

# Description Logic Knowledge Base Exchange

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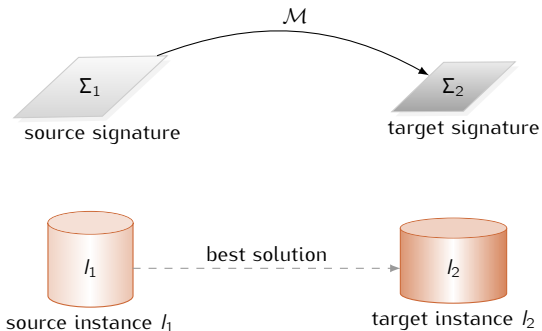
Reasoning Web and Rules Doctoral Consortium  
10 September 2012, Vienna



# Data Exchange

## Problem

given a mapping  $\mathcal{M}$  and a source instance  $I_1$ ,  
compute a target instance  $I_2$  that is a *solution* for  $I_1$  under  $\mathcal{M}$ .



# Data Exchange Example

$\mathcal{M} : \forall a, t. ( \text{AuthorOf}(a, t) \rightarrow \exists g. \text{BookInfo}(t, a, g) )$

$I_1 :$

<i>AuthorOf</i>	
nabokov	lolita
tolkien	lotr



# Data Exchange Example

$\mathcal{M} : \forall a, t. ( \text{AuthorOf}(a, t) \rightarrow \exists g. \text{BookInfo}(t, a, g) )$

$I_1 :$

<i>AuthorOf</i>	
nabokov	lolita
tolkien	lotr

$I_2 :$

<i>BookInfo</i>		
lolita	nabokov	$n_1$
lotr	tolkien	$n_2$

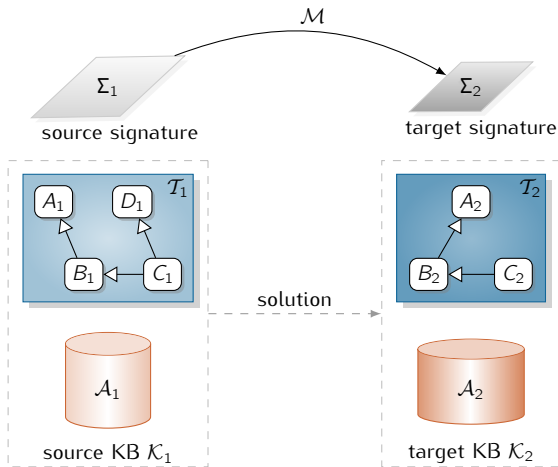
$I_2$  is a **universal** solution for  $I_1$  under  $\mathcal{M}$ .



# Knowledge Base Exchange

## Problem

given a mapping  $\mathcal{M}$  and a source knowledge base (KB)  $\mathcal{K}_1$ ,  
compute a target KB  $\mathcal{K}_2$  that is a *solution* for  $\mathcal{K}_1$  under  $\mathcal{M}$ .



# Knowledge Base Exchange: Example

$\mathcal{M}$  :             $\exists AuthorOf^-$              $\sqsubseteq$              $\exists BookGenre$   
                     $AuthorOf^-$              $\sqsubseteq$              $WrittenBy$   
                     $TaxNumber$              $\sqsubseteq$              $SSN$

$\mathcal{T}_1$  :             $\exists AuthorOf \sqsubseteq Author$   
                     $Author \sqsubseteq \exists TaxNumber$

$\mathcal{A}_1$  :

<i>AuthorOf</i>	
nabokov	lolita
tolkien	lotr



# Knowledge Base Exchange: Example

$\mathcal{M} :$ 

$\exists AuthorOf^-$	$\sqsubseteq$	$\exists BookGenre$
$AuthorOf^-$	$\sqsubseteq$	$WrittenBy$
$TaxNumber$	$\sqsubseteq$	$SSN$

$\mathcal{T}_1 :$ 

$\exists AuthorOf$	$\sqsubseteq$	$Author$
$Author$	$\sqsubseteq$	$\exists TaxNumber$

$\mathcal{A}_1 :$

<i>AuthorOf</i>	
nabokov	lolita
tolkien	lotr

$\mathcal{A}_2 :$

<i>WrittenBy</i>	
lolita	nabokov
lotr	tolkien
<i>SSN</i>	
nabokov	$m_1$
tolkien	$m_2$
<i>BookGenre</i>	
lolita	$m_3$
lotr	$m_4$

$\mathcal{A}_2$  is a **universal** solution for  $\langle \mathcal{T}_1, \mathcal{A}_1 \rangle$  under  $\mathcal{M}$ .



