A_1 = \{ AuthorOf(nabokov, lolita), AuthorOf(tolkien, lotr) \}.$

Then $A_2 = \{$ WrittenBy(lolita, nabokov), WrittenBy(lotr, tolkien), SSN(nabokov, m_1), SSN(tolkien, m_2), BookGenre(lolita, m_3), BookGenre(lotr, m_4) $\}$

is a universal solution.

We consider exchange of Description Logic KBs: each KB is constituted by a TBox and an ABox, and mapping is a set of DL inclusions from the source signature to the target signature. We start with lightweight DLs DL-Lite_{RDFS}.

Universal Solutions vs. Universal UCQ-Solutions

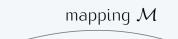
Universal UCQ-Solutions are the *preferred* solutions in our setting.

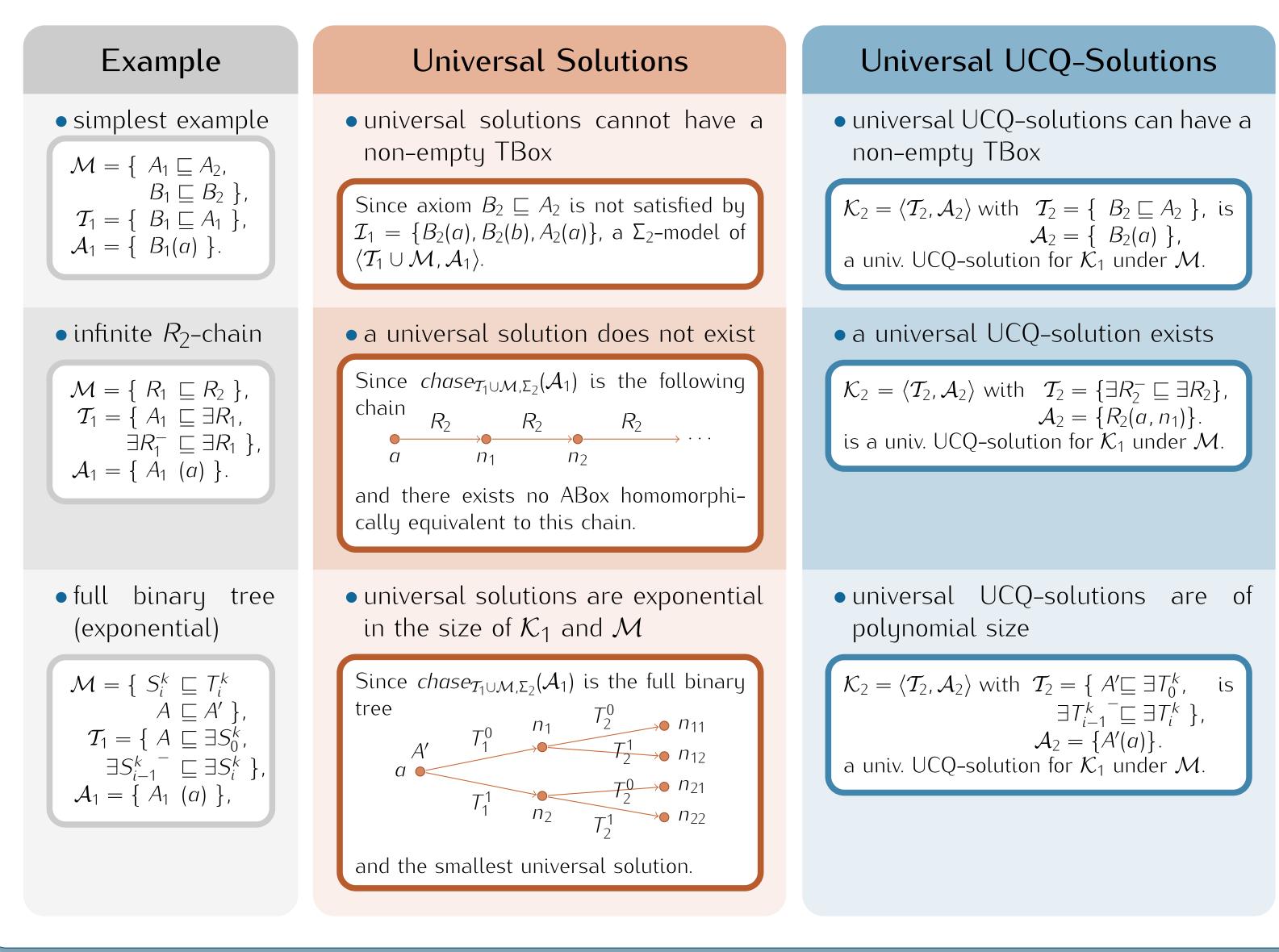
• Deciding existence of a universal solution in the case of DL-Lite_{\mathcal{R}} is \rightarrow PSpace-hard (reduction from satisfiability of QBF) and \rightarrow in ExpTIME (using two-way alternating automatas).

