

## COMP50006 Compilers - Exercise 4: Register allocation using graph colouring

### Introduction

The idea of using graph colouring for register allocation is covered at the end of Chapter 5 of the lecture notes. However, a good way to understand it is to work through this exercise.

Consider the following sequence of assignments:

```
S1:  A = 100;
P1:
S2:  B = 200;
P2:
S3:  C = A + B;
P3:
S4:  D = A * 2;
P4:
S5:  E = B * 2;
P5:
S6:  F = D - C;
P6:
S7:  G = E + F;
P7:
```

We are interested in using registers for all the variables in this code sequence. Notice that we can minimise the number of registers needed by reusing them.

For example, A and F could both be stored in the same register. We don't need a register for F until after the last statement to use A. There are several such instances in this sequence.

### Definition: live range

The *live range* of a variable is the set of program *points* *after* which the variable must be safely stored.

*Example 1:* The live range of A consists of {P1, P2, P3}.

*Example 2:* The live range of D consists of {P4, P5}

*Example 3:* The live range of F consists of {P6}.

**Subtlety:** Can the same register be used for both D and A?

The answer is yes: storage for D is only needed *after* the value of A has been read. The two live ranges do not intersect.

(as we will see later,  $A \in \text{liveIn}(S4)$ , and  $D \in \text{liveOut}(S4)$ ).

### Definition: interference

Two variables *interfere* if their live ranges overlap.

*Example 1:* The live ranges of A and F do not overlap.

*Example 2:* The live ranges of A and B do overlap.

*Example 3:* The live ranges of A and D do not overlap.

### Definition: interference graph

The interference graph for a program consists of

- *nodes* for each of the variables which have to be allocated to a register (in this example {A, B, C, D, E, F, G}), and
- *arcs* between each pair of nodes whose live ranges overlap.

### Definition: Colouring

A graph colouring is an assignment of colours to nodes. A graph colouring is valid if no pair of nodes which are linked by an arc carry the same colour.

### Exercise 4.1: Simple example

Construct the interference graph for the variables A, B, C, D, E, F and G in the example program fragment above. Colour the graph using the minimum possible number of colours, and use this colouring to assign each variable to a register. Give the final code after register allocation.

### Exercise 4.2: Register allocation using graph colouring, real example

Consider the following program fragment:

```
VAR A : ARRAY [0..99] OF INTEGER;

PROCEDURE P(i, j, size : INTEGER)
VAR k, tmp : INTEGER;
BEGIN
  FOR k := 0 TO size-1 DO
    tmp := A[i+k];
    A[i+k] := A[j+k];
    A[j+k] := tmp;
  END
END
```

The compiler's intermediate representation of the body of the procedure is as follows:

```
      t1 := size-1
      k := 0
L1:    cmp k,t1
      bgt End
      t2 := Address(A)+i
      t3 := t2+k
      tmp := LoadIndirect(t3)
      t4 := Address(A)+j
      t5 := t4+k
      t6 := LoadIndirect(t5)
      StoreIndirect(t6, t3)
      StoreIndirect(tmp, t5)
      k := k+1
      jmp L1
End:
```

1. Construct the register interference graph for the variables t1, t2, t3, t4, t5, t6, k and tmp.
2. Show how the interference graph colouring algorithm can be used to minimise the number of registers needed in this procedure.
3. What other possible optimisations are possible in this procedure? Write very brief notes on how such optimisations might be implemented.