

Iterative Learning of Answer Set Programs from Context Dependent Examples

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Context-dependent examples

- ▶ In standard ILP, we search for hypotheses H such that:
 - ▶ $\forall e \in E^+ B \cup H \models e$
 - ▶ $\forall e \in E^- B \cup H \not\models e$
- ▶ Given *context-dependent examples*, it must be the case that:
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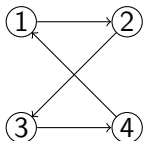
For example, we may wish to learn that when it is raining a user prefers to take the bus; otherwise, they prefer to walk.

$$E^+ = \left\{ \begin{array}{l} \langle \text{“take bus”}, \{\text{rain.}\} \rangle, \\ \langle \text{“walk”}, \{\} \rangle \end{array} \right\}, \quad E^- = \left\{ \begin{array}{l} \langle \text{“walk”}, \{\text{rain.}\} \rangle, \\ \langle \text{“take bus”}, \{\} \rangle \end{array} \right\}$$



Learning from Answer Sets (ILP_{LAS})

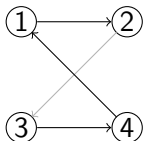
- ▶ In ILP_{LAS} (Law et al. 2014), examples are *partial interpretations*.
- ▶ A partial interpretation e is a set of pairs of atoms $\langle e^{inc}, e^{exc} \rangle$.



$$\left\langle \left\{ \begin{array}{l} \text{size}(4) \\ \text{edge}(1, 2) \\ \text{edge}(2, 3) \\ \text{edge}(3, 4) \\ \text{edge}(4, 1) \end{array} \right\}, \left\{ \begin{array}{l} \text{edge}(1, 1) \\ \text{edge}(1, 3) \\ \text{edge}(1, 4) \\ \dots \end{array} \right\} \right\rangle$$

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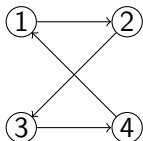


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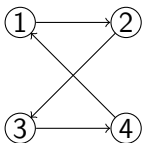


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- ▶ An answer set A extends e iff $e^{inc} \subseteq A$ and $e^{exc} \cap A = \emptyset$.
- ▶ A positive (resp. negative) example e is covered if at least one (resp. no) answer set of $B \cup H$ extends e .



ILP_{LAS} Encoding of the Hamiltonian Example



B :

```

1{size(1..4)}1.
node(1..N):-size(N).
0{edge(V0, V1)}1:-node(V0),
                    node(V1).
  
```

$$\left\langle \left\{ \begin{array}{l} \text{size}(4) \\ \text{edge}(1, 2) \\ \text{edge}(2, 3) \\ \text{edge}(3, 4) \\ \text{edge}(4, 1) \end{array} \right\}, \left\{ \begin{array}{l} \text{edge}(1, 1) \\ \text{edge}(1, 3) \\ \text{edge}(1, 4) \\ \dots \end{array} \right\} \right\rangle$$

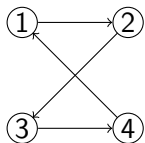
H :

```

reach(V0):-in(1, V0).
reach(V1):-in(V0, V1), reach(V0).
0{in(V0, V1)}1:-edge(V0, V1).
:-node(V0), not reach(V0).
:-in(V0, V1), in(V0, V2), V1 ≠ V2.
  
```



Context-dependent Hamiltonian Example



$B :$

None!

$$\left\langle \langle \emptyset, \emptyset \rangle, \left\{ \begin{array}{l} \text{node}(1..4). \\ \text{edge}(1,2). \\ \text{edge}(2,3). \\ \text{edge}(3,4). \\ \text{edge}(4,1). \end{array} \right\} \right\rangle$$

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Journey Preferences in ASP

$$H = \begin{cases} : \sim \text{mode}(L, \text{walk}), \text{crime_rating}(L, R), R > 3. [1@3, L, R] \\ : \sim \text{mode}(L, \text{bus}). [1@2, L] \\ : \sim \text{mode}(L, \text{walk}), \text{distance}(L, D). [D@1, L, D] \end{cases}$$



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ILP_{LOAS} (Law et al. 2015) is an extension of ILP_{LAS} with *ordering examples* of the form $\langle e_1, e_2 \rangle$.