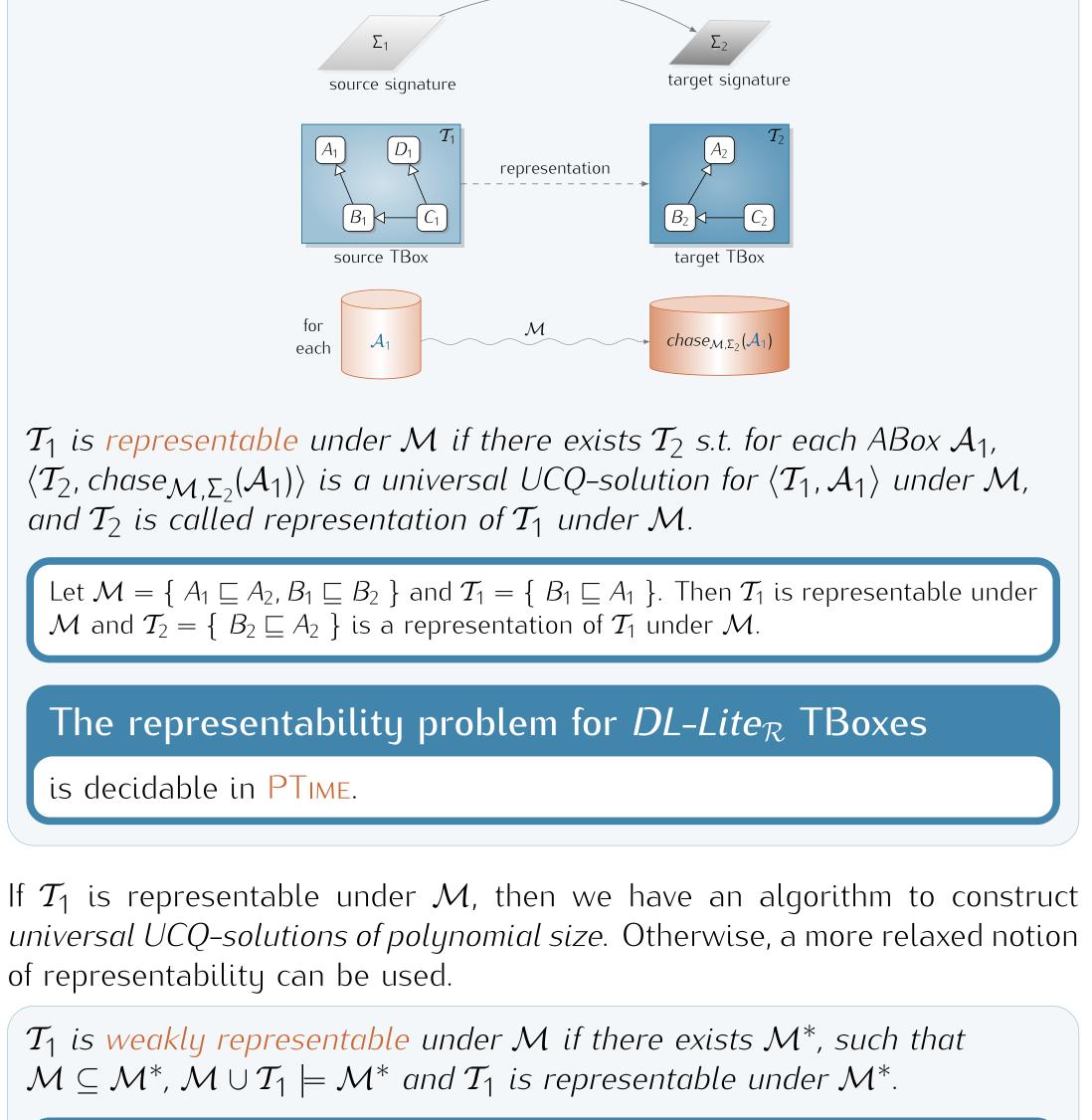
We are also interested in query-solutions for a class of queries Q. • \mathcal{K}_2 is said to be a *universal* Q-solution for \mathcal{K}_1 under \mathcal{M} , if $\forall q \in Q$ over Σ_2 , $cert(q, \langle T_1 \cup \mathcal{M}, \mathcal{A}_1 \rangle) = cert(q, \mathcal{K}_2)$ • $\mathcal{K}_2 = \langle T_2, \mathcal{A}_2 \rangle$ is a univ. UCQ-solution for $\mathcal{K}_1 = \langle T_1, \mathcal{A}_1 \rangle$ under \mathcal{M} iff $chase_{T_2}(\mathcal{A}_2) \leftrightarrow chase_{T_1 \cup \mathcal{M}, \Sigma_2}(\mathcal{A}_1)$ • The same complexity results hold for universal UCQ-solutions.

