# Learning Weak Constraints in Answer Set Programming

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Mark Law, Alessandra Russo and Krysia Broda Learning Weak Constraints in Answer Set Programming ◆□ ▶ ◆母 ▶ ◆ 臣 ▶ ◆ 臣 ▶ ○ 臣 ⑦ � @ 1/29

# Preference Learning

- Learning to rank is an approach to preference learning where the goal is to learn to order objects given pairwise examples of a user's preferences.
- For example, learning academic's preferences about interview scheduling.

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

is preferred to

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

Although traditional machine learning techniques can be used to predict preferences, their reasoning is not easily human readable.

## Inductive Logic Programming

- ▶ Given a set of positive examples E<sup>+</sup>, negative examples E<sup>-</sup> and a background knowledge B, the goal is to find a hypothesis H such that:
  - ▶  $\forall e \in E^+ : B \cup H \models e$
  - ►  $\forall e \in E^- : B \cup H \not\models e$

## Inductive Logic Programming

- ► Given a set of positive examples E<sup>+</sup>, negative examples E<sup>-</sup> and a background knowledge B, the goal is to find a hypothesis H such that:
  - ▶  $\forall e \in E^+ : B \cup H \models e$
  - ▶  $\forall e \in E^- : B \cup H \not\models e$
- The key advantages are that:
  - The hypotheses are human readable.
  - Can define useful concepts in the background knowledge.
  - Can give a very structured language bias to guide the search.

# Learning from Answer Sets (*ILP<sub>LAS</sub>*)

- In *ILP<sub>LAS</sub>* (Law et al. 2014), examples are *partial* interpretations.
- A partial interpretation e is a pair of sets of atoms  $\langle e^{inc}, e^{exc} \rangle$ .
- An answer set A extends e iff  $e^{inc} \subseteq A$  and  $e^{exc} \cap A = \emptyset$ .

	1	2	3
Μ	с1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

is extended by

	1	2	3
М	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

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# Learning from Answer Sets (ILP<sub>LAS</sub>)

#### Definition 1

An ILP<sub>LAS</sub> task is a tuple  $T = \langle B, S_M, E^+, E^- \rangle$ . A hypothesis  $H \subseteq S_M$  is in ILP<sub>LAS</sub>(T), the set of all inductive solutions of T, if and only if:

- ►  $\forall e^+ \in E^+ \exists A \in AS(B \cup H)$  such that A extends  $e^+$
- ►  $\forall e^- \in E^- \nexists A \in AS(B \cup H)$  such that A extends  $e^-$ .

(Law et al. 2014)

# Weak Constraints in ASP

$$\begin{split} &:\sim \texttt{assign}(D,S), \texttt{type}(D,S,\texttt{c1}).\, [\texttt{1@2},D,S] \\ &:\sim \texttt{assign}(D,\texttt{S1}), \texttt{assign}(D,\texttt{S2}), \texttt{neq}(\texttt{S1},\texttt{S2}).\, [\texttt{1@1},D,\texttt{S1},\texttt{S2}] \end{split}$$

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

is preferred to

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

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# Weak Constraints in ASP

# $\sim \texttt{assign}(D,S),\texttt{type}(D,S,\texttt{c1}).[1@2,D,S]$

 $:\sim \texttt{assign}(\texttt{D},\texttt{S1}), \texttt{assign}(\texttt{D},\texttt{S2}), \texttt{neq}(\texttt{S1},\texttt{S2}). \texttt{[1@1, D, S1, S2]}$ 

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

is preferred to

	1	2	3
М	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

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# Weak Constraints in ASP

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

is preferred to

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

# Weak Constraints in ASP

#### 

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

is preferred to

	1	2	3
М	c1	c2	c2
Т	c2	c2	c2
W	c2	c1	c2

# Learning from Ordered Answer Sets

- As previous ILP frameworks could only give examples of what should (or shouldn't) be an answer set of the program, no existing framework could incentivise learning weak constraints.
- We now present an extension of *ILP<sub>LAS</sub>* (Law et al. 2014), with a new type of example aimed at learning weak constraints.

# **Ordering Examples**

#### Definition 3

An ordering example is a tuple  $o = \langle e_1, e_2 \rangle$  where  $e_1$  and  $e_2$  are partial interpretations.