Journey Preferences in ASP

$$H = \begin{cases} \text{:~ mode(L, walk), crime_rating(L, R), R > 3. [1@3, L, R]} \\ \text{:~ mode(L, bus). [1@2, L]} \\ \text{:~ mode(L, walk), distance(L, D). [D@1, L, D]} \end{cases}$$

$$B = \begin{cases} 1\{\text{choose}(j_1), \dots, \text{choose}(j_n)\}1. \\ \text{mode(leg1, walk):-choose}(j_1). \\ \text{crime_rating(leg1, 2):-choose}(j_1). \\ \text{distance(leg1, 1000):-choose}(j_1). \\ \dots \end{cases}$$

$$e_1 = \langle \{\text{choose}(j_1)\}, \emptyset \rangle, \quad e_2 = \langle \{\text{choose}(j_2)\}, \emptyset \rangle, \quad \dots$$

$$O^b = \left\{ \begin{array}{c} \langle e_1, e_2 \rangle \\ \dots \end{array} \right\}$$



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$$B = \{ \text{None!} \}$$

$$e_1 = \langle \langle \emptyset, \emptyset \rangle, \left\{ \begin{array}{l} \text{mode}(\text{leg1}, \text{walk}). \\ \text{crime_rating}(\text{leg1}, 2). \\ \text{distance}(\text{leg1}, 1000). \end{array} \right\} \rangle \quad \dots$$

$$O^b = \left\{ \begin{array}{l} \langle e_1, e_2 \rangle \\ \dots \end{array} \right\}$$



Complexity

- ▶ In the paper, we present a mapping \mathcal{T}_{LOAS} from any $ILP_{LOAS}^{context}$ task to an ILP_{LOAS} task.

Theorem 1

For any $ILP_{LOAS}^{context}$ task T , $ILP_{LOAS}(\mathcal{T}_{LOAS}(T)) = ILP_{LOAS}^{context}(T)$.

Theorem 2

The complexity of deciding whether an $ILP_{LOAS}^{context}$ task is satisfiable is Σ_2^P -complete.



ILASP2i

- ▶ The mapping \mathcal{T}_{LOAS} means that we can use ILASP2 to compute solutions for any context dependent task:
 - ▶ This would be by calling $ILASP2(\mathcal{T}_{LOAS}(\langle B, S_M, E \rangle))$.
 - ▶ However, ILASP2 is known to scale poorly wrt the number of examples.
- ▶ Our new algorithm, ILASP2i, iteratively computes a subset of the examples Rel , called *relevant examples*.
 - ▶ In each iteration, we call $ILASP2(\mathcal{T}_{LOAS}(\langle B, S_M, Rel \rangle))$.

Theorem 4

ILASP2i is sound for any well defined $ILP_{LOAS}^{context}$ task, and returns an optimal solution if one exists.



Benchmarks

Learning task	#examples				time/s		Memory/kB	
	E^+	E^-	O^b	O^c	2	2i	2	2i
Hamilton A (no context)	100	100	0	0	10.3	4.3	9.7×10^4	1.2×10^4
Hamilton B (context dep.)	100	100	0	0	32.0	3.6	3.6×10^5	1.4×10^4
Journeys (context dep.)	386	0	200	0	1031.4	5.0	1.4×10^7	3.4×10^4

- ▶ ILASP2 runs the automatic translation (\mathcal{T}_{LOAS}) of context dependent tasks.
- ▶ \mathcal{T}_{LOAS} (Hamilton B) is less efficient than Hamilton A.
- ▶ \mathcal{T}_{LOAS} (Journeys) is the same as the non-context dependent Journey task.



Related work under the answer set semantics

Learning Task	Normal Rules	Choice Rules	Constraints	Classical Negation	Brave	Cautious	Weak Constraints	Context	Algorithm for optimal solutions
<i>Brave Induction</i> [Sakama, Inoue 2009]	✓	✓	✗	✓	✓	✗	✗	✗	✗
<i>Cautious Induction</i> [Sakama, Inoue 2009]	✓	✓	✗	✓	✗	✓	✗	✗	✗
<i>XHAIL</i> [Ray 2009] & <i>ASPAL</i> [Corapi et al 2011]	✓	✗	✗	✗	✓	✗	✗	✗	✓
<i>Induction of Stable Models</i> [Otero 2001]	✓	✗	✗	✗	✓	✗	✗	✗	✗
<i>Induction from Answer Sets</i> [Sakama 2005]	✓	✗	✓	✓	✓	✓	✗	✗	✗
<i>LAS</i> [Law et al 2014]	✓	✓	✓	✗	✓	✓	✗	✗	✓
<i>LOAS</i> [Law et al 2015]	✓	✓	✓	✗	✓	✓	✓	✗	✓
<i>Context Dependent LOAS</i>	✓	✓	✓	✗	✓	✓	✓	✓	✓



Current Work

- ▶ Improve the scalability of ILASP for tasks with:
 - ▶ Noisy examples
 - ▶ Large hypothesis spaces