Representability Problem

We want to maximize implicit knowledge in the target.







Let $\mathcal{M} = \{ A_1 \sqsubseteq A_2 \}$ and $\mathcal{T}_1 = \{ B_1 \sqsubseteq A_1 \}$. Then \mathcal{T}_1 is weakly representable under \mathcal{M} : consider $\mathcal{M}^* = \{ A_1 \sqsubseteq A_2, B_1 \sqsubseteq A_2 \}$ and $\mathcal{T}_2 = \{ \}$.

Open Problems and Future Work

Problems that remain open

- the exact computational complexity of computing (universal) solutions,
- computing a universal solution in presence of disjointness assertions in the mapping,
- computing a universal UCQ-solution,
- computing the minimal mapping \mathcal{M}^* for a weakly representable \mathcal{T}_1 , such that \mathcal{T}_1 is representable under \mathcal{M}^* .

Plans for future work:

- implement the representability algorithm,
- implement a simple prototype for KB exchange,
- study KB exchange for more expressive/other languages, such as DL-Lite_R with $\exists R.A, DL$ -Lite_{horn}, and \mathcal{EL} , • study composition and inversion of mappings.

The weak representability problem for DL-Lite_R TBoxes

is decidable in PTIME.

Publications

- [1] M. Arenas, E. Botoeva, and D. Calvanese. Knowledge base exchange. In *Proc. of DL 2011*, volume 745 of *CEUR*, ceur-ws.org, 2011.
- [2] M. Arenas, E. Botoeva, D. Calvanese, V. Ryzhikov, and E. Sherkhonov. Exchanging description logic knowledge bases. In *Proc. of KR 2012*, 2012.
- [3] M. Arenas, E. Botoeva, D. Calvanese, V. Ryzhikov, and E. Sherkhonov. Representability in dl-liter knowledge base exchange. In *Proc. of the 25th Int. Workshop on Description Logics (DL 2012)*, 2012.