Verifying Auctions as Artifact Systems: Decidability via Finite Abstraction

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Model Checking in one slide

Model checking: technique(s) to **automatically** verify that a system design S satisfies a property P before deployment.

More formally, given

- a model \mathcal{M}_S of system S
- a formula ϕ_P representing property P

we check that

$$\mathcal{M}_{S} \models \phi_{P}$$

Turing Award 2007

www.acm.org/press-room/news-releases-2008/turing-award-07



(a) E. Clarke (CMU, USA) (b) A. Emerson (U. Texas, USA) (c) J. Sifakis (IMAG, F)

• Jury justification

For their roles in developing model checking into a highly effective verification technology, widely adopted in the hardware and software industries.

Overview

Motivation and Background:

- Artifact Systems as data-aware systems
- Parallel English (ascending bid) Auctions as Artifact Systems (eBay, etc.)

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- ...but less suited for data-intensive applications (data typically range over infinite domains) [1].

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Sey contribution:

- Verification of bounded and uniform AS is decidable
- Verification of Parallel English Auctions is decidable

Artifact Systems Outline

- Recent paradigm in Service-Oriented Computing [2].
- Motto: let's give data and processes the same relevance!
- Artifact: data model + lifecycle
 - (nested) records equipped with actions
 - actions may affect several artifacts
 - evolution stemming from the interaction with other artifacts/external actors
- Artifact System: interacting artifacts, representing services, manipulated by agents.
- Auctions as Artifact Systems

Artifact Systems Order-to-Cash Scenario



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- each bidder is rational,
- he has an intrinsic value for each item being auctioned,
- and he keeps this information private from other bidders and the auctioneer.

Artifact Systems Auction Data Model

Bidding						
item	<i>base_price</i>	bid_1		bid_ℓ	status	

- init_A(item,base_price)
- bid_i(item,bid)
- time_out(item)
- skip_A
- skip_i
- ...

trueValue_i item true_value

• *init_i(item,true_value)*

• . . .

Artifact Systems Auction Lifecycle

- Agents operate on artifacts.
 - e.g., the bidder sends a new bid to the auctioneer.
- Actions add/remove artifacts or change artifact attributes.
 - e.g., the auctioneer puts a new item on auction.
- The whole system can be seen as a *data-aware* dynamic system.
 - at every step, an action yields a change in the current state.



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- Is verification of AS decidable?
- If not, can we identify relevant fragments that are reasonably well-behaved?
- How can we implement this?

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- ... states have a relational structure,
- data are potentially infinite,
- the state space is infinite in general.
- $\Rightarrow\,$ The model checking problem cannot be tackled by standard techniques.

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 Intuition: databases (?) that evolve in time and are manipulated by agents.

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 FO-CTLK as a specification language:

AG $\forall it, \vec{bd}, s(\exists !bp \ Bidding(it, \vec{bd}, bp, s) \land \exists^{\leq 1}tv \ trueValue_i(it, tv))$

for each item there is exactly one base price, while bidders associate at most one true value to each item (possibly none).

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- Abstraction techniques and finite interpretation to tackle model checking.
 Main result: under specific conditions MC can be reduced to the finite case.
- Gase study: modelling and veryfing auctions as AC-MAS.

Semantics: Databases

The data model of AS is given as a particular kind of database.

- a database schema is a finite set $\mathcal{D} = \{P_1/a_1, \ldots, P_n/a_n, Q_1/b_1, \ldots, Q_m/b_m\}$ of (typed) relation symbols R_i with arity $c_i \in \mathbb{N}$.
- an *instance* on a domain U is a mapping D associating
 - each symbol P_i with a *finite* a_i -ary relation on U
 - each symbol Q_i with a (possibly infinite) b_i -ary relation on U
- the active domain adom(D) is the set of all $u \in U$ appearing in some $D(P_i)$.
- the *disjoint union* $D \oplus D'$ is the $(\mathcal{D} \cup \mathcal{D}')$ -interpretation s.t.
 - (i) $D \oplus D'(R_i) = D(R_i)$ (ii) $D \oplus D'(R'_i) = D'(R_i)$
- We consider untyped languages; the extension to types is not problematic.

Artifact-centric Multi-agent Systems Agents

Agents have partial access (views) to the artifact system.