# Knowledge Base Exchange: Example

$\mathcal{M}$  :             $\exists AuthorOf^-$              $\sqsubseteq$              $\exists BookGenre$   
                     $AuthorOf^-$              $\sqsubseteq$              $WrittenBy$   
                     $TaxNumber$              $\sqsubseteq$              $SSN$

$\mathcal{T}_1$  :             $\exists AuthorOf \sqsubseteq Author$   
                     $Author \sqsubseteq \exists TaxNumber$

$\mathcal{A}_1$  :

<i>AuthorOf</i>	
nabokov	lolita
tolkien	lotr





# Knowledge Base Exchange: Example

$\mathcal{M}$  :             $\exists \text{AuthorOf}^-$              $\sqsubseteq$              $\exists \text{BookGenre}$   
                       $\text{AuthorOf}^-$              $\sqsubseteq$              $\text{WrittenBy}$   
                       $\text{TaxNumber}$              $\sqsubseteq$              $\text{SSN}$

$\mathcal{T}_1$  :             $\exists \text{AuthorOf} \sqsubseteq \text{Author}$   
                       $\text{Author} \sqsubseteq \exists \text{TaxNumber}$

$\mathcal{A}_1$  :

AuthorOf	
nabokov	lolita
tolkien	lotr

$\mathcal{T}_2$  :             $\exists \text{WrittenBy}^- \sqsubseteq \exists \text{SSN}$   
                       $\exists \text{WrittenBy} \sqsubseteq \exists \text{BookGenre}$

$\mathcal{A}_2$  :

WrittenBy	
lolita	nabokov
lotr	tolkien

$\langle \mathcal{T}_2, \mathcal{A}_2 \rangle$  is a **universal-UCQ** solution for  $\langle \mathcal{T}_1, \mathcal{A}_1 \rangle$  under  $\mathcal{M}$ .



# Reasoning Problems

We are interested in

- computing universal solutions

Does the **core** exist?

(Is there a **finite subset of**  $\text{chase}_{T_1 U M, \Sigma_2}(\mathcal{A}_1)$  homomorphically equivalent to  $\text{chase}_{T_1 U M, \Sigma_2}(\mathcal{A}_1)$ )

- ▶ PSPACE-hard
- ▶ in EXPTIME

- computing universal-UCQ solutions

Is  $\text{chase}_{T_2}(\mathcal{A}_2)$  homomorphically equivalent to  $\text{chase}_{T_1 U M, \Sigma_2}(\mathcal{A}_1)$ ?

- maximizing the implicit knowledge in the target

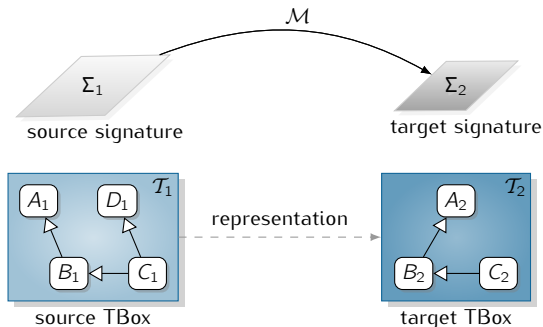
Universal solutions vs. Universal-UCQ solutions



# Representability Problem

## Problem

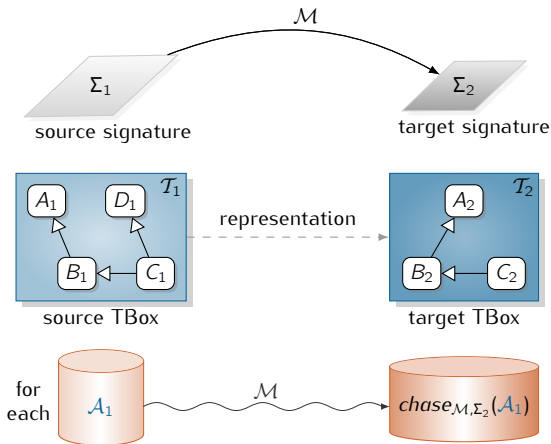
given a mapping  $\mathcal{M}$  and a source TBox  $\mathcal{T}_1$ ,  
compute (if exists) a target TBox  $\mathcal{T}_2$  such that for each source ABox  $\mathcal{A}_1$ ,  
 $\langle \mathcal{T}_2, \text{chase}_{\mathcal{M}, \Sigma_2}(\mathcal{A}_1) \rangle$  is a universal UCQ-solution for  $\langle \mathcal{T}_1, \mathcal{A}_1 \rangle$  under  $\mathcal{M}$ .