# Brave Scheduling Example

$$\label{eq:sign_loss} \begin{split} &:\sim \texttt{assign}(D,S1), \texttt{assign}(D,S2), \texttt{neq}(S1,S2).\, \texttt{[1@1}, D,S1,S2] \\ &:\sim \texttt{assign}(D,S), \texttt{type}(D,S,\texttt{c1}).\, \texttt{[1@2}, D,S] \end{split}$$

	1	2	3
Μ	c1	c2	c2
Т	c2	c2	c2
W	c2	с1	c2

is sometimes preferred to

	1	2	3	
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Т	c2	c2	c2	
W	c2	c1	c2	

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#### Definition 3

An ASP program P bravely respects o iff ∃A<sub>1</sub>, A<sub>2</sub> ∈ AS(P) such that A<sub>1</sub> extends e<sub>1</sub>, A<sub>2</sub> extends e<sub>2</sub> and A<sub>1</sub> ≻<sub>P</sub> A<sub>2</sub>.

# Cautious Scheduling Example

	1	2	3	
Μ	c1	c2	c2	
Т	c2	c2	c2	
W	c2	c1	c2	

is always preferred to

	1	2	3	
М	c1	c2	c2	
Т	c2	c2	c2	
W	c2	c1	c2	

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#### Definition 3

P cautiously respects o iff ∀A<sub>1</sub>, A<sub>2</sub> ∈ AS(P) such that A<sub>1</sub> extends e<sub>1</sub> and A<sub>2</sub> extends e<sub>2</sub>, it is the case that A<sub>1</sub> ≻<sub>P</sub> A<sub>2</sub>.

Learning from Ordered Answer Sets (*ILP<sub>LOAS</sub>*)

#### Definition 4

An ILP<sub>LOAS</sub> task is a tuple  $T = \langle B, S_M, E^+, E^-, O^b, O^c \rangle$ . A hypothesis  $H \subseteq S_M$  is in ILP<sub>LOAS</sub>(T), the inductive solutions of T, if and only if:

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- 1.  $\forall e^+ \in E^+ \exists A \in AS(B \cup H)$  such that A extends  $e^+$
- 2.  $\forall e^- \in E^- \nexists A \in AS(B \cup H)$  such that A extends  $e^-$ .
- 3.  $\forall o \in O^b \ B \cup H$  bravely respects o
- 4.  $\forall o \in O^c \ B \cup H$  cautiously respects o

## Complexity

#### Theorem 3

Let T be any propositional  $ILP_{LAS}$  or  $ILP_{LOAS}$  task. Deciding whether T has at least one inductive solution is  $NP^{NP}$ -complete.

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# Algorithm

- Our new algorithm ILASP2 (Inductive Learning of Answer Set Programs) is sound and complete wrt the optimal (shortest) solutions of any *ILP<sub>LOAS</sub>* task.
- It is available for download at https://www.doc.ic.ac.uk/~ml1909/ILASP.
- It extends our previous ILASP1 algorithm for solving *ILP<sub>LAS</sub>* tasks (Law et al. 2014).

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## Positive and Violating Hypotheses

Definition 5/6

Let  $T = \langle B, S_M, E^+, E^- \rangle$  be an ILP<sub>LAS</sub> task. Any  $H \subseteq S_M$  is a positive hypothesis iff  $\forall e \in E^+ \exists A \in AS(B \cup H)$  such that A extends e.

A positive hypothesis H is violating iff  $\exists e^- \in E^-$ ,  $\exists A \in AS(B \cup H)$  such that A extends  $e^-$ .

(Law et al. 2014)

### Positive and Violating Hypotheses

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$$E^{+} = \left\{ \begin{array}{|c|c|c|} \hline 1 & 2 \\ \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\} \quad E^{-} = \left\{ \begin{array}{|c|c|} \hline 1 & 2 \\ \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\}, \begin{array}{|c|c|} \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\}, \begin{array}{|c|} \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\}$$

$$B = \begin{cases} \text{slot}(m, 1..2). \text{ slot}(t, 1..2). \text{ type}(m, 1, c1). \\ \text{type}(m, 2, c2). \text{ type}(t, 1, c2). \text{ type}(t, 2, c2). \\ 0\{\text{assign}(D, S)\}1:-\text{slot}(D, S). \end{cases}$$