- An *agent* is a tuple $A_i = \langle D_i, Act_i, Pr_i \rangle$ where
 - *D_i* is the local database schema
 - Act_i is the set of *local actions* $\alpha(\vec{x})$ with parameters \vec{x}
 - ▶ $Pr_i : D_i(U) \mapsto 2^{Act_i(U)}$ is the local protocol function
- the setting is reminiscent of the interpreted systems semantics for MAS [4],...
- ...but here the local state of each agent is relational.

Intuitively, agents manipulate artifacts and have (partial) access to the information contained in the global db schema $\mathcal{D} = \mathcal{D}_1 \cup \cdots \cup \mathcal{D}_\ell$.

Example 1: Parallel English (ascending bid) Auction

- Agents: <u>A</u>uctioneer, <u>B</u>idder₁, ..., <u>B</u>idder_l
- local db schema \mathcal{D}_A
 - ▶ Bidding(item, base_price, bid₁, ..., bid_ℓ, status)
 - \blacktriangleright < on \mathbb{Q}
- local db schema \mathcal{D}_i
 - Bidding(item, base_price, bid1, ..., bidl, status)
 - trueValue_i (item, true_value)
 - \blacktriangleright < on \mathbb{Q}
- then, $\mathcal{D} = \{\textit{Bidding}, \textit{trueValue}_1, \dots, \textit{trueValue}_\ell, <\}$
- Actions introduce values from an infinite domain U = Items ∪ Q ∪ {active, term}:
 - init_A(item, base_price), time out(item), skip_A belong to Act_A
 - init_i(item, true_value), bid_i(item, bid), skip_i belong to Act_i
- the protocol function specifies the preconditions for actions:
 - e.g., bid_i(item, bid) ∈ Pr_i(D) whenever item appears in D(trueValue_i), the highest bid bid_j in Bidding, j ≠ i, for item is < true_value for bidder B_i, bid_j < bid ≤ true_value, and D(status) = active for item.
 - the skip actions are always enabled.

Artifact-centric Multi-agent Systems AC-MAS

Agents are modules that can be composed together to obtain AC-MAS.

- Global states are tuples s = ⟨D₀,..., D_ℓ⟩ ∈ D(U).
- An <code>AC-MAS</code> is a tuple $\mathcal{P} = \langle Ag, s_0,
 ightarrow
 angle$ where
 - $Ag = \{A_0, \ldots, A_\ell\}$ is a finite set of agents
 - $s_0 \in \mathcal{D}(U)$ is the *initial global state*
 - $s \xrightarrow{\alpha(\vec{u})} s'$ is the transition relation
- Epistemic relation: $s \sim_i s'$ iff $D_i = D'_i$
- An AC-MAS \mathcal{P} is *rigid* iff for all states *s*, *s'*, symbol *Q*, and agents A_i , $A_j \in Ag$, $D_i(Q) = D'_j(Q)$.
- AC-MAS are infinite-state systems in general

AC-MAS are first-order temporal epistemic structures. Hence, FO-CTLK can be used as a specification language.

Example 2: the Auction AC-MAS

The Auction AC-MAS $\mathcal{A} = \langle Ag, s_0,
ightarrow
angle$ is defined as

- $Ag = \{A, B_1, \ldots, B_\ell\}$
- s₀ is the *empty interpretation* of D = {Bidding, trueValue₁,..., trueValue_ℓ, <} but for <
- \rightarrow is the *transition relation* s.t. $s \xrightarrow{\alpha(\vec{u})} s'$ whenever
 - α_i = bid_i(item, bid') and s' modifies s by replacing any tuple (item,..., bid_i,..., status) in D_s(Bidding) with (item,..., bid_i',..., status)
 - $\alpha_A = timeout(item)$ and the value of status in $D_{s'}(Bidding)$ for item is term

▶ ...

Notice:

- the auction AC-MAS ${\cal A}$ is rigid
- actions preserve the consistency of the underlying database
- the active domain *adom*(s₀) is empty

Syntax: FO-CTLK

- Data call for First-order Logic.
- Evolution calls for Temporal Logic.
- Agents (operating on artifacts) call for Epistemic Logic.