# Representability Problem

## Problem

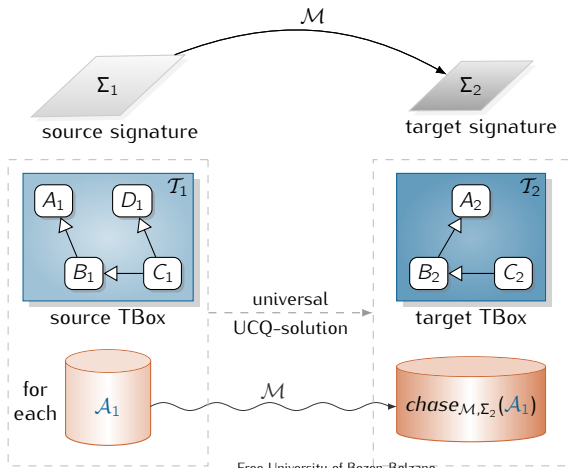
given a mapping  $\mathcal{M}$  and a source TBox  $\mathcal{T}_1$ ,  
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# Representability Problem

## Problem

given a mapping  $\mathcal{M}$  and a source TBox  $\mathcal{T}_1$ ,  
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# Representability: Example

$\mathcal{M}$  :       $\exists \text{AuthorOf}^- \sqsubseteq$        $\exists \text{BookGenre}$   
                  $\text{AuthorOf}^-$        $\sqsubseteq$        $\text{WrittenBy}$   
                  $\text{TaxNumber}$        $\sqsubseteq$        $\text{SSN}$

$\mathcal{T}_1$  :       $\exists \text{AuthorOf} \sqsubseteq$   
                  $\exists \text{TaxNumber}$

$\mathcal{T}_2$  :       $\exists \text{WrittenBy}^- \sqsubseteq \exists \text{SSN}$   
                  $\exists \text{WrittenBy} \sqsubseteq \exists \text{BookGenre}$

$\mathcal{T}_2$  is a **representation** of  $\mathcal{T}_1$  under  $\mathcal{M}$ .



# Representability: Example

$\mathcal{M} :$ 
 $\begin{array}{l} \exists \text{AuthorOf}^- \\ \text{AuthorOf}^- \\ \text{TaxNumber} \end{array} \sqsubseteq \begin{array}{l} \exists \text{BookGenre} \\ \text{WrittenBy} \\ \text{SSN} \end{array}$

$\mathcal{T}_1 :$ 
 $\begin{array}{l} \exists \text{AuthorOf} \sqsubseteq \\ \exists \text{TaxNumber} \end{array}$

$\mathcal{T}_2 :$ 
 $\begin{array}{l} \exists \text{WrittenBy}^- \sqsubseteq \exists \text{SSN} \\ \exists \text{WrittenBy} \sqsubseteq \exists \text{BookGenre} \end{array}$

$\mathcal{A}_1 :$

AuthorOf	
nabokov	lolita
TaxNumber	
smith	000

$\text{chase}_{\mathcal{M}, \Sigma_2}(\mathcal{A}_1) :$

WrittenBy	
lolita	nabokov
SSN	
smith	000
BookGenre	
lolita	$n_1$

$\mathcal{T}_2$  is a **representation** of  $\mathcal{T}_1$  under  $\mathcal{M}$ .



# Representability Problem

## Theorem

*Representability problem is decidable in polynomial time.*

Note that given  $\langle \mathcal{T}_1, \mathcal{A}_1 \rangle$  and  $\mathcal{M}$ , if  $\mathcal{T}_1$  is representable under  $\mathcal{M}$ , then we can construct a universal UCQ-solution of polynomial size.

Note also that the query inseparability problem for  $DL-Lite_{\mathcal{R}}$  TBoxes is PSPACE-hard.





# Open Problems and Future Work

## Open problems

- the exact computational complexity of computing (universal) solutions,
- computing a universal solution in presence of disjointness assertions in the mapping,
- computing a universal UCQ-solution,

## Future work:

- implementation of the representability algorithm,
- study KB exchange for more expressive/other languages, such as  $DL-Lite_{\mathcal{R}}$  with  $\exists R.A$ ,  $DL-Lite_{horn}$ , and  $\mathcal{EL}$ ,
- study composition and inversion of mappings.



Thank you  
for your attention!