 $H = \emptyset$ 

#### This is a positive hypothesis, but is also violating.

### Positive and Violating Hypotheses

$$E^{+} = \left\{ \begin{array}{c|c} 1 & 2 \\ \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\} \quad E^{-} = \left\{ \begin{array}{c|c} 1 & 2 \\ \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\}, \begin{array}{c|c} 1 & 2 \\ \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\}, \begin{array}{c|c} \hline M & c1 & c2 \\ \hline T & c2 & c2 \end{array} \right\}$$

$$B = \begin{cases} \text{slot}(m, 1..2). \text{ slot}(t, 1..2). \text{ type}(m, 1, c1). \\ \text{type}(m, 2, c2). \text{ type}(t, 1, c2). \text{ type}(t, 2, c2). \\ 0\{\text{assign}(D, S)\}1:-\text{slot}(D, S). \end{cases}$$

$$H = \left\{ \text{ :-assign(m,S). } \right\}$$

This is a positive hypothesis which is not violating. Hence, it is an inductive solution.

## Positive and Violating Hypotheses

#### Definition 5/6

Let  $T = \langle B, S_M, E^+, E^-, O^b, O^c \rangle$  be an  $ILP_{LOAS}$  task. Any  $H \subseteq S_M$  is a positive hypothesis iff  $\forall e \in E^+ \exists A \in AS(B \cup H)$  such that A extends e, and  $\forall o \in O^b B \cup H$  bravely respects o.

A positive hypothesis H is violating iff at least one of the following cases is true:

- ▶  $\exists e^- \in E^-$ ,  $\exists A \in AS(B \cup H)$  such that A extends  $e^-$ .
- ▶  $\exists A_1, A_2 \in AS(B \cup H)$  and  $\exists \langle e_1, e_2 \rangle \in O^c$  such that  $A_1$  extends  $e_1, A_2$  extends  $e_2$  and  $A_1 \nvDash_P A_2$  with respect to  $B \cup H$ .