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- ▶ ILASP2 and ILASP2i are available to download from <https://www.doc.ic.ac.uk/~m11909/ILASP>

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For example, we may wish to learn that when it is raining a user prefers to take the bus; otherwise, they prefer to walk.

$$E^+ = \left\{ \begin{array}{l} \langle \text{"take bus"}, \{1\{\text{rain, snow}\}1.\} \rangle, \\ \langle \text{"walk"}, \{\} \rangle \end{array} \right\}, \quad E^- = \left\{ \begin{array}{l} \langle \text{"walk"}, \{\text{rain.}\} \rangle, \\ \langle \text{"take bus"}, \{\} \rangle \end{array} \right\}$$



ILASP2i

```
1: procedure ILASP2I( $\langle B, S_M, E \rangle$ )
2:   Relevant =  $\langle \emptyset, \emptyset, \emptyset, \emptyset \rangle$ ; H =  $\emptyset$ ;
3:   re = findRelevantExample( $\langle B, S_M, E \rangle, H$ );
4:   while re  $\neq$  nil do
5:     Relevant  $\ll$  re;
6:     H = ILASP2( $\mathcal{T}_{LOAS}(\langle B, S_M, Relevant \rangle)$ );
7:     if (H == nil) return UNSATISFIABLE;
8:     else re = findRelevantExample( $\langle B, S_M, E \rangle, H$ );
9:   end while
10:  return H;
```

Theorem 4

ILASP2i is sound for any well defined $ILP_{LOAS}^{context}$ task, and returns an optimal solution if one exists.

Journey Preference Experiments

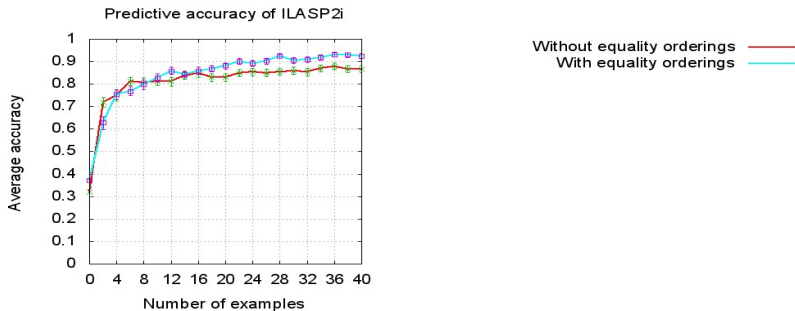


Figure : average accuracy of ILASP2i



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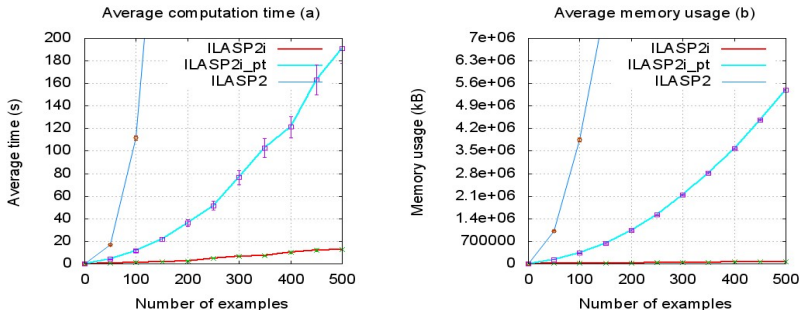


Figure : (a) the average computation time and (b) the memory usage of ILASP2, ILASP2i and ILASP2i_pt for learning journey preferences.



Hamilton Experiment

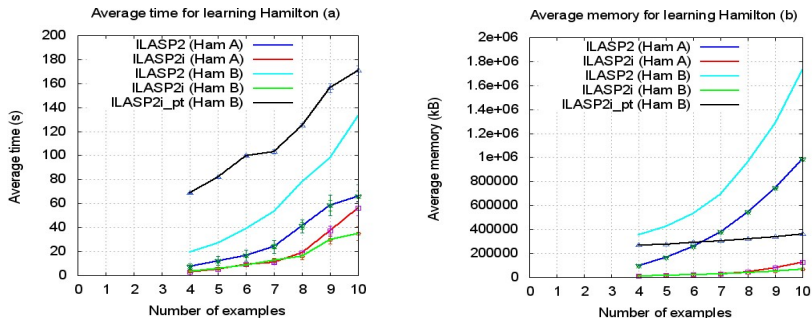







Figure : (a) the average computation time and (b) the memory usage of ILASP2, ILASP2i and ILASP2i_pt for Hamilton A and B.



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