The specification language FO-CTLK:

 $\varphi \quad ::= \quad R(t_1, \ldots, t_c) \mid t = t' \mid \neg \varphi \mid \varphi \rightarrow \varphi \mid \forall x \varphi \mid AX\varphi \mid A\varphi U\varphi \mid E\varphi U\varphi \mid K_i \varphi$

Alternation of free variables and modal operators is enabled.

Semantics of FO-CTLK

Formal definition

An AC-MAS \mathcal{P} satisfies an FO-CTLK-formula φ in a state s for an assignment σ , iff

$$\begin{array}{lll} (\mathcal{P},s,\sigma)\models R(\vec{t}) & \text{iff} & \langle \sigma(t_1),\ldots,\sigma(t_c)\rangle \in D_s(R) \\ (\mathcal{P},s,\sigma)\models t=t' & \text{iff} & \sigma(t)=\sigma(t') \\ (\mathcal{P},s,\sigma)\models \neg\varphi & \text{iff} & (\mathcal{P},s,\sigma) \not\models \varphi \\ (\mathcal{P},s,\sigma)\models \varphi \rightarrow \psi & \text{iff} & (\mathcal{P},s,\sigma) \not\models \varphi \text{ or } (\mathcal{P},s,\sigma)\models \psi \\ (\mathcal{P},s,\sigma)\models \forall x\varphi & \text{iff} & \text{for all } u \in adom(s), (\mathcal{P},s,\sigma_u^x)\models \varphi \\ (\mathcal{P},s,\sigma)\models A \chi\varphi & \text{iff} & \text{for all runs } r, r(0)=s \text{ implies } (\mathcal{P},r(1),\sigma)\models \varphi \\ (\mathcal{P},s,\sigma)\models A \varphi U \varphi' & \text{iff} & \text{for all runs } r, r(0)=s \text{ implies } (\mathcal{P},r(k),\sigma)\models \varphi' \text{ for some } k \ge 0, \\ and & (\mathcal{P},r(k'),\sigma)\models \varphi \text{ for all } 0 \le k' < k \\ (\mathcal{P},s,\sigma)\models K_i\varphi & \text{iff} & \text{for all states } s', s \sim_i s' \text{ implies } (\mathcal{P},s',\sigma)\models \varphi \end{array}$$

- Active-domain semantics, but...
 - ...we can refer to no longer existing individuals
 - the number of states is infinite in general

Semantics of FO-CTLK

Intuition



(d) *AX \varphi*

(e) *AφU***ψ**

(f) *EφU*ψ

Verification of AC-MAS

How do we verify FO-CTLK specifications on auctions?

• the true value of items for each bidder is secret to all other bidders and to the auctioneer:

 $AG \;\forall item \; \neg \exists true_value \bigvee_{j \neq i \lor j = A} K_j \; trueValue_i(item, true_value)$

• for each bidder, each bid is less or equal to her true value:

 $AG \ \forall it, \vec{x}, bd_i, \vec{y}, tv(Bidding(it, \vec{x}, bd_i, \vec{y}) \land trueValue_i(it, tv) \rightarrow bd_i \leq tv)$

• each bidder can raise her bid unless she has already hit her true value: $AG \forall it, \vec{x}, bd_i, \vec{y}(Bidding(it, \vec{x}, bd_i, \vec{y}) \rightarrow$

 $\rightarrow (\textit{trueValue}_i(\textit{it},\textit{bd}_i) \lor \textit{EF} \exists \vec{x}',\textit{bd}_i', \vec{y}'(\textit{bd}_i' > \textit{bd}_i \land \textit{Bidding}(\textit{it},\vec{x}',\textit{bd}_i',\vec{y}'))))$

<u>Problem</u>: the infinite domain U may generate infinitely many states!

Investigated solution: can we simulate the concrete values from U with a finite set of abstract symbols?