### **ILASP1**

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```
procedure ILASP1(T)
    solutions = []
    n = 0
    while solutions == [] do
        V = violating_hypotheses(T, n)
        solutions = remaining_positive_hypothses(T, n, V)
        n = n + 1
    end while
    return solutions
end procedure
(Law et al. 2014)
```

### Positive Hypotheses and Violating Reasons

#### Definition 5/6

Let  $T = \langle B, S_M, E^+, E^-, O^b, O^c \rangle$  be an  $ILP_{LOAS}$  task. Any  $H \subseteq S_M$  is a positive hypothesis iff  $\forall e \in E^+ \exists A \in AS(B \cup H)$  such that A extends e, and  $\forall o \in O^b$   $H \cup B$  bravely respects o.

A positive hypothesis H is violating iff at least one of the following cases is true:

- ∃e<sup>-</sup>∈E<sup>-</sup>, ∃A∈AS(B∪H) such that A extends e<sup>-</sup>. In this case we call A a violating interpretation of T.
- ▶  $\exists A_1, A_2 \in AS(B \cup H)$  and  $\exists \langle e_1, e_2 \rangle \in O^c$  such that  $A_1$  extends  $e_1, A_2$  extends  $e_2$  and  $A_1 \not\succ_P A_2$  with respect to  $B \cup H$ . In this case, we call  $\langle A_1, A_2 \rangle$  a violating pair of T.

### Meta Representation: Properties

Given a task T and a set of violating reasons VR, we defined a meta program  $\mathcal{M}(T, VR)$ .

The A's ∈ AS(M(T, VR)) map to the positive hypotheses M<sup>-1</sup><sub>hvp</sub>(A) which do not violate any vr ∈ VR.

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- ▶ If *H* is violating, there is an  $A \in AS(\mathcal{M}(T, VR))$  st  $H = \mathcal{M}_{hvp}^{-1}(A)$  and violating  $\in A$ .
- ► The optimality of each answer set A is 2|M<sup>-1</sup><sub>hyp</sub>(A)| if violating ∈ A and 2|M<sup>-1</sup><sub>hyp</sub>(A)| + 1 otherwise.

### ILASP2

#### procedure ILASP2(*T*) VR = [] $A = solve(\mathcal{M}(T, VR))$ while $A \neq nil \&\& violating \in A$ do $VR + = \mathcal{M}_{vr}^{-1}(A)$ $A = solve(\mathcal{M}(T, VR))$ end while return $\{\mathcal{M}_{hvn}^{-1}(A) \mid A \in AS^*(\mathcal{M}(T, VR))\}$

#### end procedure

▶ solve(P) returns an optimal answer set of P (it returns nil if  $AS(P) = \emptyset$ ).

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- $\mathcal{M}_{hyp}^{-1}$  maps an answer set of  $\mathcal{M}(\mathcal{T}, VR)$  to the corresponding hypothesis.
- ▶ M<sup>-i</sup><sub>vr</sub> maps an answer set of M(T, VR) to the corresponding violating reason.

## Soundness and Completeness

#### Theorem 5

Let T be an  $ILP_{LOAS}$  task. If ILASP2(T) terminates, then ILASP2(T) returns the set of optimal inductive solutions of  $ILP_{LOAS}(T)$ .

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## Sudoku Experiment

- ► In (Law et al. 2014) we showed that ILASP1 could be used to learn the rules of a 4x4 version of sudoku.
- This took 486.2s (over 8 minutes) to solve with ILASP1 as there were 332437 violating hypotheses found before the first inductive solution.
- ILASP2 only needs 9 violating reasons and so solves the same task in 0.69s (less than 1 second).

### Experiments

Our main experiments were on the interview scheduling example.

- ► For each experiment, we randomly generated hypotheses H with up to 3 weak constraints from S<sub>M</sub>.
- ▶ We used each *H* to randomly generate orderings.
- ► We then used ILASP2 to learn a hypothesis *H*′ which covered these examples.
- ► We checked the accuracy of H' at predicting the orderings of the timetables given by H.

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### Experiments

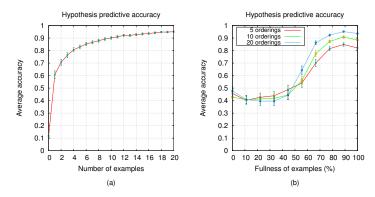


Figure : Accuracy with varying (a) numbers of examples; (b) fullness of examples

### Experiments

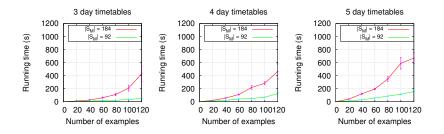


Figure : Average running time of ILASP2 with varying numbers of examples

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### Comparison of Non-monotonic ILP systems

Learning Task	Normal Rules	Choice Rules	Constraints	Brave	Cautious	Weak Constraints	Algorithm for optimal solutions
Brave Induction [Sakama, Inoue 2009]	~	•	×	•	×	×	×
Cautious Induction [Sakama, Inoue 2009]	~	~	×	×	~	×	×
XHAIL [Ray 2009] & ASPAL [Corapi et al 2011]	•	×	×	•	×	×	<ul> <li></li> </ul>
Induction of Stable Models [Otero 2001]	~	×	×	V	×	×	×
Induction from Answer Sets [Sakama 2005]	~	×	~	~	~	×	×
LAS [Law et al 2014]	~	~	~	~	•	×	~
LOAS	~	~	× .	~	~	<b>v</b>	<ul> <li>✓</li> </ul>

### Other Related Work in ILP

ILP systems have previously been used for preference learning (Dastani et al. 2001, Horváth 2012). This addressed learning ratings, such as good, poor and bad, rather than rankings over the examples.

# Summary

- Presented *ILP<sub>LOAS</sub>*, which is the first framework capable of learning weak constraints.
- Presented ILASP2, which is sound and complete wrt  $ILP_{LOAS}$ .
- Proved the complexity of deciding the existence of solutions for ILP<sub>LAS</sub> and ILP<sub>LOAS</sub>.
- Showed that ILASP2 is more efficient than ILASP1 for the previous ILP<sub>LAS</sub> task.
- Gave experimental results of ILASP2 in the setting of learning accademic's preferences for interview scheduling.

# Future Work

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- Support noisy examples.
- Improve the performance with larger numbers of examples.

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