• two states s, s' are *isomorphic*, or $s \simeq s'$, if there is a bijection

$$\iota: \mathit{adom}(s) \cup \mathit{C} \mapsto \mathit{adom}(s') \cup \mathit{C}$$

such that

- ι is the identity on C
- ▶ for every \vec{u} in adom(s), $A_i \in Ag$, $\vec{u} \in D_i(R) \Leftrightarrow \iota(\vec{u}) \in D'_i(R)$



 $\iota : a \mapsto 1$ $b \mapsto 2$ $c \mapsto c$ $d \mapsto 4$ $e \mapsto 5$









- the other direction holds as well
- similarly for the epistemic relation \sim_i

However, bisimulation is not sufficient to preserve FO-CTLK formulas:



 $\phi = AG \forall x (P(x) \rightarrow AX AG \neg P(x))$

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- More formally, an AC-MAS \mathcal{P} is *uniform* iff for $s, t, s' \in S$ and $t' \in \mathcal{D}(U)$:

```
\textcircled{9} \ s \to t \text{ and } s \oplus t \simeq s' \oplus t' \text{ imply } s' {\to} t'
```



S	s'		
1	2		
2	с		
4	5		

t'		
1	6	
6	С	

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- Uniform AC-MAS cover a number of interesting cases [2, 5], including the auction AC-MAS $\mathcal{A}.$

Bisimulation and Equivalence w.r.t. FO-CTLK

Theorem

Consider

- bisimilar and uniform AC-MAS \mathcal{P} and \mathcal{P}'
- an FO-CTLK formula φ

lf

$$|U'| \ge 2 \cdot \sup_{s \in \mathcal{P}} |adom(s)| + |C| + |vars(\varphi)|$$

$$|U| \geq 2 \cdot \sup_{s' \in \mathcal{P}'} |adom(s')| + |C| + |vars(\varphi)|$$

then

$$\mathcal{P} \models \varphi \quad \textit{iff} \quad \mathcal{P}' \models \varphi$$

Can we apply this result to finite abstraction?

Abstraction

- · Abstractions are defined in an agent-based, modular way.
- Let A = ⟨D, Act, Pr⟩ be an agent defined on the domain U.
 Given a domain U', the abstract agent A' = ⟨D, Act, Pr'⟩ on U' is s.t.
 - Pr' is the smallest function s.t. if α(ũ) ∈ Pr(D), D' ∈ D'(U') and D' ≃ D for some witness ι, then α(ũ') ∈ Pr'(D') where ũ' = ι'(ũ) for some constant-preserving bijection ι' extending ι to ū.
- Let P = ⟨Ag, s₀, →⟩ be an AC-MAS. The AC-MAS P' = ⟨Ag', s'₀, →'⟩ is an *abstraction* of P iff
 Ag' be the set of abstract agents on U'
 s'₀ ≃ s₀
 - ► →' is the smallest function s.t. if $s \xrightarrow{\alpha(\vec{u})} t$, and $s \oplus t \simeq s' \oplus t'$ for some witness ι , then $s' \xrightarrow{\alpha(\iota'(\vec{u}))} t'$ for some constant-preserving bijection ι' extending ι to \vec{u} .
- The abstraction of a rigid AC-MAS is not necessarily rigid!

Abstraction

Let N_{Ag} = ∑_{A_i∈Ag} max_{α(x)∈Act_i} |x| be the sum of the maximum numbers of parameters contained in the action types of each agent

Lemma

Consider

- a uniform and rigid AC-MAS \mathcal{P}
- a set $U' \supseteq C$ s.t. $|U'| \ge 2 \sup_{s \in \mathcal{P}} |adom(s)| + |C| + N_{Ag}$

Then, there exists an abstraction \mathcal{P}' of \mathcal{P} that is uniform and bisimilar to \mathcal{P} .

How can we define finite abstractions?

Bounded Models and Finite Abstractions

- An AC-MAS \mathcal{P} is *b*-bounded iff for all $s \in \mathcal{P}$, $|adom(s)| \leq b$.
- Bounded systems can still be infinite!

Theorem

Consider

■ a b-bounded, uniform and rigid AC-MAS \mathcal{P} on an infinite domain U ■ an FO-CTLK formula φ Given a finite U' \supset C s.t.

 $|U'| \geq 2b + |C| + \max\{|vars(\varphi)|, N_{Ag}\}$

there exists a finite abstraction \mathcal{P}' of \mathcal{P} s.t. \mathcal{P}' is uniform and bisimilar to \mathcal{P}

In particular,

$$\mathcal{P} \models \varphi \quad iff \quad \mathcal{P}' \models \varphi$$

 \Rightarrow Under specific circumstances, we can model check an infinite-state system by verifying its finite abstraction.

Finite Abstract Auction I

- the auction AC-MAS $\mathcal A$ is bounded by b = |Items|(2|Ag| 1) + 2
- Consider a finite $U' \ge 2b + vars(\phi)$
- Abstract agents <u>A</u>uctioneer A' and <u>B</u>idders B'_i
 - the local db schemas \mathcal{D}'_A and \mathcal{D}'_i are the same as for A and B_i
 - the sets of actions Act' and Act' are the same as for A and Bi
 - the protocol function Pr'_A is the same as for A
 - ▶ as to Pr'_i , $bid_i(item, bid) \in Pr'_i(D')$ whenever *item* appears in $D'(trueValue_i)$, the highest bid bid_j in *Bidding*, $j \neq i$, for *item* is $< true_value$ for bidder B_i , and bid is an abstract value that does not represent any bid in D', and for *item*, D'(status) = active.

Finite Abstract Auction II

The abstract auction AC-MAS $\mathcal{A}' = \langle Ag', s'_0, au'
angle$ is defined as

- $Ag' = \{A', B'_1, \dots, B'_\ell\}$
- s_0' is the empty interpretation of ${\cal D}$
- \rightarrow' mimics \rightarrow
 - ▶ e.g., if $\alpha_i = bid_i(item, bid)$, then $s \xrightarrow{\alpha(\vec{u})}' t$ whenever t is the db instance that modifies s by replacing any tuple ($item, \ldots, bid_i, \ldots, status$) in $D_s(Bidding)$ with ($item, \ldots, bid'_i, \ldots, status$), where the value $bid' \in U'$ has been found as above. In particular, $bid < bid' \leq true_value$ in t.
- By the assumption that $U' \ge 2b + vars(\phi)$ and Theorem 3 we have that \mathcal{A}' is a finite abstraction of \mathcal{A} . In particular,
 - \mathcal{A}' is uniform and bisimilar to \mathcal{A} (but not rigid) and

$$\mathcal{A} \models \varphi \quad \text{iff} \quad \mathcal{A}' \models \varphi$$

• Non-uniform AC-MAS: for sentence-atomic FO-CTL the results above still hold. $AG \ \forall it, \vec{bd}, s(\exists !bp \ Bidding(it, \vec{bd}, bp, s) \land \exists^{\leq 1}tv \ trueValue_i(it, tv))$

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On-uniform and unbounded AC-MAS: one-way preservation result for FO-ACTLK⁻.

Theorem

For every AC-MAS \mathcal{P} and $\varphi \in \text{FO-ACTLK}^-$, there exists a finite abstraction \mathcal{P}' such that if $\mathcal{P}' \models \varphi$ then $\mathcal{P} \models \varphi$.

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Model checking bounded AC-MAS w.r.t. FO-CTL is undecidable.

Complexity result:

Theorem

The model checking problem for finite AC-MAS w.r.t. FO-CTLK is EXPSPACE-complete in the size of the formula and data.

- We are able to model check AC-MAS w.r.t. full FO-CTLK...
- ...however, our results hold only for *rigid*, *uniform* and *bounded* systems.
- This class includes many interesting systems (AS programs, [2, 5]).
- The model checking problem is EXPSPACE-complete.

Next Steps

- Techniques for finite abstraction.
- Model checking techniques for finite-state systems are effective on the abstract system?
- How to perfom the boundedness check.

Merci!

References

eamericonart@aristel Baier and Joost-Pieter Katoen. Principles of Model Checking. MIT Press, 2008. eamericonartigle Cohn and R. Hull. Business Artifacts: A Data-Centric Approach to Modeling Business Operations and Processes. IEEE Data Eng. Bull., 32(3):3-9, 2009. eamericonartigle Easley and J. Kleinberg. Networks, Crowds, and Markets: Reasoning About a Highly Connected World. Cambridge University Press, New York, NY, USA, 2010. eamericonartRle Fagin, J.Y. Halpern, Y. Moses, and M.Y. Vardi. Reasoning About Knowledge. The MIT Press, 1995. americorlart®le Bagheri Hariri, D. Calvanese, G. De Giacomo, R. De Masellis, and P. Felli.

Foundations of Relational Artifacts Verification. In *Proc. of BPM*, 2011.